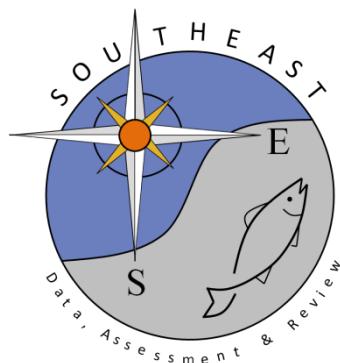


# **The Beaufort Assessment Model (BAM) with application to Gulf menhaden: mathematical description, implementation details, and computer code**

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**SEDAR32A-RW-01**

Submitted: 9 August 2013



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Please cite this document as:

Sustainable Fisheries Branch, National Marine Fisheries Service, Southeast Fisheries Science Center – Beaufort Lab. 2013. The Beaufort Assessment Model (BAM) with application to Gulf menhaden: mathematical description, implementation details, and computer code. SEDAR32A-RW01. SEDAR, North Charleston, SC. 37 pp.

The Beaufort Assessment Model (BAM) with application to Gulf menhaden:  
mathematical description, implementation details, and computer code

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## 1 Overview

The primary model in this assessment was the Beaufort assessment model (BAM), which applies a statistical catch-age formulation. The model was implemented with the AD Model Builder software (Fournier et al. 2012), and its structure and equations are detailed herein. In essence, a statistical catch-age model simulates a population forward in time while including fishing processes (Quinn and Deriso 1999; Shertzer et al. 2008). Quantities to be estimated are systematically varied until characteristics of the simulated population match available data on the real population. Statistical catch-age models share many attributes with ADAPT-style tuned and untuned VPAs.

The method of forward projection has a long history in fishery models. It was introduced by Pella and Tomlinson (1969) for fitting production models and has been used by many applications including by Fournier and Archibald (1982), by Deriso et al. (1985) in their CAGEAN model, and by Methot (1989; 2009) in his Stock Synthesis model. The catch-age model of this assessment is similar in structure to the CAGEAN and Stock Synthesis models. Versions of this assessment model have been used in previous SEDAR assessments in the U.S. South Atlantic, such as red porgy, black sea bass, snowy grouper, gag grouper, greater amberjack, vermillion snapper, Spanish mackerel, red grouper, red snapper, tilefish, and Atlantic menhaden assessments.

## 2 Model configuration and equations

Model equations are detailed in Table 2.1, and AD Model Builder code is supplied in Appendix A. A general description of the assessment model follows.

**Stock dynamics** In the assessment model, new biomass was acquired through growth and recruitment, while abundance of existing cohorts experienced exponential decay from fishing and natural mortality. The population was assumed closed to immigration and emigration. The model included age classes  $0 - 4^+$ , where the oldest age class  $4^+$  allowed for the accumulation of fish (i.e., plus group).

**Initialization** Initial (1977) abundance at age was computed in the model assuming an equilibrium age structure and fishing mortality rate. The equilibrium age structure was computed for ages  $1 - 4^+$  based on natural and fishing mortality ( $F$ ), where  $F$  was set equal to the geometric mean fishing mortality from the first three assessment years (1977-1979). In addition, deviations from the equilibrium age structure were also estimated for each age 1 through  $4^+$ . The deviations were informed by the age composition data available in the first year of the assessment. Finally, initial age-0 abundance was computed in the model using the Beverton–Holt stock-recruitment curve plus an estimated annual recruitment deviation.

**Natural mortality rate** The natural mortality rate ( $M$ ) was assumed constant over time, but decreasing with age. The form of  $M$  as a function of age was based on Lorenzen (1996). The Lorenzen (1996) approach inversely relates the natural mortality at age  $M_a$  to mean weight at age  $W_a$  by the power function  $M_a = \alpha W_a^\beta$ , where  $\alpha$  is a scale parameter and  $\beta$  is a shape parameter. Lorenzen (1996) provided point estimates of  $\alpha$  and  $\beta$  for oceanic fishes, which were used for this assessment. The Lorenzen version of  $M$  was scaled to 1.10 at age-2, which is the estimated natural mortality rate based on the tagging study completed by Arhenholz.

**Growth** Mean size at age of the fishery and the population (fork length, FL) were modeled with the von Bertalanffy equation, and weight at age of the fishery and the population were modeled as a function of FL. Weight at age of the fishery and population were estimated during the assessment process and were treated as an input to the model. For fitting length composition data, a von Bertalanffy growth curve was estimated within the model where the distribution of size at age was assumed normal with a constant coefficient of variation (CV) estimated by the assessment model.

**Female maturity** Females were modeled to be fully mature at ages-2+ and not mature for ages-0 and -1.

**Spawning stock** Spawning stock was modeled using total fecundity (mature ova) at the time of peak spawning. For Gulf menhaden, peak spawning was considered to occur January 1.

**Recruitment** Expected recruitment of age-0 fish was predicted from spawning stock in fecundity using the Beverton–Holt spawner-recruit model. Annual variation in recruitment was assumed to occur with lognormal deviations for the years 1977–2011.

**Landings** The model included one time series of combined landings from 1977–2011. Reduction, bait, and recreational landings were pooled outside of the model and were entered as one data stream. Landings consisted of mostly commercial reduction fishery landings, which made up about 99% of the total landings. The landings were modeled with the Baranov catch equation (Baranov 1918) and were fitted in units of weight (1,000s metric tons).

**Fishing Mortality** For the time series of removals, the assessment model estimated an annual full fishing mortality rate ( $F$ ). Age-specific rates were then computed as the product of full  $F$  and selectivity at age.

**Selectivities** The selectivity curve for the gill net survey CPUE series was estimated using a parametric approach, while the selectivity for the seine CPUE and the landings were not. The parametric approach applies plausible structure on the shape of the curve and achieves greater parsimony than occurs with unique parameters for each age. Selectivity of the gill net index was modeled as flat-topped, using a two parameter logistic function. The selectivity for the recruitment index based on the state seine data was fixed with selectivity of age-0 being 1.0, while the selectivity of all the other ages was 0.0. The selectivity for the fishery was estimated for age-1 but was fixed for all other ages. Specifically, the selectivity was fixed at 0.0 for age-0, 1.0 for age-2, and 0.35 for ages-3 and -4.

**Indices of abundance** The model was fit to two indices of relative abundance: the Louisiana gill net CPUE index (1988–2011) and the seine recruitment CPUE index (1996–2010). Predicted indices were conditional on selectivities and were computed from abundance at the midpoint of the year for the gill net index and for April 1 for the seine index.

**Catchability** In the BAM, catchability scales indices of relative abundance to estimated population abundance at large. Several options for time-varying catchability can be implemented in the BAM following recommendations of the 2009 SEDAR procedural workshop on catchability (SEDAR Procedural Guidance 2009). Parameters for each option could be estimated or fixed based on *a priori* considerations. For the base model, the AW assumed time-invariant catchability for both the gill net and seine indices. Because both of these indices are based on consistent, fishery-independent sampling, a constant catchability value was a reasonable assumption.

**Biological reference points** No benchmarks have been formally adopted for Gulf menhaden. The Menhaden Advisory Committee is discussing goals and objectives for the fishery, after which benchmarks can be discussed. Therefore, for the current assessment, a suite of benchmark options was provided. None of the benchmark options is preferred.

Biological reference points (benchmarks) were calculated based on maximum sustainable yield ( $MSY$ ) estimates from the Beverton–Holt spawner-recruit model with bias correction (expected values in arithmetic space). However, the value of  $MSY$  that resulted was infinite. This characteristic was explored and appears to be infinite because Gulf menhaden are not harvested until after they mature and reproduce. Additional benchmark options were therefore provided and included  $F_{MED}$  and a series of benchmarks based on spawners per recruit. In this assessment, spawning stock measures total fecundity in mature ova. These benchmarks are conditional on the estimated selectivity functions.

**Fitting criterion** The fitting criterion was a penalized likelihood approach in which observed landings were fit closely, and observed composition data and abundance indices were fit to the degree that they were compatible. Landings and index data were fitted using lognormal likelihoods. Length and age composition data were fitted using robust multinomial likelihoods.

The model includes the capability for each component of the likelihood to be weighted by user-supplied values (for instance, to give more influence to stronger data sources). For data components, these weights were applied by either adjusting CVs (lognormal components) or adjusting effective sample sizes (multinomial components). In this application to Gulf menhaden, the CV of removals (in arithmetic space) was assumed equal to 0.04, to achieve a close fit to this time series yet allow some imprecision. In practice, the small CVs are a matter of computational

convenience, as they help achieve the desired result of close fits to the landings, while avoiding having to solve the Baranov equation iteratively. Weights on other data components (indices, age and length compositions) were adjusted iteratively, starting from initial weights as follows. The CVs of indices were set equal to the values estimated by jackknifing as reported in the stock assessment report. Effective sample sizes of the annual length compositions were assumed equal to the annual number of sets sampled. Number of annual trips sampled was the effective sample size for the age composition data. These initial weights were then adjusted until standard deviations of normalized residuals (SDNRs) were near 1.0 (SEDAR24-RW03, SEDAR25-RW05, Francis 2011). Computed SDNRs accounted for potential correlations in the composition data (TA1.8 in Table A1 of (Francis 2011)).

The compound objective function included some penalties on the recruitment time series based on Beddington and Cooke (1983) and Mertz and Myers (1996)]. Penalties or priors were applied to maintain parameter estimates near reasonable values, and to prevent the optimization routine from drifting into parameter space with negligible gradient in the likelihood.

**Model testing** Experiments with a reduced model structure indicated that parameters estimated from the BAM were unbiased and could be recovered from simulated data. Further, the general model structure has been through multiple SEDAR reviews. As an additional measure of quality control, Gulf menhaden code and input data were examined for accuracy by multiple analysts. This combination of testing and verification procedures suggest that the assessment model is implemented correctly and can provide an accurate assessment of Gulf menhaden stock dynamics.

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*Table 2.1. General definitions, input data, population model, and negative log-likelihood components of the statistical catch-age model applied to Gulf menhaden. Hat notation ( $\hat{}$ ) indicates parameters estimated by the assessment model, and breve notation ( $\breve{}$ ) indicates estimated quantities whose fit to data forms the objective function.*

| Quantity                         | Symbol                  | Description or definition   |
|----------------------------------|-------------------------|---|
| <b>General Definitions</b>       |                         |   |
| Index of years                   | $y$                     | $y \in \{1977 \dots 2011\}$   |
| Index of ages                    | $a$                     | $a \in \{0, 1 \dots A\}$ , where $A = 4^+$  |
| Index of length bins             | $l$                     | $l \in \{1, 2 \dots 15\}$   |
| Length bins                      | $l'$                    | $l' \in \{85, 95, \dots, 295\text{mm}\}$ , with midpoint of 10 mm bin used to match length compositions. Largest 7 length bins ( $FL \geq 225$ mm) treated as a plus group, but retained for weight calculations.                       |
| Index of fishery                 | $f$                     | $f$ is the combined commercial reduction, bait, and recreational landings   |
| Index of CPUE                    | $u$                     | $u \in \{1, 2\}$<br>where 1 = Louisiana gill net index, 2 = seine index   |
| <b>Input Data</b>                |                         |   |
| Observed length compositions     | $p_{(u=1),l,y}^\lambda$ | Proportional contribution of length bin $l$ in year $y$ to index $u = 1$  |
| Observed age compositions        | $p_{(f),a,y}^\alpha$    | Proportional contribution of age class $a$ in year $y$ to the fishery $f$   |
| Ageing error matrix              | $\mathcal{E}$           | Estimated from a comparison between scales and otoliths.  |
| Length comp. sample sizes        | $n_{(u=1),y}^\lambda$   | Effective number of length samples collected in year $y$ from an index $u$  |
| Age comp. sample sizes           | $n_{(f),y}^\alpha$      | Effective number of age samples collected in year $y$ from the fishery $f$  |
| Observed landings                | $L_{f,y}$               | Reported landings in year $y$ from the fishery $f$ . Landings are reported in 1000s of metric tons  |
| CVs of landings                  | $c_{f,y}^L$             | Assumed 0.04 in arithmetic space  |
| Observed abundance indices       | $U_{u,y}$               | $u = 1$ , Louisiana gill net index (numbers), $y \in \{1988 \dots 2011\}$<br>$u = 2$ , seine index (numbers), $y \in \{1996 \dots 2010\}$<br>Annual values estimated from delta-lognormal GLM. Each time series was scaled to its mean. |
| CVs of abundance indices         | $c_{u,y}^U$             | $u = \{1, 2\}$ as above.  |
| Natural mortality rate           | $M_a$                   | Function of weight at age ( $w_a$ ): $M_a = \alpha w_a^\beta$ , with estimates of $\alpha$ and $\beta$ from Lorenzen (1996). Lorenzen $M_a$ then rescaled such that age-2 mortality was 1.10 as estimated in the tagging study.         |
| <b>Population Model</b>          |                         |   |
| Proportion female at age         | $\rho_a$                | Considered constant (50:50) across years and ages   |
| Proportion females mature at age | $m_a$                   | Increasing with age $\{0, 0, 1 \dots, 1\}$ for ages $0 - 4^+$ ; assumed constant across years.  |

Table 2.1. (continued)

| Quantity                               | Symbol              | Description or definition   |
|--|---------------------|---|
| Spawning date                          | $t_{\text{spawn}}$  | Fraction denoting the proportional time of year when spawning occurs. Set to 0.0 for Gulf menhaden by assuming peak spawning occurs January 1.  |
| Annual fecundity at age                | $\mathcal{F}_a$     | $\mathcal{F}_a = 0.000051604\ell_a^{3.87751629}$<br>based on equation provided in Lewis and Roithmayr and was a model input   |
| Mean length at age for the population  | $l_a$               | Fork length (January 1); $l_a = L_\infty(1 - \exp[-K(a - t_0)])$<br>where $K$ , $L_\infty$ , and $t_0$ are parameters estimated by the DW   |
| Mean length at age for the fishery     | $l_a^f$             | Fork length (midyear); $l_a^f = L_\infty(1 - \exp[-K(a - t_0 + 0.5)])$<br>where $K$ , $L_\infty$ , and $t_0$ are parameters estimated in the assessment model and used for the age-length transition for the length compositions  |
| CV of $l_a$                            | $\hat{c}_a^\lambda$ | Estimated coefficient of variation of growth, assumed constant across ages  |
| SD of $l_a$                            | $\sigma_a^\lambda$  | Standard deviation of growth, assumed constant across ages.   |
| Age-length conversion of population    | $\psi_{a,l}^u$      | $\psi_{a,l}^u = \frac{1}{\sqrt{2\pi}(\sigma_a^\lambda)} \frac{\exp[-(l_l' - l_a)^2]}{(2(\sigma_a^\lambda)^2)}$ , the Gaussian density function.<br>Matrix $\psi^u$ is rescaled to sum to one within ages, with the largest size a plus group. This matrix is constant across years. |
| Individual weight at age of population | $w_a$               | Computed from length at age by<br>$w_a = \theta_1 l_a^{\theta_2}$<br>where $\theta_1$ and $\theta_2$ are parameters from the DW   |
| Individual weight at age of landings   | $w_{(f),a,y}^L$     | Computed from length at age by $w_{(f),a,y}^L = \theta_1 (\xi_{(f),a,y}^L)^{\theta_2}$ .<br>With weight at age of landings being a model input.   |
| Index selectivity                      | $s_{(u),a}$         | $s_{(u),a} = \frac{1}{1 + \exp[-\hat{\eta}_{(u)}(a - \hat{\alpha}_{(u)})]}$<br>where $\hat{\eta}_{(u)}$ and $\hat{\alpha}_{(u)}$ are estimated parameters for $u=1$ . For $u=2$ , the selectivity was 1.0 for age-0 and 0.0 for all other ages.                                     |
| Fishery selectivity                    | $s_{(f),a}$         | $s_{(f),a} = \begin{cases} s_{f,0} & \text{was fixed at 0.0} \\ s_{f,1} & \text{was estimated} \\ s_{f,2} & \text{was fixed at 1.0} \\ s_{f,3} & \text{was fixed at 0.35} \\ s_{f,4+} & \text{was fixed at 0.35} \end{cases}$   |
| Fishing mortality rate of landings     | $F_{f,a,y}$         | $F_{f,a,y} = s_{f,a,y} \hat{F}_{f,y}$<br>where $\hat{F}_{f,y}$ is an estimated fully selected fishing mortality rate by fishery   |
| Total fishing mortality rate           | $F_{a,y}$           | $F_{a,y} = \sum_f F_{f,a,y}$  |
| Total mortality rate                   | $Z_{a,y}$           | $Z_{a,y} = M_a + F_{a,y}$   |

Table 2.1. (continued)

| Quantity  | Symbol         | Description or definition  |
|---|----------------|--|
| Abundance at age  | $N_{a,y}$      | $N_{0,1977} = \frac{\hat{R}_0(0.8\varsigma h\phi_{init} - 0.2\phi_0(1-h))}{(h-0.2)\phi_{init}} \exp(\hat{R}_y)$ $\hat{N}_{1+,1977} \exp(\hat{N}_a)$ <p>equilibrium conditions expected given assumptions about initial fishing mortality (described below), which includes an estimated deviation from the equilibrium age structure for each age</p> $N_{0,y+1} = \frac{0.8\hat{R}_0 h S_y}{0.2\phi_0 \hat{R}_0 (1-h) + (h-0.2) S_y} \exp(\hat{R}_{y+1})$ $N_{a+1,y+1} = N_{a,y} \exp(-Z_{a,y}) \quad \forall a \in (0 \dots A-1)$ $N_{A,y} = N_{A-1,y-1} \frac{\exp(-Z_{A-1,y-1})}{1 - \exp(-Z_{A,y-1})}$ <p><math>\hat{R}_0</math> (asymptotic maximum recruitment) is an estimated parameter of the spawner-recruit curve, and <math>\hat{R}_y</math> are estimated annual recruitment deviations in log space for 1977-2011. The bias correction is <math>\varsigma = \exp(\sigma_R^2/2)</math>, where <math>\sigma_R^2</math> was fixed at 0.6 and was the variance of recruitment deviations. In the SEDAR-32A base run, <math>h=0.75</math> was a fixed parameter. Quantities <math>\phi_0</math>, <math>\phi_{init}</math>, and <math>S_y</math> are described below.</p> |
| Abundance at age (mid-year)                               | $N'_{a,y}$     | Used to match to the gill net index of abundance<br>$N'_{a,y} = N_{a,y} \exp(-Z_{a,y}/2)$  |
| Abundance at age at time of spawning                      | $N''_{a,y}$    | Assumed in January 1 to correspond with peak spawning<br>$N''_{a,y} = \exp(-t_{spawn} Z_{a,y}) N_{a,y}$  |
| Unfished abundance at age per recruit at time of spawning | $NPR_a$        | $NPR_1 = 1 \times \exp(-t_{spawn} M_1)$ $NPR_{a+1} = NPR_a \exp[-(M_a(1-t_{spawn}) + M_{a+1}t_{spawn})] \quad \forall a \in (1 \dots A-1)$ $NPR_A = \frac{NPR_{A-1} \exp[-(M_{A-1}(1-t_{spawn}) + M_A t_{spawn})]}{1 - \exp(-M_A)}$  |
| Initial abundance at age per recruit at time of spawning  | $NPR_a^{init}$ | Same calculations as for $NPR_a$ , but including fishing mortality (see $Z^{init}$ below).   |
| Unfished spawning biomass per recruit                     | $\phi_0$       | $\phi_0 = \sum_{a=0}^A NPR_a \rho_a m_a \mathcal{F}_a$ <p>In units of fecundity</p>  |
| Initial spawning biomass per recruit                      | $\phi_{init}$  | $\phi_{init} = \sum_{a=0}^A NPR_a^{init} \rho_a m_a \mathcal{F}_a$ <p>In units of fecundity</p>  |
| Spawning biomass  | $S_y$          | $\sum_{a=1}^A N''_{a,y} \rho_a m_a \mathcal{F}_a$ <p>Spawning biomass is in units of total fecundity</p>   |
| Initialization mortality at age                           | $Z_a^{init}$   | $Z_a^{init} = M_a + s_a^{init} F^{init}$ <p>where <math>F^{init}</math> is an initialization <math>F</math> assumed to be the geometric mean of <math>F</math> from the first three assessment years (1977-1979) and <math>s_a^{init}</math> is the commercial selectivity for these three years.</p>  |
| Initial equilibrium abundance at age                      | $N_a^{eq}$     | Equilibrium age structure given $Z_a^{init}$   |
| Population biomass  | $B_y$          | $B_y = \sum_a N_{a,y} w_a$   |
| Landings at age in numbers                                | $L'_{f,a,y}$   | $L'_{f,a,y} = \frac{F_{f,a,y}}{Z_{a,y}} N_{a,y} [1 - \exp(-Z_{a,y})]$  |

Table 2.1. (continued)

| Quantity  | Symbol                       | Description or definition   |
|---|------------------------------|---|
| Landings at age in weight                                 | $L''_{f,a,y}$                | $L''_{f,a,y} = w^L_{f,a,y} L'_{f,a,y}$  |
| Index catchability  | $\hat{q}_u$                  | estimated constant catchability for each index $u$  |
| Predicted landings  | $\check{L}_{f,y}$            | $\check{L}_{f,y} = \sum_a L'_{f,a,y}$   |
| Predicted length compositions of fishery independent data | $\check{p}_{u,l,y}^\lambda$  | $\check{p}_{u,l,y}^\lambda = \frac{\sum_a \psi_{a,l} s_{u,a,y} N'_{a,y}}{\sum_a s_{u,a,y} N'_{a,y}}$  |
| Predicted age compositions of fishery                     | $\check{p}_{(f),a,y}^\alpha$ | $\check{p}_{(f),a,y}^\alpha = \frac{\varepsilon L'_{(f),a,y}}{\sum_a L'_{(f),a,y}}$ this formulation accounts for ageing error              |
| Predicted CPUE  | $\check{U}_{u,y}$            | $\check{U}_{u,y} = \hat{q}_u \sum_a N'_{a,y} s_{u,a}$<br>where $s_{u,a}$ is the selectivity of index $u$ in the year corresponding to $y$ . |

Table 2.1. (continued)

| Quantity                               | Symbol      | Description or definition  |
|--|-------------|--|
| <b>Objective Function</b>              |             |  |
| Robust multinomial length compositions | $\Lambda_1$ | $\Lambda_1 = \sum_u \sum_y 0.5 \log(E') - \log \left[ \exp \left( -\frac{(p_{(u),l,y}^\lambda - \check{p}_{(u),l,y}^\lambda)^2}{2E' / (n_{(u),y}^\lambda \omega_{(u)}^\lambda)} \right) + x \right]$ <p>where <math>E' = [(1 - p_{(u),l,y}^\lambda)(p_{(u),l,y}^\lambda) + \frac{0.1}{mbin}]</math>, <math>mbin</math> is the number of length bins, <math>\omega_{(u)}^\lambda</math> is a preset weight (selected by iterative re-weighting) and <math>x = 1e-5</math> is an arbitrary value to avoid log zero. Bins are 10 mm wide.</p>   |
| Robust multinomial age compositions    | $\Lambda_2$ | $\Lambda_2 = \sum_f \sum_y 0.5 \log(E') - \log \left[ \exp \left( -\frac{(p_{(f),a,y}^\alpha - \check{p}_{(f),a,y}^\alpha)^2}{2E' / (n_{(f),y}^\alpha \omega_{(f)}^\alpha)} \right) + x \right]$ <p>where <math>E' = [(1 - p_{(f),a,y}^\alpha)(p_{(f),a,y}^\alpha) + \frac{0.1}{mbin}]</math>, <math>mbin</math> is the number of age bins, <math>\omega_{(f)}^\alpha</math> is a preset weight (selected by iterative re-weighting) and <math>x = 1e-5</math> is an arbitrary value to avoid log zero.</p>  |
| Lognormal landings                     | $\Lambda_3$ | $\Lambda_3 = \sum_f \sum_y \frac{\left[ \log((L_{f,y}+x) / (\check{L}_{f,y}+x)) \right]^2}{2(\sigma_{f,y}^L)^2}$ <p>where <math>x = 1e-5</math> is an arbitrary value to avoid log zero or division by zero. Here, <math>\sigma_{f,y}^L = \sqrt{\log(1 + (c_{f,y}^L / \omega_f^L)^2)}</math>, with <math>\omega_f^L = 1</math> a preset weight.</p>  |
| Lognormal CPUE                         | $\Lambda_4$ | $\Lambda_4 = \sum_u \sum_y \frac{\left[ \log((U_{u,y}+x) / (\check{U}_{u,y}+x)) \right]^2}{2(\sigma_{u,y}^U)^2}$ <p>where <math>x = 1e-5</math> is an arbitrary value to avoid log zero or division by zero. Here, <math>\sigma_{u,y}^U = \sqrt{\log(1 + (c_{u,y}^U / \omega_u^U)^2)}</math>, with <math>\omega_u^U</math> a preset weight.</p>  |
| Lognormal recruitment deviations       | $\Lambda_5$ | $\Lambda_5 = \omega_5 \left[ \frac{[R_{1977} + (\hat{\sigma}_R^2 / 2)]^2}{2\hat{\sigma}_R^2} + \sum_{y>1978}^{2011} \frac{[(R_y - \hat{\varrho}R_{y-1}) + (\hat{\sigma}_R^2 / 2)]^2}{2\hat{\sigma}_R^2} + n \log(\hat{\sigma}_R) \right]$ <p>where <math>R_y</math> are recruitment deviations in log space, <math>n</math> is the number of years, <math>\omega_5 = 1</math> is a preset weight, <math>\hat{\varrho}</math> is the first-order autocorrelation, and <math>\hat{\sigma}_R^2</math> is the estimated recruitment variance (<math>\varrho = 0</math> in the SEDAR-32A base run).</p> |
| Total objective function               | $\Lambda$   | $\Lambda = \sum_{i=1}^5 \Lambda_i$ <p>Objective function minimized by the assessment model</p>   |

## **Appendix A AD Model Builder code to implement the Beaufort Assessment Model**





```

const double selpar_age0_cR_LD=set_sel_age0_cR(2); const double selpar_age0_cR_HI=set_sel_age0_cR(3); const double selpar_age0_cR_PH=set_sel_age0_cR(4);
const double selpar_age1_cR_LD=set_sel_age1_cR(2); const double selpar_age1_cR_HI=set_sel_age1_cR(3); const double selpar_age1_cR_PH=set_sel_age1_cR(4);
const double selpar_age2_cR_LD=set_sel_age2_cR(2); const double selpar_age2_cR_HI=set_sel_age2_cR(3); const double selpar_age2_cR_PH=set_sel_age2_cR(4);
const double selpar_age3_cR_LD=set_sel_age3_cR(2); const double selpar_age3_cR_HI=set_sel_age3_cR(3); const double selpar_age3_cR_PH=set_sel_age3_cR(4);
const double selpar_age4_cR_LD=set_sel_age4_cR(2); const double selpar_age4_cR_HI=set_sel_age4_cR(3); const double selpar_age4_cR_PH=set_sel_age4_cR(4);
const double selpar_age0_cR2_LD=set_sel_age0_cR2(2); const double selpar_age0_cR2_HI=set_sel_age0_cR2(3); const double selpar_age0_cR2_PH=set_sel_age0_cR2(4);
const double selpar_age1_cR2_LD=set_sel(sel_age1_cR2(2); const double selpar_age1_cR2_HI=set_sel(sel_age1_cR2(3); const double selpar_age1_cR2_PH=set_sel(sel_age1_cR2(4);
const double selpar_age2_cR2_LD=set_sel(sel_age2_cR2(2); const double selpar_age2_cR2_HI=set_sel(sel_age2_cR2(3); const double selpar_age2_cR2_PH=set_sel(sel_age2_cR2(4);
const double selpar_age3_cR2_LD=set_sel(sel_age3_cR2(2); const double selpar_age3_cR2_HI=set_sel(sel_age3_cR2(3); const double selpar_age3_cR2_PH=set_sel(sel_age3_cR2(4);
const double selpar_age4_cR2_LD=set_sel(sel_age4_cR2(2); const double selpar_age4_cR2_HI=set_sel(sel_age4_cR2(3); const double selpar_age4_cR2_PH=set_sel(sel_age4_cR2(4);
const double selpar_L50_gill_L0=set_selpar_L50_gill(2); const double selpar_slope_gill_L0=set_selpar_slope_gill(2); const double selpar_slope_gill_HI=set_selpar_slope_gill(3); const double selpar_slope_gill_PH=set_selpar_slope_gill(4);
const double log_q_gill_L0=set_log_q_gill(2); const double log_q_gill_HI=set_log_q_gill(3); const double log_q_gill_PH=set_log_q_gill(4);
const double log_q_seine_L0=set_log_q_seine(2); const double log_q_seine_HI=set_log_q_seine(3); const double log_q_seine_PH=set_log_q_seine(4);
const double log_avg_F_cR_LD=set_log_avg_F_cR(2); const double log_avg_F_cR_HI=set_log_avg_F_cR(3); const double log_avg_F_cR_PH=set_log_avg_F_cR(4);
//dev vectors
const double log_F_dev_cR_LD=set_log_F_dev_cR(1); const double log_F_dev_cR_HI=set_log_F_dev_cR(2); const double log_F_dev_cR_PH=set_log_F_dev_cR(3);
const double log_recDev_LD=set_log_recDev(1); const double log_recDev_HI=set_log_recDev(2); const double log_recDev_PH=set_log_recDev(3);
const double M_dev_LD=set_M_dev(1); const double M_dev_HI=set_M_dev(2); const double M_dev_PH=set_M_dev(3);
const double N_dev_LD=set_log_N_dev(1); const double N_dev_HI=set_log_N_dev(2); const double N_dev_PH=set_log_N_dev(3);

END_CALCS

//----Growth-----
init_bounded_number Linf(Linf_L0,Linf_HI,Linf_PH);
init_bounded_number K(K_L0,K_HI,K_PH);
init_bounded_number t0(t0_L0,t0_HI,t0_PH);
init_bounded_number len_cv_val(len_cv_L0,len_cv_HI,len_cv_PH);
vector Linf_out(1,8);
vector K_out(1,8);
vector t0_out(1,8);
vector len_cv_val_out(1,8);

vector meanlen_FL(1,nages); //mean fork length (mm) at age all fish
vector wgt_fish_mt(1,nages); //wgt in mt
vector wgt_spawn_mt(1,nages); //wgt in mt

matrix wholewgt_cR_mt(styr,endyr,1,nages); //whole wgt of cR landings in mt
vector lbins(1,nlenbins);

matrix lenprob(1,nages,1,nlenbins); //distn of size at age (age-length key, 1 cm bins) in population
matrix lenprob_plus(1,nages,1,nlenbins_plus); //used to compute mass in last length bin (a plus group)
matrix lenprob_all(1,nages,1,nlenbins_all); //extended lenprob
vector lenbins_all(1,nlenbins_all);

//matrices below are used to match length comps
matrix lenprob_gill(1,nages,1,nlenbins); //distn of size at age in gill nets

//matrices below pertain to the popn at large, used to compute mean weights
matrix lenprob_gill_all(1,nages,1,nlenbins_all); //distn of size at age in gill

// //init_bounded_dev_vector log_len_cv_dev(1,nages,-2,2,3)
// number log_len_cv
vector len_sd(1,nages);
vector len_cv(1,nages); //for fishgraph

//----Predicted length and age compositions
matrix pred_gill_lenc(1,nyr_gill_lenc,1,nlenbins);
matrix pred_cR_agec(1,nyr_cR_agec,1,nages);
matrix ErrorFree_cR_agec(1,nyr_cR_agec,1,nages);

//effective sample size applied in multinomial distributions
vector nsamp_gill_lenc_allyr(styr,endyr);
vector nsamp_cR_agec_allyr(styr,endyr);

//Nfish used in MCB analysis (not used in fitting)
vector nfish_gill_lenc_allyr(styr,endyr);
vector nfish_cR_agec_allyr(styr,endyr);

//Computed effective sample size for output (not used in fitting)
vector neff_gill_lenc_allyr_out(styr,endyr);
vector neff_cR_agec_allyr_out(styr,endyr);

//----Population-----
matrix N(styr,endyr+1,1,nages); //Population numbers by year and age at start of yr
matrix N_endyr(styr,endyr,1,nages); //Population numbers by year and age at mdpt of yr: used for comps and cpue
matrix N_spawn(styr,endyr,1,nages); //Population numbers by year and age at peaking spawning: used for SSB
//vector log_Nage_dev(2,nages);
init_bounded_dev_vector log_Nage_dev(2,nages,N_dev_LD,N_dev_HI,N_dev_PH);
vector log_Nage_dev_output(2,nages); //used in output. equals zero for first age
matrix B(styr,endyr+1,1,nages); //Population biomass by year and age at start of yr
vector totB(styr,endyr+1); //Total biomass by year
vector totN(styr,endyr+1); //Total abundance by year
vector SSB(styr,endyr+1); //Total spawning biomass by year (fecundity in mature ova)
vector rec(styr,endyr+1); //Recruits by year
vector pred_SPR(styr,endyr); //spawning biomass-per-recruit (lagged) for Fmed calcs
vector prop_f(1,nages); //Proportion female by age
vector maturity_f(1,nages); //Proportion of female mature at age
vector reprod(1,nages); //vector used to compute spawning biomass (fecundity)
matrix SSBatage(styr,endyr,1,nages);

//----Stock-Recruit Function (Beverton-Holt, steepness parameterization)-----
init_bounded_number log_RO(log_RO_L0,log_RO_HI,log_RO_PH); //log(virgin Recruitment)
vector log_RO_out(1,8);
number RO; //virgin recruitment

init_bounded_number steep(steep_L0,steep_HI,steep_PH); //steepness
vector steep_out(1,8);
init_bounded_number rec_sigma(rec_sigma_L0,rec_sigma_HI,rec_sigma_PH); //sd recruitment residuals
vector rec_sigma_out(1,8);

number rec_sigma_sq; //square of rec_sigma

```

```

number rec_logL_add; //additive term in -logL term

init_bounded_dev_vector log_rec_dev(styr_rec_dev,endyr_rec_dev,log_rec_dev_L0,log_rec_dev_HI,log_rec_dev_PH); //log recruitment deviations
vector log_rec_dev_output(styr,endyr+1); //used in output. equals zero except for yrs in log_rec_dev

number var_rec_dev; //variance of log recruitment deviations, from yrs with unconstrained S-R
number sigma_rec_dev; //sample SD of log residuals (may not equal rec_sigma)

number BiasCor; //Bias correction in equilibrium recruits
init_bounded_number R_autocorr(R_autocorr_L0,R_autocorr_HI,R_autocorr_PH);
vector R_autocorr_out(1,8);

number S0; //equal to spr_FO*RO = virgin SSB
number B0; //equal to bpr_FO*RO = virgin B
number R1; //Recruits in styr
number R_virgin; //unfinished recruitment with bias correction
vector SdS0(styr,endyr+1); //SSB / virgin SSB

//-----
//----Selectivity-----
//Commercial Reduction-----
matrix sel_cR(styr,endyr,1,nages);
init_bounded_number selpar_L50_cR(selpar_L50_cR_L0,selpar_L50_cR_HI,selpar_L50_cR_PH);
init_bounded_number selpar_slope_cR(selpar_slope_cR_L0,selpar_slope_cR_HI,selpar_slope_cR_PH);
init_bounded_number selpar_L502_cR(selpar_L502_cR_L0,selpar_L502_cR_HI,selpar_L502_cR_PH);
init_bounded_number selpar_slope2_cR(selpar_slope2_cR_L0,selpar_slope2_cR_HI,selpar_slope2_cR_PH);
vector selpar_L50_cR_out(1,8);
vector selpar_slope_cR_out(1,8);
vector selpar_L502_cR_out(1,8);
vector selpar_slope2_cR_out(1,8);

init_bounded_number sel_age0_cR_logit(selpar_age0_cR_L0,selpar_age0_cR_HI,selpar_age0_cR_PH); //cR selectivity at age in logit space
init_bounded_number sel_age1_cR_logit(selpar_age1_cR_L0,selpar_age1_cR_HI,selpar_age1_cR_PH);
init_bounded_number sel_age2_cR_logit(selpar_age2_cR_L0,selpar_age2_cR_HI,selpar_age2_cR_PH);
init_bounded_number sel_age3_cR_logit(selpar_age3_cR_L0,selpar_age3_cR_HI,selpar_age3_cR_PH);
init_bounded_number sel_age4_cR_logit(selpar_age4_cR_L0,selpar_age4_cR_HI,selpar_age4_cR_PH);
vector sel_age_cR_vec(1,nages);
number selpar_age0_cR;
number selpar_age1_cR;
number selpar_age2_cR;
number selpar_age3_cR;
number selpar_age4_cR;
vector selpar_age0_cR_out(1,8);
vector selpar_age1_cR_out(1,8);
vector selpar_age2_cR_out(1,8);
vector selpar_age3_cR_out(1,8);
vector selpar_age4_cR_out(1,8);

init_bounded_number sel_age0_cR2_logit(selpar_age0_cR2_L0,selpar_age0_cR2_HI,selpar_age0_cR2_PH); //cR selectivity at age in logit space-period 2
init_bounded_number sel_age1_cR2_logit(selpar_age1_cR2_L0,selpar_age1_cR2_HI,selpar_age1_cR2_PH);
init_bounded_number sel_age2_cR2_logit(selpar_age2_cR2_L0,selpar_age2_cR2_HI,selpar_age2_cR2_PH);
init_bounded_number sel_age3_cR2_logit(selpar_age3_cR2_L0,selpar_age3_cR2_HI,selpar_age3_cR2_PH);
init_bounded_number sel_age4_cR2_logit(selpar_age4_cR2_L0,selpar_age4_cR2_HI,selpar_age4_cR2_PH);
vector sel_age_cR2_vec(1,nages);
number selpar_age0_cR2;
number selpar_age1_cR2;
number selpar_age2_cR2;
number selpar_age3_cR2;
number selpar_age4_cR2;
vector selpar_age0_cR2_out(1,8);
vector selpar_age1_cR2_out(1,8);
vector selpar_age2_cR2_out(1,8);
vector selpar_age3_cR2_out(1,8);
vector selpar_age4_cR2_out(1,8);

//Gill net survey selectivity
matrix sel_gill(styr_gill_cpue,endyr_gill_cpue,1,nages);
init_bounded_number selpar_L50_gill(selpar_L50_gill_L0,selpar_L50_gill_HI,selpar_L50_gill_PH);
init_bounded_number selpar_slope_gill(selpar_slope_gill_L0,selpar_slope_gill_HI,selpar_slope_gill_PH);
vector selpar_L50_gill_out(1,8);
vector selpar_slope_gill_out(1,8);

//Weighted total selectivity-----
//effort-weighted, recent selectivities
vector sel_wgted_l(1,nages); //toward landings
vector sel_wgted_tot(1,nages);

//-----
//----CPUE Predictions-----
vector pred_gill_cpue(styr_gill_cpue,endyr_gill_cpue); //predicted gill net U
matrix N_gill(styr_gill_cpue,endyr_gill_cpue,1,nages); //used to compute gill net index
vector pred_seine_cpue(styr_seine_cpue,endyr_seine_cpue); //predicted seine index
vector N_seine(styr_seine_cpue,endyr_seine_cpue); //used to compute seine index

//---Catchability (CPUE q's)-----
init_bounded_number log_q_gill(log_q_gill_L0,log_q_gill_HI,log_q_gill_PH);
init_bounded_number log_q_seine(log_q_seine_L0,log_q_seine_HI,log_q_seine_PH);
vector log_q_gill_out(1,8);
vector log_q_seine_out(1,8);

//init_bounded_number q_rate(0.001,0.1,set_q_rate_phase);
number q_rate;
vector q_rate_fcn_gill(styr_gill_cpue,endyr_gill_cpue); //increase due to technology creep (saturates in 2003)
vector q_rate_fcn_seine(styr_seine_cpue,endyr_seine_cpue); //increase due to technology creep (saturates in 2003)

//init_bounded_number q_DD_beta(0.1,0.9,set_q_DD_phase);
number q_DD_beta;
vector q_DD_fcn(styr,endyr); //density dependent function as a multiple of q (scaled a la Katsukawa and Matsuda. 2003)
number BO_q_DD; //BO of ages q_DD_age plus
vector B_q_DD(styr,endyr); //annual biomass of ages q_DD_age plus

vector q_RW_log_dev_gill(styr_gill_cpue,endyr_gill_cpue-1);

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vector q_RW_log_dev_seine(styr_seine_cpue,endyr_seine_cpue-1);
vector q_gill(styr_gill_cpue,endyr_gill_cpue); //number q_gill;
vector q_seine(styr_seine_cpue,endyr_seine_cpue); //number q_seine;

//-----
//---Landings in numbers (total or 1000 fish) and in wgt (1000s mt)-----
matrix L_CR_num(styr,endyr,1,nages); //landings (numbers) at age
matrix L_CR_mt(styr,endyr,1,nages); //landings (mt) at age
vector pred_cr_L_knum(styr,endyr); //yearly landings in 1000 fish summed over ages
vector pred_cr_L_mt(styr,endyr); //yearly landings in 1000s mt summed over ages

matrix L_total_num(styr,endyr,1,nages); //total landings in number at age
matrix L_total_mt(styr,endyr,1,nages); //landings in mt at age
vector L_total_knum_yr(styr,endyr); //total landings in 1000 fish by yr summed over ages
vector L_total_mt_yr(styr,endyr); //total landings (1000s mt) by yr summed over ages

//----MSY calcs-----
number F_CR_prop; //proportion of F_sum attributable to cr
number F_temp_sum; //sum of geom mean Fsum's in last X yrs, used to compute F_fishery_prop

vector F_end(1,nages);
vector F_end_L(1,nages);
number F_end_apex;

number SSB_msy_out; //SSB (total fecundity) at msy
number F_msy_out; //F at msy
number msy_mt_out; //max sustainable yield (1000s mt)
number msy_knum_out; //max sustainable yield (1000 fish)
number B_msy_out; //total biomass at MSY
number R_msy_out; //equilibrium recruitment at F=Fmsy
number spr_msy_out; //spr at F=Fmsy

vector N_age_msy(1,nages); //numbers at age for MSY calculations: beginning of yr
vector N_age_msy_mdyr(1,nages); //numbers at age for MSY calculations: mdpt of yr
vector Z_age_msy(1,nages); //total mortality at age for MSY calculations
vector F_L_age_msy(1,nages); //fishing mortality landings (not discards) at age for MSY calculations
vector F_msy(1,n_iter_msy); //values of full F to be used in equilibrium calculations
vector spr_msy(1,n_iter_msy); //reproductive capacity-per-recruit values corresponding to F values in F_msy
vector R_eq(1,n_iter_msy); //equilibrium recruitment values corresponding to F values in F_msy
vector L_eq_mt(1,n_iter_msy); //equilibrium landings(1000s mt) values corresponding to F values in F_msy
vector L_eq_knum(1,n_iter_msy); //equilibrium landings(1000 fish) values corresponding to F values in F_msy
vector SSB_eq(1,n_iter_msy); //equilibrium reproductive capacity (fecundity) values corresponding to F values in F_msy
vector B_eq(1,n_iter_msy); //equilibrium biomass values corresponding to F values in F_msy

vector Pdf_msy(styr,endyr);
vector SdSSB_msy(styr,endyr+1);
number SdSSB_msy_end;
number Pdf_msy_end;
number Pdf_msy_end_mean; //geometric mean of last 3 yrs

vector wgt_wgted_L_mt(1,nages); //fishery-weighted average weight at age of landings
number wgt_wgted_L_denom; //used in intermediate calculations

number iter_inc_msy; //increments used to compute msy, equals 1/(n_iter_msy-1)

//----Fmed calcs-----
number quant_decimal;
number quant_diff;
number quant_result;

number R_med; //median recruitment for chosen benchmark years
vector R_temp(styr,endyr);
vector R_sort(styr,endyr);
number SPR_med; //median SSB/R (R = SSB year+1) for chosen SSB years
number SPR_75th;
vector SPR_temp(styr,endyr);
vector SPR_sort(styr,endyr);
number SSE_med; //SSB corresponding to SSB/R median and R median
number SSE_med_thresh; //SSB threshold
vector SPR_diff(1,n_iter_spr);
number SPR_diff_min;
number F_med; //Fmed benchmark
number F_med_target; //Fmed benchmark
number F_med_age2plus; //Fmed benchmark
number F_med_target_age2plus;
number L_med;
number L_med_target;

//-----Mortality-----
//Stuff immediately below used only if M is estimated
//init_bounded_number M_constant(0.1,0.2,1); //age-independent: used only for MSST
//vector Mscale_ages(1,max_obs_age);
//vector Mscale_len(1,max_obs_age);
//vector Mscale_wgt_g(1,max_obs_age);
//vector M_lorenzen(1,max_obs_age);
//number cum_surv_1plus;

vector M(1,nages); //age-dependent natural mortality
init_bounded_number M_constant(M_constant_L0,M_constant_HI,M_constant_PH); //age-independent: used only for MSST
vector M_constant_out(1,8);

//-----set up for M at age-1 to be estimated
init_bounded_dev_vector M_dev(styr_seine_cpue,endyr_seine_cpue,M_dev_L0,M_dev_HI,M_dev_PH); //M devs deviations
vector M_dev_output(styr_seine_cpue,endyr_seine_cpue);

matrix F(styr,endyr,1,nages); //Full fishing mortality rate by year
vector Fsum(styr,endyr); //Max across ages, fishing mortality rate by year (may differ from Fsum bc of dome-shaped sel)
//sdreport_vector fullF_sd(styr,endyr);
matrix Z(styr,endyr,1,nages);

```





```

sqrt2pi=sqrt(2.*3.14159265);
g2mt=0.000001;           //conversion of grams to metric tons
g2kg=0.001;              //conversion of grams to kg
mt2klb=2.0462;           //conversion of metric tons to 1000 lb
mt2lb=mt2lb*1000.0;      //conversion of metric tons to lb
g2klb=g2mt*mt2klb;      //conversion of grams to 1000 lb
dzero=0.00001;
huge_number=1.0e+10;

SSB_msy_out=0.0;

iter_inc_msy=max_F_spr_msy/(n_iter_msy-1);
iter_inc_spr=max_F_spr_msy/(n_iter_spr-1);

maturity_f=maturity_f_obs;
prop_f=prop_f_obs;

lbins=lenbins;

lenbins_all(1,nlenbins)=lenbins(1,nlenbins);
for (iyear=1;iyear<nlenbins_plus; iyear++) {lenbins_all(nlenbins+iyear)=lenbins_plus(iyear);}

//Fill in sample sizes of comps, possibly sampled in nonconsec yrs
//Used primarily for output in R object

nsamp_gill_lenc_allyr=missing;//"missing" defined in admb2r.cpp
nsamp_ch_agec_allyr=missing;

nfish_gill_lenc_allyr=missing;//"missing" defined in admb2r.cpp
nfish_ch_agec_allyr=missing;

for (iyear=1; iyear<=nyr_gill_lenc; iyear++)
  if (nsamp_gill_lenc(iyear)>minSS_gill_lenc)
    {nsamp_gill_lenc_allyr(yrs_gill_lenc(iyear))=nsamp_gill_lenc(iyear);
     nfish_gill_lenc_allyr(yrs_gill_lenc(iyear))=nfish_gill_lenc(iyear);}

for (iyear=1; iyear<=nyr_cr_agec; iyear++)
  if (nsamp_cr_agec(iyear)>minSS_cr_agec)
    {nsamp_cr_agec_allyr(yrs_cr_agec(iyear))=nsamp_cr_agec(iyear);
     nfish_cr_agec_allyr(yrs_cr_agec(iyear))=nfish_cr_agec(iyear);}

//fill in Fs for msy and per-recruit analyses
F_msy(1)=0.0;
for (ff=2;ff<=n_iter_msy;ff++)
{
  F_msy(ff)=F_msy(ff-1)+iter_inc_msy;
}
F_spr(1)=0.0;
for (ff=2;ff<=n_iter_spr;ff++)
{
  F_spr(ff)=F_spr(ff-1)+iter_inc_spr;
}

//fill in F's, Catch matrices, and log rec dev with zero's
F_cr.initialize();
L_cr_num.initialize();

F_cr_out.initialize();
sel_cr.initialize();
sel_gill.initialize();

log_rec_dev_output.initialize();
log_Nage_dev_output.initialize();
log_rec_devset.log_rec_dev_vals;

log_Nage_dev.initialize();
M_dev_output.initialize();

//##-->--><--><--><--><--><--><--><--><--><--><--><--><--><-->
//##-->--><--><--><--><--><--><--><--><--><--><--><--><--><--><-->
TOP_OF_MAIN_SECTION
time(&start);
armrbisize(20000000);
gradient_structure::set_MAX_NVAR_OFFSET(1600);
gradient_structure::set_GRADSTACK_BUFFER_SIZE(2000000);
gradient_structure::set_CMPDPII_BUFFER_SIZE(2000000);
gradient_structure::set_NUM_DEPENDENT_VARIABLES(10000);

//>--><--><--><-->
//##-->--><--><--><--><--><--><--><--><--><--><--><--><-->
PROCEDURE_SECTION

R0=exp(log_R0);

//cout<<"start"<<endl;

get_length_weight_at_age();
//cout << "got length, weight, fecundity transitions" << endl;
get_reprod();
//cout << "got repro stuff" << endl;
get_length_at_age_dist();
//cout << "got predicted length at age distribution" << endl;
get_weight_at_age_landings();
//cout << "got weight at age of landings" << endl;
get_spr_F0();
//cout << "got F0 spr" << endl;
get_selectivity();
//cout << "got selectivity" << endl;

```

```

get_mortality();
//cout << "got mortalities" << endl;
get_bias_corr();
//cout<< "got recruitment bias correction" << endl;
get_numbers_at_age();
//cout << "got numbers at age" << endl;
//exit(0);
get_landings_numbers();
//cout << "got catch at age" << endl;
get_landings_wgt();
//cout << "got landings" << endl;
get_catchability_fcns();
//cout << "got catchability_fcns" << endl;
get_indices();
//cout << "got indices" << endl;
get_length_comps();
//cout<< "got length comps"<< endl;
get_age_comps();
//cout<< "got age comps"<< endl;
evaluate_objective_function();
//cout << "objective function calculations complete" << endl;

FUNCTION get_length_weight_at_age
//compute mean length (mm FL) and weight (whole) at age
meanlen_FL=Linf*(1.0-mfexp(-K*(agebins-t0+0.5))); //fork length in mm
wgt_fish_mt=g2mt*wgt_start; //wgt in mt
wgt_spawn_mt=g2mt*wgt_spawn; //mt of whole wgt

FUNCTION get_reprod
//for reproductive capacity calcs
//product of sex ratio, maturity, and fecundity for gulf menhaden
reprod=elem_prod(elem_prod(prop_f,maturity_f),fec_at_age);

FUNCTION get_length_at_age_dist
//compute matrix of length at age, based on the normal distribution

for (iage=1;iage<=nages;iage++)
{
  //len_cv(iage)=mfexp(log_len_cv*log_len_cv_dev(iage));
  len_cv(iage)=len_cv_val;
  len_sd(iage)=meanlen_FL(iage)*len_cv(iage);

  //len_cv(iage)=len_cv_max-(len_cv_max-len_sd)/(1.0+mfexp(-len_cv_slope*(iage-len_cv_a50)));
  for (ilen=1;ilen<=nlenbins_all;ilen++)
  { lenprob_all(iage,ilen)=(mfexp(-(square(lenbins_all(ilen))-meanlen_FL(iage))/ (2.*square(len_sd(iage))))/(sqrt2pi*len_sd(iage)));
  }

  lenprob_all(iage)=sum(lenprob_all(iage)); //standardize to approximate integration and to account for truncated normal (i.e., no sizes<smallest)

  for (ilen=1;ilen<=nlenbins;ilen++) {lenprob(iage,ilen)=lenprob_all(iage,ilen);
  }
  for (ilen=nlenbins+1;ilen<=nlenbins_all;ilen++) {lenprob(iage)(nlenbins)=lenprob(iage)(nlenbins)+lenprob_all(iage)(ilen);
  } //plus group
}
//fishery specific length probs
lenprob_gill=lenprob;
lenprob_gill_all=lenprob_all;

FUNCTION get_weight_at_age_landings
for (iyear=styr; iyear<=endyr; iyear++)
{
  wholewgt_cR_mt(iyear)=wgt_fish_mt; //whole weight in mt
}

FUNCTION get_spr_F0
//at mdyr, apply half this yr's mortality, half next yr's
N_spr_F0(i)=1.0*mfexp(-1.0*M(i)*spawn_time_frac); //at peak spawning time
N_bpr_F0(i)=1.0; //at start of year
for (iage=2; iage<=nages; iage++)
{
  N_spr_F0(iage)=N_spr_F0(iage-1)*mfexp(-1.0*(M(iage-1)*(1.0-spawn_time_frac) + M(iage)*spawn_time_frac));
  N_bpr_F0(iage)=N_bpr_F0(iage-1)*mfexp(-1.0*(M(iage-1)));
}
N_spr_F0(nages)=N_spr_F0(nages)/(1.0-mfexp(-1.0*M(nages))); //plus group (sum of geometric series)
N_bpr_F0(nages)=N_bpr_F0(nages)/(1.0-mfexp(-1.0*M(nages)));

spr_F0=sum(elem_prod(N_spr_F0,reprod));
bpr_F0=sum(elem_prod(N_bpr_F0,wgt_spawn_mt));

FUNCTION get_selectivity
selpar_age0_ch=1.0/(1.0+mfexp(-sel_age0_cR_logit));
selpar_age1_ch=1.0/(1.0+mfexp(-sel_age1_cR_logit));
//selpar_age2_ch=1.0/(1.0+mfexp(-sel_age2_cR_logit));
selpar_age2_ch=1.0;
//selpar_age3_ch=1.0/(1.0+mfexp(-sel_age3_cR_logit));
selpar_age3_ch=0.35;
//selpar_age4_ch=1.0/(1.0+mfexp(-sel_age4_cR_logit));
selpar_age4_ch=0.35;
sel_age_cR_vec(1)=selpar_age0_cR;
sel_age_cR_vec(2)=selpar_age1_cR;
sel_age_cR_vec(3)=selpar_age2_cR;
sel_age_cR_vec(4)=selpar_age3_cR;
sel_age_cR_vec(5)=selpar_age4_cR;

selpar_age0_ch2=1.0/(1.0+mfexp(-sel_age0_cR2_logit));

```

```

selpar_age1_cR2=1.0/(1.0+mfexp(-sel_age1_cR2_logit));
//selpar_age2_cR2=1.0/(1.0+mfexp(-sel_age2_cR2_logit));
selpar_age2_cR2=1.0;
//selpar_age3_cR2=1.0/(1.0+mfexp(-sel_age3_cR_logit));
selpar_age3_cR2=0.35;
//selpar_age4_cR2=1.0/(1.0+mfexp(-sel_age4_cR_logit));
selpar_age4_cR2=0.35;
sel_age_cR2_vec(1)=selpar_age0_cR2;
sel_age_cR2_vec(2)=selpar_age1_cR2;
sel_age_cR2_vec(3)=selpar_age2_cR2;
sel_age_cR2_vec(4)=selpar_age3_cR2;
sel_age_cR2_vec(5)=selpar_age4_cR2;

for (iyear=styr; iyear<endyr_period1; iyear++)
{
  //sel_cR(iyear)=logistic(agebins, selpar_L50_cR, selpar_slope_cR);
  //sel_cR(iyear)=logistic_double(agebins, selpar_L50_cR, selpar_slope_cR, selpar_L502_cR, selpar_slope2_cR);
  sel_cR(iyear)=sel_age_cR_vec;
}

for (iyear=(endyr_period1+1); iyear<=endyr_period2; iyear++)
{
  //sel_cR(iyear)=logistic(agebins, selpar_L50_cR, selpar_slope_cR);
  //sel_cR(iyear)=logistic_double(agebins, selpar_L50_cR, selpar_slope_cR, selpar_L502_cR, selpar_slope2_cR);
  //sel_cR(iyear)=sel_age_cR_vec;
  sel_cR(iyear)=sel_age_cR_vec;
}

for (iyear=styr_gill_cpue; iyear<endyr_gill_cpue; iyear++)
{
  sel_gill(iyear)=logistic(agebins,selpar_L50_gill,selpar_slope_gill);
}

sel_initial=sel_cR(styr);

FUNCTION get_mortality
Fsum.initialize();
Fapex.initialize();
F.initialize();

//initialization F is avg from first 3 yrs of observed landings
log_F_dev_init_cR=sum(log_F_dev_cR(styr_cR_L,(styr_cR_L+2)))/3.0;

for (iyear=styr; iyear<endyr; iyear++)
{
  if(iyear>=styr_cR_L & iyear<=endyr_cR_L)
  {
    F_cR_out(iyear)=mfexp(log_avg_F_cR*log_F_dev_cR(iyear));
    F_cR(iyear)=sel_cR(iyear)*F_cR_out(iyear);
    Fsum(iyear)+=F_cR_out(iyear);
  }

  //Total F at age
  F(iyear)=F_cR(iyear); //first in additive series (NO +=)

  Fapex(iyear)=max(F(iyear));
  Z(iyear)=M+F(iyear);

  if(iyear>=styr_seine_cpue & iyear<=endyr_seine_cpue)
  {
    Z(iyear,2)=M(2)+M_dev(iyear)+F(iyear,2); //adds deviations in age-1 M
  }
}

} //end iyear

FUNCTION get_bias_corr
var_rec_dev=norm2(log_rec_dev(styr_rec_dev,endyr_rec_dev)-
  sum(log_rec_dev(styr_rec_dev,endyr_rec_dev))/nyrs_rec)
/(nyrs_rec-1.0);

rec_sigma_sq=square(rec_sigma);
if (set_BiasCor <= 0.0) {BiasCor=mfexp(rec_sigma_sq/2.0);} //bias correction
else {BiasCor=set_BiasCor;};

FUNCTION get_numbers_at_age
//Initialization

SO=spr_F0*RO; //virgin SSB

R_virgin=SR_eq_func(R0, steep, spr_F0, spr_F0, BiasCor, SR_switch);

BO=bpr_F0*R_virgin*1000000; //virgin biomass
BO_q_DD=R_virgin*sum(elem_prod(N_bpr_F0(set_q_DD_stage,nages),wgt_fish_mt(set_q_DD_stage,nages)));

F_initial=sel_cR(styr)*mfexp(log_avg_F_cR*log_F_dev_init_cR);
Z_initial=M*F_initial;

//Initial equilibrium age structure
N_spr_initial(1)=1.0*mfexp(-1.0*Z_initial(1)*spawning_time_frac); //at peak spawning time;
for (iage>2; iage<nages; iage++)
{
  N_spr_initial(iage)=N_spr_initial(iage-1)*
    mfexp(-1.0*(Z_initial(iage-1)*(1.0-spawning_time_frac) + Z_initial(iage)*spawning_time_frac));
}
N_spr_initial(nages)=N_spr_initial(nages)/(1.0-mfexp(-1.0*Z_initial(nages))); //plus group

spr_initial=sum(elem_prod(N_spr_initial,reprod)); //initial sbb for s-r curve

R1=SR_eq_func(R0, steep, spr_F0, spr_initial, BiasCor, SR_switch)*mfexp(log_rec_dev(styr_rec_dev));
//R1=SR_eq_func(R0, steep, spr_F0, spr_initial, BiasCor, SR_switch);
if(R1<0.0) {R1=1.0;} //Avoid negative popn sizes during search algorithm

//Compute equilibrium age structure for first year

```

```

N_initial_eq(i)=R1;
for (iage=2; iage<=nages; iage++)
{
  N_initial_eq(iage)=N_initial_eq(iage-1)*
    mfexp(-1.0*(Z_initial(iage-1)));
}
//plus group calculation
N_initial_eq(nages)=N_initial_eq(nages)/(1.0-mfexp(-1.0*Z_initial(nages))); //plus group

//Add deviations to initial equilibrium N
N(styr)(2,nages)=elem_prod(N_initial_eq(2,nages),mfexp(log_Nage_dev));

//if (styr==styr_rec_dev) {N(styr,1)=N_initial_eq(1)*mfexp(log_rec_dev(styr_rec_dev));}
//else {N(styr,1)=N_initial_eq(1);}
N(styr,1)=N_initial_eq(1);

N_mdry(styr)(1,nages)=elem_prod(N(styr)(1,nages),(mfexp(-1.*Z_initial(1,nages))*0.5)); //mid year
N_spawn(styr)(1,nages)=elem_prod(N(styr)(1,nages),(mfexp(-1.*Z_initial(1,nages))*spawn_time_frac)); //peak spawning time

SSB(styr)=sum(elem_prod(N_spawn(styr),reprod));
B_q_DD(styr)=sum(elem_prod(N(styr)(set_q_DD_stage,nages),wgt_fish_mt(set_q_DD_stage,nages)));

//Rest of years
for (iyear=styr; iyear<endyr; iyear++)
{
  if(iyear<(styr_rec_dev-1)||iyear>(endyr_rec_dev-1)) //recruitment follows S-R curve exactly
  {
    //N(iyear+1)=BiasCor*SR_func(R0, steep, spr_F0, SSB(iyear),SR_switch);
    N(iyear+1)(2,nages)+=elem_prod(N(iyear)(1,nages-1),(mfexp(-1.*Z(iyear)(1,nages-1)))); //plus group
    //N_mdry(iyear+1)=elem_prod(N(iyear+1)(1,nages),(mfexp(-1.*Z(iyear+1)(1,nages))*0.5));
    N_spawn(iyear+1)(1,nages)=elem_prod(N(iyear+1)(1,nages),(mfexp(-1.*Z(iyear+1)(1,nages))*spawn_time_frac)); //peak spawning time
    SSB(iyear+1)=sum(elem_prod(N_spawn(iyear+1),reprod));
    B_q_DD(iyear+1)=sum(elem_prod(N(iyear+1)(set_q_DD_stage,nages),wgt_fish_mt(set_q_DD_stage,nages)));
  }
  else //recruitment follows S-R curve with lognormal deviation
  {
    N(iyear+1,1)=BiasCor*SR_func(R0, steep, spr_F0, SSB(iyear+1),SR_switch);
    N_mdry(iyear+1)(1,nages)=elem_prod(N(iyear+1)(1,nages),(mfexp(-1.*Z(iyear+1)(1,nages))*0.5));
  }
}

//values for projections
N(endyr+1)(2,nages)+=elem_prod(N(endyr)(1,nages-1),(mfexp(-1.*Z(endyr)(1,nages-1))));
N(endyr+1,nages)+=N(iyear,nages)*mfexp(-1.*Z(endyr,nages)); //plus group
SSB(endyr+1)=sum(elem_prod(N(endyr+1),reprod));
N(endyr+1,1)=BiasCor*SR_func(R0, steep, spr_F0, SSB(endyr+1),SR_switch);

//Time series of interest
rec=column(N,1);
SdSO=SSB/S0;

for (iyear=styr; iyear<endyr; iyear++)
{
  pred_SPR(iyear)=SSB(iyear)/rec(iyear);
}

FUNCTION get_landings_numbers //Baranov catch eqn
for (iyear=styr; iyear<endyr; iyear++)
{
  for (iage=1; iage<=nages; iage++)
  {
    L_cR_num(iyear,iage)=N(iyear,iage)*F_cR(iyear,iage)*
      (1.-mfexp(-1.*Z(iyear,iage)))/Z(iyear,iage);
  }
  pred_cR_L_knum(iyear)=sum(L_cR_num(iyear)); //landings already being estimated in 1000s
}

FUNCTION get_landings_wgt
//----Predicted landings-----
for (iyear=styr; iyear<endyr; iyear++)
{
  L_cR_mt(iyear)=elem_prod(L_cR_num(iyear),wholewgt_cR_mt(iyear))*1000000; //in 1000 mt
  pred_cR_L_mt(iyear)=sum(L_cR_mt(iyear));
}

FUNCTION get_catchability_fcns
//Get rate increase if estimated, otherwise fixed above
if (set_q_rate_phase>0.0)
{
  for (iyear=styr_gill_cpue; iyear<=endyr_gill_cpue; iyear++)
  {
    if (iyear>2003)
      //q_rate_fcn_gill(iyear)=(1.0+q_rate)*q_rate_fcn_gill(iyear-1); //compound
      q_rate_fcn_gill(iyear)=(1.0+(iyear-styr_gill_cpue)*q_rate)*q_rate_fcn_gill(styr_gill_cpue); //linear
    if (iyear>2003) {q_rate_fcn_gill(iyear)=q_rate_fcn_gill(iyear-1);}
  }
}

```

```

for (iyear=styr_seine_cpue; iyear<=endyr_seine_cpue; iyear++)
{
    if (iyear>styr_seine_cpue & iyear <=2003)
        {q_rate_fcn_seine(iyear)=(1.0*q_rate)*q_rate_fcn_seine(iyear-1); //compound
        q_rate_fcn_seine(iyear)=(1.0+(iyear-styr_seine_cpue)*q_rate)*q_rate_fcn_seine(styr_seine_cpue); //linear
    }
    if (iyear>2003) fq_rate_fcn_seine(iyear)=q_rate_fcn_seine(iyear-1);
}

} //end q_rate conditional

//Get density dependence scalar (=1.0 if density independent model is used)
if (q_DD_beta>0.0)
{
    B_q_DD+=dzero;
    for (iyear=styr;iyear<=endyr;iyear++)
        {q_DD_fcn(iyear)=pow(B0_q_DD,q_DD_beta)*pow(B_q_DD(iyear),-q_DD_beta);}
        //{q_DD_fcn(iyear)=1.0+4.0/(1.0+mfexp(0.75*(B_q_DD(iyear)-0.1*B0_q_DD))); }
}

FUNCTION get_indices
//---Predicted CPUEs-----

//Gill net index
q_gill(styr_gill_cpue)=mfexp(log_q_gill);
for (iyear=styr_gill_cpue; iyear<=endyr_gill_cpue; iyear++)
{
    N_gill(iyear)=elem_prod(N_mdyr(iyear),sel_gill(iyear));
    pred_gill_cpue(iyear)=q_gill(iyear)*q_rate_fcn_gill(iyear)*q_DD_fcn(iyear)*sum(N_gill(iyear));
    if (iyear<endyr_gill_cpue){q_gill(iyear+1)=q_gill(iyear)*mfexp(q_RW_log_dev_gill(iyear));}
}

//seine index
q_seine(styr_seine_cpue)=mfexp(log_q_seine);
for (iyear=styr_seine_cpue; iyear<=endyr_seine_cpue; iyear++)
{
    N_seine(iyear)=N(iyear,1)*mfexp(-1.*Z(iyear)(1)*0.25); //matching seine index with April 1 (1/4 of the year completed)
    pred_seine_cpue(iyear)=q_seine(iyear)*q_rate_fcn_seine(iyear)*q_DD_fcn(iyear)*N_seine(iyear);
    if (iyear<endyr_seine_cpue){q_seine(iyear+1)=q_seine(iyear)*mfexp(q_RW_log_dev_seine(iyear));}
}

FUNCTION get_length_comps
//gill net survey
for (iyear=1;iyear<=nyr_gill_lenc;iyear++)
{
    pred_gill_lenc(iyear)=(N_gill(yrs_gill_lenc(iyear))*lenprob_gill
                           /sum(N_gill(yrs_gill_lenc(iyear))));
}

FUNCTION get_age_comps
//Commerical reduction
for (iyear=1;iyear<=nyr_cR_agec;iyear++)
{
    ErrorFree_cR_agec(iyear)=L_cR_num(yrs_cR_agec(iyear))/sum(L_cR_num(yrs_cR_agec(iyear)));
    pred_cR_agec(iyear)=age_error*ErrorFree_cR_agec(iyear);
}

////-----
FUNCTION get_weighted_current
F_temp_sum=0.0;
F_temp_sum+=mfexp((selpar_n_yrs_wgted*log_avg_F_cR+
                     sum(log_F_dev_cr((endyr-selpar_n_yrs_wgted+1),endyr)))/selpar_n_yrs_wgted);

F_cR_prop=mfexp((selpar_n_yrs_wgted*log_avg_F_cR+
                  sum(log_F_dev_cr((endyr-selpar_n_yrs_wgted+1),endyr)))/selpar_n_yrs_wgted)/F_temp_sum;

log_F_dev_end_cR=(sum(log_F_dev_R((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted;

F_end_L=sel_cR(endyr)*mfexp(log_avg_F_cR+log_F_dev_end_cR);

F_end=F_end_L;
F_end_apex=max(F_end);

sel_wgted_tot=F_end/F_end_apex;
sel_wgted_L=elem_prod(sel_wgted_tot, elem_div(F_end_L,F_end));

wgt_wgted_L_denom=F_cR_prop;
wgt_wgted_L_mt=F_cR_prop/wgt_wgted_L_denom*wholewgt_cR_mt(endyr)*1000; //to scale to 1000s mt

FUNCTION get_msy
//compute values as functions of F
for (ff=1; ff<n_iter_msy; ff++)
{
    //uses fishery-weighted F's
    Z_age_msy=0.0;
    F_L_age_msy=0.0;

    F_L_age_msy=F_msy(ff)*sel_wgted_L;
    Z_age_msy=M*F_L_age_msy;

    N_age_msy(1)=1.0;
    for (iage=2; iage<=nages; iage++)
    {
        N_age_msy(iage)=N_age_msy(iage-1)*mfexp(-1.*Z_age_msy(iage-1));
    }
    N_age_msy(nages)=N_age_msy(nages)/(1.0-mfexp(-1.*Z_age_msy(nages)));
    N_age_msy_mdyr(1,(nages-1))=elem_prod(N_age_msy(1),(nages-1)),
}

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```

        mfxp((-1.*Z_age_msy(1,(nages-1))*spawn_time_frac));
N_age_msy_mdry(nages)=(N_age_msy_mdry(nages-1)*
        (mfxp(-1.*(Z_age_msy(nages-1)*(1.0-spawn_time_frac) +
        Z_age_msy(nages)*spawn_time_frac) )))
/(1.0-mfxp(-1.*Z_age_msy(nages))));

spr_msy(ff)=sum(elem_prod(N_age_msy_mdry,reprod));

//Compute equilibrium values of R (including bias correction), SSB and Yield at each F
R_eq(ff)=SR_eq_func(R0, steep, spr_msy(i), spr_msy(ff), BiasCor, SR_switch);

if (R_eq(ff)<dzero) {R_eq(ff)=dzero;}
N_age_msy=R_eq(ff);
N_age_msy_mdry=R_eq(ff);

for (iage=1; iage<=nages; iage++)
{
    L_age_msy(iage)=N_age_msy(iage)*(F_L_age_msy(iage)/Z_age_msy(iage))*(
        (1.-mfxp(-1.*Z_age_msy(iage))));
}

SSB_eq(ff)=sum(elem_prod(N_age_msy_mdry,reprod));
B_eq(ff)=sum(elem_prod(N_age_msy,wgt_spawn_mt))*1000000;//to scale to 1000s mt and catch in 1000s
L_eq_mt(ff)=sum(elem_prod(L_age_msy,wgt_wgtd_L_mt))*1000;//to scale to catch in 1000s, wgt_wgtd_L_mt is already scaled to 1000s mt
L_eq_knum(ff)=sum(L_age_msy)/1000.0;
}

msy_mt_out=max(L_eq_mt);

for (ff=1; ff<=n_iter_msy; ff++)
{
    if(L_eq_mt(ff) == msy_mt_out)
    {
        SSB_msy_out=SSB_eq(ff);
        B_msy_out=B_eq(ff);
        R_msy_out=R_eq(ff);
        msy_knum_out=L_eq_knum(ff);
        F_msy_out=F_msy(ff);
        spr_msy_out=spr_msy(ff);
    }
}

//FUNCTION get_miscellaneous_stuff
FUNCTION get_miscellaneous_stuff

//switch here if var_rec_dev <=dzero
if(var_rec_dev>0.0)
{sigma_rec_dev=sqrt(var_rec_dev); //pow(var_rec_dev,0.5); //sample SD of predicted residuals (may not equal rec_sigma)
else(sigma_rec_dev=0.0; }

len_cv=elem_div(len_sd,meanlen_FL);

//compute total landings-at-age in 1000 fish and 1000s mt
L_total_num.initialize();
L_total_mt.initialize();
L_total_knum_yr.initialize();
L_total_mt_yr.initialize();

for(iyear=styr; iyear<=endyr; iyear++)
{
    L_total_mt_yr(iyear)=pred_cR_L_mt(iyear);
    L_total_knum_yr(iyear)=pred_ch_L_knum(iyear);

    B(iyear)=elem_prod(N(iyear),wgt_spawn_mt)*1000000;//scale to 1000s mt and 1000s fish landed
    totH(iyear)=sum(N(iyear)); //in 1000s of fish
    totB(iyear)=sum(B(iyear)); //in 1000s of mt
    SSBatage(iyear)=elem_prod(N(iyear),reprod);
}

L_total_num=L_cR_num; //landings at age in 1000s fish
L_total_mt=L_cR_mt; //landings at age in 1000s mt whole weight

B(endyr+1)=elem_prod(N(endyr+1),wgt_spawn_mt)*1000000;//scale to 1000s mt and 1000s fish
totH(endyr+1)=sum(N(endyr+1));//in 1000s of fish
totB(endyr+1)=sum(B(endyr+1));//in 1000s of mt

if(F_msy_out>0)
{
    FdF_msy=Fapex/F_msy_out;
    FdF_msy_end=FdF_msy(endyr);
    FdF_msy_end_mean=pow((FdF_msy(endyr)*FdF_msy(endyr-1)*FdF_msy(endyr-2)),(1.0/3.0));
}
if(SSB_msy_out>0)
{
    SdSSB_msy=SSB/SSB_msy_out;
    SdSSB_msy_end=SdSSB_msy(endyr);
}

//fill in log recruitment deviations for yrs they are nonzero
for(iyear=styr_rec_dev; iyear<=endyr_rec_dev; iyear++)
{log_rec_dev_output(iyear)=log_rec_dev(iyear);}

//fill in log Nage deviations for ages they are nonzero (ages2+)
for(iage=2; iage<=nages; iage++)
{
    log_Nage_dev_output(iage)=log_Nage_dev(iage);
}

//FUNCTION get_per_recruit_stuff

```

```

//static per-recruit stuff

for(iyear=styr; iyear<=endyr; iyear++)
{
  N_age_spr(1)=1.0;
  for(iage=2; iage<=nages; iage++)
  {
    N_age_spr(iage)=N_age_spr(iage-1)*mfexp(-1.*Z(iyear, iage-1));
  }
  N_age_spr(nages)=N_age_spr(nages)/(1.0-mfexp(-1.*Z(iyear, nages)));
  N_age_spr_mdyr(1,(nages-1))=elem_prod(N_age_spr(1,(nages-1)),
                                         mfexp(-1.*Z(iyear)(1,(nages-1))*spawn_time_frac));
  N_age_spr_mdyr(nages)=(N_age_spr_mdyr(nages-1)*
                           (mfexp(-1.*Z(iyear)(nages-1)*(1.0-spawn_time_frac) + Z(iyear)(nages)*spawn_time_frac) ))
                           /(1.0-mfexp(-1.*Z(iyear)(nages)));
  spr_static(iyear)=sum(elem_prod(N_age_spr_mdyr,reprod))/spr_F0;
}

//compute SSB/R and YPR as functions of F
for(ff=1; ff<=n_iter_spr; ff++)
{
  //uses fishery-weighted F's, same as in MSY calculations
  Z_age_spr=0.0;
  F_L_Age_spr=0.0;

  F_L_Age_spr=F_spr(ff)*sel_wgtd_L;

  Z_age_spr=M+F_L_Age_spr;

  N_age_spr(1)=1.0;
  for (iage=2; iage<=nages; iage++)
  {
    N_age_spr(iage)=N_age_spr(iage-1)*mfexp(-1.*Z_age_spr(iage-1));
  }
  N_age_spr(nages)=N_age_spr(nages)/(1-mfexp(-1.*Z_age_spr(nages)));
  N_age_spr_mdyr(1,(nages-1))=elem_prod(N_age_spr(1,(nages-1)),
                                         mfexp((-1.*Z_age_spr(1,(nages-1)))*spawn_time_frac));
  N_age_spr_mdyr(nages)=(N_age_spr_mdyr(nages-1)*
                           (mfexp(-1.*Z_age_spr(nages-1)*(1.0-spawn_time_frac) + Z_age_spr(nages)*spawn_time_frac) ))
                           /(1.0-mfexp(-1.*Z_age_spr(nages)));

  spr_spr(ff)=sum(elem_prod(N_age_spr_mdyr,reprod));
  L_spr(ff)=0.0;
  for (iage=1; iage<=nages; iage++)
  {
    L_age_spr(iage)=N_age_spr(iage)*(F_L_Age_spr(iage)/Z_age_spr(iage))*(
      (1.-mfexp(-1.*Z_age_spr(iage)));
    L_spr(ff)+=L_age_spr(iage)*wgtd_wgtd_L_mt(iage)*1000; //already scaled to 1000s mt, but need to scale to 1000s fish
  }
}

FUNCTION get_effective_sample_sizes

neff_gill_lenc_allyr_out=missing;//"missing" defined in admb2r.cpp
neff_cR_agec_allyr_out=missing;

for (iyear=1; iyear<=nyr_gill_lenc; iyear++)
{
  if (nsamp_gill_lenc(iyear)>minSS_gill_lenc)
    {neff_gill_lenc_allyr_out(yrs_gill_lenc(iyear))=multinom_eff_N(pred_gill_lenc(iyear),obs_gill_lenc(iyear));}
  else {neff_gill_lenc_allyr_out(yrs_gill_lenc(iyear))=-99;}
}

for (iyear=1; iyear<=nyr_cR_agec; iyear++)
{
  if (nsamp_cR_agec(iyear)>minSS_cR_agec)
    {neff_cR_agec_allyr_out(yrs_cR_agec(iyear))=multinom_eff_N(pred_cR_agec(iyear),obs_cR_agec(iyear));}
  else {neff_cR_agec_allyr_out(yrs_cR_agec(iyear))=-99;}
}

FUNCTION get_Fmed_benchmarks

//sorting function for recruitment and SPR values (slow algorithm, but works)
R_temp=rec(styr,endyr);
SPR_temp=pred_SPR(styr,endyr);
for(int jyear=endyr; jyear>=styr; jyear--)
{
  R_sort(jyear)=max(R_temp);
  SPR_sort(jyear)=max(SPR_temp);
  for(iyear=styr; iyear<=endyr; iyear++)
  {
    if(R_temp(iyear)==R_sort(jyear))
    {
      R_temp(iyear)=0.0;
    }
    if(SPR_temp(iyear)==SPR_sort(jyear))
    {
      SPR_temp(iyear)=0.0;
    }
  }
}

// compute the quantile using quant_whole (declared in the data section)
// which computes the floor integer of a decimal number
//median
quant_decimal=(endyr-styr)*0.5;
quant_whole=(endyr-styr)*0.5;
quant_diff=quant_decimal-quant_whole;
R_med=R_sort(styr+quant_whole)*(1-quant_diff)+R_sort(styr+quant_whole+1)*(quant_diff);
SPR_med=SPR_sort(styr+quant_whole)*(1-quant_diff)+SPR_sort(styr+quant_whole+1)*(quant_diff);
//cout << "quant_decimal = " << quant_decimal << endl;
//cout << "quant_whole = " << quant_whole << endl;

```

```

//cout << "quant_diff = " << quant_diff << endl;
//cout << "result = " << quant_whole*(1-quant_diff)+(quant_whole+1)*quant_diff << endl;
//cout << "R_med = " << R_med << endl;
//cout << "R_sort = " << R_sort << endl;
//cout << "R = " << R_temp << endl;

//75th quantile
quant_decimal=(endyr-styr)*0.75;
quant_whole=(endyr-styr)*0.75;
quant_diff=quant_decimal-quant_whole;
SPR_75th=SPR_sort(styr+quant_whole)*(1-quant_diff)+SPR_sort(styr+quant_whole+1)*(quant_diff);
//cout << "quant_decimal = " << quant_decimal << endl;
//cout << "quant_whole = " << quant_whole << endl;
//cout << "quant_diff = " << quant_diff << endl;
//cout << "result = " << quant_whole*(1-quant_diff)+(quant_whole+1)*quant_diff << endl;

//find F that matches SPR_med = F_med
SPR_diff=square(spr_spr-SPR_med);
SPR_diff_min=min(SPR_diff);
for(ff=1; ff<=n_iter_spr; ff++)
{
  if(SPR_diff(ff)==SPR_diff_min)
  {
    F_med=F_spr(ff);
    //F_med_age2plus=F_spr_age2plus(ff);
    L_med=L_spr(ff)*R_med;
  }
}
SSB_med=SPR_med*R_med;
SSB_med_thresh=SSB_med*0.5;

//get the target that corresponds to Fmed, based on 75th quantile of SPR scatter
SPR_diff=square(spr_spr-SPR_75th);
SPR_diff_min=min(SPR_diff);
for(ff=1; ff<=n_iter_spr; ff++)
{
  if(SPR_diff(ff)==SPR_diff_min)
  {
    F_med_target=F_spr(ff);
    //F_med_target_age2plus=F_spr_age2plus(ff);
    L_med_target=L_spr(ff)*R_med;
  }
}

//-----
FUNCTION evaluate_objective_function
fval=0.0;
fval_data=0.0;
//---likelihoods-----
//---Indices-----
f_gill_cpue=0.0;
f_gill_cpue=lk_lognormal(pred_gill_cpue, obs_gill_cpue, gill_cpue_cv, w_I_gill);
fval+=f_gill_cpue;
fval_data+=f_gill_cpue;

f_seine_cpue=0.0;
f_seine_cpue=lk_lognormal(pred_seine_cpue, obs_seine_cpue, seine_cpue_cv, w_I_seine);
fval+=f_seine_cpue;
fval_data+=f_seine_cpue;

//----Landsings-----
//f_cR_L in 1000s mt
f_cR_L=lk_lognormal(pred_cR_L_mt, obs_cR_L, cR_L_cv, w_L);
fval+=f_cR_L;
fval_data+=f_cR_L;

//---Length comps-----
//f_gill_lenc
f_gill_lenc=lk_robust_multinomial(nsamp_gill_lenc, pred_gill_lenc, obs_gill_lenc, nyr_gill_lenc, double(nlenbins), minSS_gill_lenc, w_lc_gill);
//f_gill_lenc=lk_multinomial(nsamp_gill_lenc, pred_gill_lenc, obs_gill_lenc, nyr_gill_lenc, minSS_gill_lenc, w_lc_gill);
fval+=f_gill_lenc;
fval_data+=f_gill_lenc;

//----Age comps-----
//f_cR_agec
f_cR_agec=lk_robust_multinomial(nsamp_cR_agec, pred_cR_agec, obs_cR_agec, nyr_cR_agec, double(nages), minSS_cR_agec, w_ac_cR);
//f_cR_agec=lk_multinomial(nsamp_cR_agec, pred_cR_agec, obs_cR_agec, nyr_cR_agec, minSS_cR_agec, w_ac_cR);
fval+=f_cR_agec;
fval_data+=f_cR_agec;

//----Constraints and penalties-----
f_M_dev=0.0;
f_M_dev=norm2(M_dev);
fval+=w_M_dev*f_M_dev;

f_rec_dev=0.0;
//rec_sigma_sq=square(rec_sigma);
rec_logL_add=nyrs_rec*log(rec_sigma);
fval+=w_rec_dev*f_rec_dev;

```

```

f_rec_dev=(square(log_rec_dev(styr_rec_dev) + rec_sigma_sq/2.0)/(2.0*rec_sigma_sq));
for(iyear=(styr_rec_dev+1); iyear<=endyr_rec_dev; iyear++)
  {f_rec_dev+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
    (2.0*rec_sigma_sq));}
f_rec_dev+=rec_logL_add;
fval+=w_recf_rec_dev;

f_rec_dev_early=0.0; //possible extra constraint on early rec deviations
if (w_rec_early>0.0)
  { if (styr_rec_dev<endyr_rec_phase1)
    {
      for(iyear=styr_rec_dev; iyear<=endyr_rec_phase1; iyear++)
        //f_rec_dev_early+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
        //  (2.0*rec_sigma_sq)) + rec_logL_add;
      {f_rec_dev_early+=square(log_rec_dev(iyear));}
    }
  fval+=w_rec_early*f_rec_dev_early;
}

f_rec_dev_end=0.0; //possible extra constraint on ending rec deviations
if (w_rec_end>0.0)
{ if (endyr_rec_phase2<endyr)
  {
    for(iyear=(endyr_rec_phase2+1); iyear<=endyr; iyear++)
      //f_rec_dev_end+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
      //  (2.0*rec_sigma_sq)) + rec_logL_add;
    {f_rec_dev_end+=square(log_rec_dev(iyear));}
  }
  fval+=w_rec_end*f_rec_dev_end;
}

//fval+=norm2(log_Nage_dev); //applies if initial age structure is estimated

//Random walk components of fishery dependent indices

//f_gill_RW_cpue=0.0;
//for (iyear=styr_gill_cpue; iyear<endyr_gill_cpue; iyear++)
//  {f_gill_RW_cpue+=square(q_RW_log_dev_gill(iyear))/(2.0*set_q_RW_gill_var);}
//fval+=f_gill_RW_cpue;

//f_seine_RW_cpue=0.0;
//for (iyear=styr_seine_cpue; iyear<endyr_seine_cpue; iyear++)
//  {f_seine_RW_cpue+=square(q_RW_log_dev_seine(iyear))/(2.0*set_q_RW_seine_var);}
//fval+=f_seine_RW_cpue;

//---Priors-----
//neg_log_prior arguments: estimate, prior mean, prior var/-CV, pdf type
//Variance input as a negative value is considered to be CV in arithmetic space (CV=-1 implies loose prior)
//pdf type 1=none, 2=lognormal, 3=normal, 4=beta
f_priors=0.0;
//f_priors+=neg_log_prior(Linf,set_Linf(5),set_Linf(6),set_Linf(7));
//f_priors+=neg_log_prior(K,set_K(5),set_K(6),set_K(7));
//f_priors+=neg_log_prior(t0,set_t0(5),set_t0(6),set_t0(7));
//f_priors+=neg_log_prior(len_cv_val,set_len_cv(5),set_len_cv(6),set_len_cv(7));
//f_priors+=neg_log_prior(M_constant,set_M_constant(5),set_M_constant(6),set_M_constant(7));

//f_priors+=neg_log_prior(stEEP,set_stEEP(5),set_log_R0(6),set_log_R0(7));
//f_priors+=neg_log_prior(log_R0,set_log_R0(5),set_log_R0(6),set_log_R0(7));
//f_priors+=neg_log_prior(R_autocorr,set_R_autocorr(5),set_R_autocorr(6),set_R_autocorr(7));
//f_priors+=neg_log_prior(rec_sigma,set_rec_sigma(5),set_rec_sigma(6),set_rec_sigma(7));

//f_priors+=neg_log_prior(selpar_L50_cR(set_selpar_L50_cR(5),set_selpar_L50_cR(6), set_selpar_L50_cR(7));
//f_priors+=neg_log_prior(selpar_slope_cR(5),set_selpar_slope_cR(6), set_selpar_slope_cR(7));
//f_priors+=neg_log_prior(selpar_L502_cR(set_selpar_L502_cR(5),set_selpar_L502_cR(6), set_selpar_L502_cR(7));
//f_priors+=neg_log_prior(selpar_slope2_cR(5),set_selpar_slope2_cR(6), set_selpar_slope2_cR(7));
//f_priors+=neg_log_prior(sel_age1_cR(5),set_sel_age1_cR(6), set_sel_age1_cR(7));
//f_priors+=neg_log_prior(sel_age3_cR(logit),set_sel_age3_cR(5),set_sel_age3_cR(6), set_sel_age3_cR(7));
//f_priors+=neg_log_prior(sel_age4_cR(logit),set_sel_age4_cR(5),set_sel_age4_cR(6), set_sel_age4_cR(7));

//f_priors+=neg_log_prior(selpar_L50_gill(set_selpar_L50_gill(5),set_selpar_L50_gill(6), set_selpar_L50_gill(7));
//f_priors+=neg_log_prior(selpar_slope_gill(5),set_selpar_slope_gill(6), set_selpar_slope_gill(7),set_selpar_slope_gill(7));

//f_priors+=neg_log_prior(log_q_gill,set_log_q_gill(5),set_log_q_gill(6),set_log_q_gill(7));
//f_priors+=neg_log_prior(log_q_seine,set_log_q_seine(5),set_log_q_seine(6),set_log_q_seine(7));

//f_priors+=neg_log_prior(log_avg_F_cR(set_log_avg_F_cR(5),set_log_avg_F_cR(6),set_log_avg_F_cR(7));

fval+=f_priors;

//cout << "fval = " << fval << " fval_data = " << fval_data << endl;
//cout << endl;

//-----
//Logistic function: 2 parameters
FUNCTION dvar_vector logistic(const dvar_vector& ages, const dvariable& L50, const dvariable& slope)
  //ages=vector of ages, L50=age at 50% selectivity, slope=rate of increase
  RETURN_ARRAYS_INCREMENT();
  dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
  Sel_Tmp+=1./(.1.+mfexp(-1.*slope*(ages-L50))); //logistic;
  RETURN_ARRAYS_DECREMENT();
  return Sel_Tmp;

//-----
//Logistic function: 4 parameters
FUNCTION dvar_vector logistic_double(const dvar_vector& ages, const dvariable& L501, const dvariable& slope1, const dvariable& L502, const dvariable& slope2)
  //ages=vector of ages, L50=age at 50% selectivity, slope=rate of increase, L502=age at 50% decrease additive to L501, slope2=slope of decrease
  RETURN_ARRAYS_INCREMENT();
  dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
  Sel_Tmp+=prod( (1./(.1.+mfexp(-1.*slope1*(ages-L501)))),(1.-(.1./(.1.+mfexp(-1.*slope2*(ages-(L501+L502)))))) );
  Sel_Tmp=Sel_Tmp/max(Sel_Tmp);

```

```

RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Jointed logistic function: 6 parameters (increasing and decreasing logistics joined at peak selectivity)
FUNCTION dvar_vector logistic_joint(const dvar_vector& ages, const dvariable& L501, const dvariable& slope1, const dvariable& L502, const dvariable& slope2, const dvariable& satval, const dvariable& joint)
//ages=vector of ages, L501=age at 50% sel (ascending limb), slope1=rate of increase,L502=age at 50% sel (descending), slope2=rate of decrease (ascending),
//satval=saturation value of descending limb, joint=location in age vector to join curves (may equal age or age + 1 if age=0 is included)
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
Sel_Tmp=1.0;
for (iage=1; iage<=nages; iage++)
{
    if (double(iage)<joint) {Sel_Tmp(iage)=1.0/(1.+mfexp(-1.*slope1*(ages(iage)-L501)));}
    if (double(iage)>joint){Sel_Tmp(iage)=1.0-(1.0-satval)/(1.+mfexp(-1.*slope2*(ages(iage)-L502)));}
}
Sel_Tmp=Sel_Tmp/max(Sel_Tmp);
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Double Gaussian function: 6 parameters (as in SS3)
FUNCTION dvar_vector gaussian_double(const dvar_vector& ages, const dvariable& peak, const dvariable& top, const dvariable& ascwid, const dvariable& deswid, const dvariable& init, const dvariable& final)
//ages=vector of ages, peak=ascending inflection location (as logistic), top=width of plateau, ascwid=ascent width (as log(width))
//deswid=descent width (as log(width))
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
dvar_vector sel_step1(ages.indexmin(),ages.indexmax());
dvar_vector sel_step2(ages.indexmin(),ages.indexmax());
dvar_vector sel_step3(ages.indexmin(),ages.indexmax());
dvar_vector sel_step4(ages.indexmin(),ages.indexmax());
dvar_vector sel_step5(ages.indexmin(),ages.indexmax());
dvar_vector sel_step6(ages.indexmin(),ages.indexmax());
dvar_vector pars_tmp(1,6); dvar_vector sel_tmp_iq(1,2);

pars_tmp(1)*peak;
pars_tmp(2)*peak+1.0+(0.99*ages(nages)-peak-1.0)/(1.0+mfexp(-top));
pars_tmp(3)=mfexp(ascwid);
pars_tmp(4)=mfexp(deswid);
pars_tmp(5)=1.0/(1.0+mfexp(-init));
pars_tmp(6)=1.0/(1.0+mfexp(-final));

sel_tmp_iq(1)=mfexp(-(square(ages(1)-pars_tmp(1))/pars_tmp(3)));
sel_tmp_iq(2)=mfexp(-(square(ages(nages)-pars_tmp(2))/pars_tmp(4)));

sel_step1=mfexp(-(square(ages-pars_tmp(1))/pars_tmp(3)));
sel_step2=pars_tmp(5)+(1.0-pars_tmp(5))*(sel_step1-sel_tmp_iq(1))/(1.0-sel_tmp_iq(1));
sel_step3=mfexp(-(square(ages-pars_tmp(2))/pars_tmp(4)));
sel_step4=1.0*(pars_tmp(6)-1.0)*(sel_step3-1.0)/(sel_tmp_iq(2)-1.0);
sel_step5=1.0/(1.0+mfexp((20.0* elem_div((ages-pars_tmp(1)), (1.0+sfabs(ages-pars_tmp(1)))) )) );
sel_step6=1.0/(1.0+mfexp(-(20.0*elem_div((ages-pars_tmp(2)),(1.0+sfabs(ages-pars_tmp(2)))) )) );

Sel_Tmp=elem_prod(sel_step2,(1.0-sel_step5))+ elem_prod(sel_step5,((1.0-sel_step6)+ elem_prod(sel_step4,sel_step6)) );

Sel_Tmp=Sel_Tmp/max(Sel_Tmp);
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Spawner-recruit function (Beverton-Holt or Ricker)
FUNCTION dvariable SR_func(const dvariable& R0, const dvariable& h, const dvariable& spr_F0, const dvariable& SSB, int func)
//R0=virgin recruitment, h=steepness, spr_F0=spawners per recruit @ F=0, SSB=spawning biomass
//func=1 for Beverton-Holt, 2 for Ricker
RETURN_ARRAYS_INCREMENT();
dvariable Recruits_Tmp;
switch(func) {
    case 1: //Beverton-Holt
        Recruits_Tmp=((0.8*R0*h*SSB)/(0.2*R0*spr_F0*(1.0-h)+(h-0.2)*SSB));
        break;
    case 2: //Ricker
        Recruits_Tmp=((SSB/spr_F0)*mfexp(h*(1-SSB/(R0*spr_F0))));
        break;
}
RETURN_ARRAYS_DECREMENT();
return Recruits_Tmp;

//-----
//Spawner-recruit equilibrium function (Beverton-Holt or Ricker)
FUNCTION dvariable SR_eq_func(const dvariable& R0, const dvariable& h, const dvariable& spr_F0, const dvariable& spr_F, const dvariable& BC, int func)
//R0=virgin recruitment, h=steepness, spr_F0=spawners per recruit @ F=0, spr_F=spawners per recruit @ F, BC=bias correction
//func=1 for Beverton-Holt, 2 for Ricker
RETURN_ARRAYS_INCREMENT();
dvariable Recruits_Tmp;
switch(func) {
    case 1: //Beverton-Holt
        Recruits_Tmp=(R0/((5.0*h-1.0)*spr_F))*(BC*4.0*h*spr_F-spr_F0*(1.0-h));
        break;
    case 2: //Ricker
        Recruits_Tmp=R0/(spr_F/spr_F0)*(1.0+log(BC*spr_F/spr_F0)/h);
        break;
}
RETURN_ARRAYS_DECREMENT();
return Recruits_Tmp;

//-----
//compute multinomial effective sample size for a single yr
FUNCTION dvariable multinom_eff_N(const dvar_vector& pred_comp, const dvar_vector& obs_comp)
//pred_comp=vector of predicted comps, obscomp=vector of observed comps
dvariable EffN_Tmp; dvariable numer; dvariable denom;
RETURN_ARRAYS_INCREMENT();
numer=sum( elem_prod(pred_comp,(1.0-pred_comp)) );
denom=sum( square(obs_comp-pred_comp) );

```

```

if (denom>0.0) {EffN_Tmp=numer/denom;}
else {EffN_Tmp=missing;}
RETURN_ARRAYS_DECREMENT();
return EffN_Tmp;

//-----
//Likelihood contribution: lognormal
FUNCTION dvariable lk_lognormal(const dvar_vector& pred, const dvar_vector& obs, const dvar_vector& cv, const dvariable& wgt_dat)
//pred=vector of predicted vals, obs=vector of observed vals, cv=vector of CVs in arithmetic space, wgt_dat=constant scaling of CVs
//small_number is small value to avoid log(0) during search
RETURN_ARRAYS_INCREMENT();
dvariable LkvalTmp;
dvariable small_number=0.00001;
dvar_vector var(cv.indexmin(),cv.indexmax()); //variance in log space
var=log(1.0+square(cv/wgt_dat)); // convert cv in arithmetic space to variance in log space
LkvalTmp=sum(0.5*elem_div(square(log(elem_div((pred+small_number),(obs+small_number)))),var));
RETURN_ARRAYS_DECREMENT();
return LkvalTmp;

//-----
//Likelihood contribution: multinomial
FUNCTION dvariable lk_multinomial(const dvar_vector& nsamp, const dvar_matrix& pred_comp, const dvar_matrix& obs_comp, const double& ncomp, const double& minSS, const dvariable& wgt_dat)
//nsamp=vector of N's, pred_comp=matrix of predicted comps, obs_comp=matrix of observed comps, ncomp = number of yrs in matrix, minSS=min N threshold, wgt_dat=scaling of N's
RETURN_ARRAYS_INCREMENT();
dvariable LkvalTmp;
dvariable small_number=0.00001;
LkvalTmp=0.0;
for (int ii=1; ii<=ncomp; ii++)
{if (nsamp(ii)>minSS)
 {LkvalTmp+=wgt_dat*nsamp(ii)*sum(elem_prod((obs_comp(ii)+small_number),
 log(elem_div((pred_comp(ii)+small_number), (obs_comp(ii)+small_number))))));
 }
}
RETURN_ARRAYS_DECREMENT();
return LkvalTmp;

//-----
//Likelihood contribution: multinomial
FUNCTION dvariable lk_robust_multinomial(const dvar_vector& nsamp, const dvar_matrix& pred_comp, const dvar_matrix& obs_comp, const double& ncomp, const dvariable& mbin, const double& minSS, const dvariable& wgt_dat)
//nsamp=vector of N's, pred_comp=matrix of predicted comps, obs_comp=matrix of observed comps, ncomp = number of yrs in matrix, mbin=number of bins, minSS=min N threshold, wgt_dat=scaling of N's
RETURN_ARRAYS_INCREMENT();
dvariable LkvalTmp;
dvariable small_number=0.00001;
LkvalTmp=0.0;
dvar_matrix Eprime=elem_prod((1.0-obs_comp), obs_comp)+0.1/mbin; //E' of Francis 2011, p.1131
dvar_vector nsamp_wgt=nsamp*wgt_dat;
//cout<<nsamp_wgt<<endl;
for (int ii=1; ii<=ncomp; ii++)
{if (nsamp(ii)>minSS)
 {LkvalTmp+= sum(0.5*log(Eprime(ii))-log(small_number+mfexp(elem_div((-square(obs_comp(ii)-pred_comp(ii))), (Eprime(ii)*2.0/nsamp_wgt(ii))))));
 }
}
RETURN_ARRAYS_DECREMENT();
return LkvalTmp;

//-----
//Likelihood contribution: priors
FUNCTION dvariable neg_log_prior(dvariable pred, const double& prior, dvariable var, int pdf)
//prior=prior point estimate, var=variance (if negative, treated as CV in arithmetic space), pred=predicted value, pdf=prior type (1=none, 2=lognormal, 3=normal, 4=beta)
dvariable LkvalTmp;
dvariable alpha, beta, ab_iq;
dvariable big_number=1e10;
LkvalTmp=0.0;
// compute generic pdf's
switch(pdf) {
  case 1: //option to turn off prior
    LkvalTmp=0.0;
    break;
  case 2: // lognormal
    if(prior<0.0) cout << "VIKES: Don't use a lognormal distn for a negative prior" << endl;
    else if(pred<0) LkvalTmp=big_number=1e10;
    else {
      if(var<0.0) var=log(1.0+var*var); // convert cv to variance on log scale
      LkvalTmp= 0.5*( square(log(pred/prior))/var + log(var) );
    }
    break;
  case 3: // normal
    if(var<0.0 && prior!=0.0) var=square(var*prior); // convert cv to variance on observation scale
    else if(var<0.0 && prior==0.0) var=-var; // cv not really appropriate if prior value equals zero
    LkvalTmp= 0.5*( square(pred-prior)/var + log(var) );
    break;
  case 4: // beta
    if(var<0.0) var=square(var*prior); // convert cv to variance on observation scale
    if(prior<0.0 || prior>1.0) cout << "VIKES: Don't use a beta distn for a prior outside (0,1)" << endl;
    ab_iq=prior*(1.0-prior)/var - 1.0; alpha=prior*ab_iq; beta=(1.0-prior)*ab_iq;
    if(pred==0 && pred<1) LkvalTmp= (1.0-alpha)*log(pred)+(1.0-beta)*log(1.0-pred)-gammln(alpha+beta)+gammln(alpha)+gammln(beta);
    else LkvalTp=big_number;
    break;
  default: // no such prior pdf currently available
    cout << "The prior must be either 1(lognormal), 2(normal), or 3(beta)." << endl;
    cout << "Presently it is " << pdf << endl;
    exit(0);
}
return LkvalTmp;

//SDNR: age comp likelihood (assumes fits are done with the robust multinomial function)
FUNCTION dvariable sdnr_multinomial(const double& ncomp, const dvar_vector& ages, const dvar_vector& nsamp,
                                     const dvar_matrix& pred_comp, const dvar_matrix& obs_comp, const dvariable& wgt_dat)
//ncomp=number of years of data, ages=vector of ages, nsamp=vector of N's,
//pred_comp=matrix of predicted comps, obs_comp=matrix of observed comps, wgt_dat=likelihood weight for data source

```

```

RETURN_ARRAYS_INCREMENT();
dvariable SdnrmTp;
dvar_vector o(1,ncomp);
dvar_vector p(1,ncomp);
dvar_vector ose(1,ncomp);
dvar_vector res(1,ncomp);
SdnrmTp=0.0;
for (int ii=1; ii<=ncomp; ii++)
{
    o(ii)=sum(elem_prod(ages,obs_comp(ii)));
    p(ii)=sum(elem_prod(ages,pred_comp(ii)));
    ose(ii)=sqrt((sum(elem_prod(square(ages),pred_comp(ii)))-square(p(ii)))/(nsamp(ii)*wgt_dat));
}
res=elem_div((o-p),ose);
SdnrmTp=sqrt(sum(square(res-(sum(res)/ncomp))/(ncomp-1.0)));
RETURN_ARRAYS_DECREMENT();
return SdnrmTp;

//-----
//SDNR: lognormal likelihood
FUNCTION dvariable sdnr_lognormal(const dvar_vector& pred, const dvar_vector& obs, const dvar_vector& cv, const dvariable& wgt_dat)
//nry=number of years of data, pred=vector of predicted data, obs=vector of observed data, cv=vector of cv's, wgt_dat=likelihood weight for data source
RETURN_ARRAYS_INCREMENT();
dvariable SdnrmTp;
dvariable small_number=0.00001;
dvariable n;
dvar_vector res(cv.indexmin(),cv.indexmax());
SdnrmTp=0.0;
res=elem_div(log(elem_div(obs+small_number,pred+small_number)),sqrt(log(1+square(cv/wgt_dat))));
n=cv.indexmax()-cv.indexmin()+1;
SdnrmTp=sqrt(sum(square(res-(sum(res)/n))/(n-1.0)));
RETURN_ARRAYS_DECREMENT();
return SdnrmTp;

//-----
REPORT_SECTION

if (last_phase())
{
    // cout<<"start report" << endl;
    get_weighted_current();
    //cout<<"got weighted" << endl;
    get_msy();
    //cout<<"got msy" << endl;
    get_misellaneous_stuff();
    //cout<<"got misc stuff" << endl;
    get_per_recruit_stuff();
    //cout<<"got peer recruit" << endl;
    get_effective_sample_sizes();
    get_Fmed_benchmarks();
    cout << "got Fmed benchmarks" << endl;

    time(&finish);
elapsed_time=difftime(finish,start);
hour=(long(elapsed_time))/3600;
minute=(long(elapsed_time)%3600)/60;
second=(long(elapsed_time)%3600)/60;
cout << endl << "*****" << endl;
cout << "Start time: " << ctime(&start) << endl;
cout << "Finish time: " << ctime(&finish) << endl;
cout << "Runtime: ";
cout << hour << " hours, " << minute << " minutes, " << second << " seconds" << endl;
cout << "*****" << endl;

cout << endl;
cout << ">-><>-><>-><>-><>-><>-><>-><>-><>-><>" << endl;
cout << "BC Fmsy=" << F_msy_out << " BC SSBmsy=" << SSB_msy_out << endl;
cout << "F status=" << Fdf_msy_end << endl;
cout << "Pop status=" << SdSSB_msy_end << endl;
cout << "h" << steep << " RO=" << R0 << endl;
cout << ">-><>-><>-><>-><>-><>-><>-><>" << endl;

report << "TotalLikelihood " << fval << endl;
report << "N" << endl;
report << N << endl;
report << "F" << endl;
report << F << endl;

sdnr_lc_gill=sdnr_multinomial(nyr_gill_lenc, lbins, nsamp_gill_lenc, pred_gill_lenc, obs_gill_lenc, w_lc_gill);

sdnr_ac_CR=sdnr_multinomial(nyr_CR_agec, agebins, nsamp_CR_agec, pred_CR_agec, obs_CR_agec, w_ac_CR);

sdnr_L_gill=sdnr_lognormal(pred_gill_cpue, obs_gill_cpue, gill_cpue_cv, w_L_gill);
sdnr_I_seine=sdnr_lognormal(pred_seine_cpue, obs_seine_cpue, seine_cpue_cv, w_I_seine);

//#####
//## Passing parameters to vector for bounds check plotting
//#####
Linf_out(8)=Linf; Linf_out(1,7)=set_Linf;
K_out(8)=K; K_out(1,7)=set_K;
t0_out(8)=t0; t0_out(1,7)=set_t0;
len_cv_val_out(8)=len_cv_val; len_cv_val_out(1,7)=set_len_cv;
log_RO_out(8)=log_RO; log_RO_out(1,7)=set_log_RO;
steep_out(8)=steep; steep_out(1,7)=set_steepest;
rec_sigma_out(8)=rec_sigma; rec_sigma_out(1,7)=set_rec_sigma;
R_autocorr_out(8)=R_autocorr; R_autocorr_out(1,7)=set_R_autocorr;
selpar_L50_cr_out(8)=selpar_L50_cr; selpar_L50_cr_out(1,7)=set_selpar_L50_cr;
selpar_slope_cr_out(8)=selpar_slope_cr; selpar_slope_cr_out(1,7)=set_selpar_slope_cr;
selpar_L502_cr_out(8)=selpar_L502_cr; selpar_L502_cr_out(1,7)=set_selpar_L502_cr;
selpar_slope2_cr_out(8)=selpar_slope2_cr; selpar_slope2_cr_out(1,7)=set_selpar_slope2_cr;
selpar_age0_cr_out(8)=selpar_age0_cr; selpar_age0_cr_out(1,7)=set_selpar_age0_cr;

```

```

selpar_age1_cr_out(8)=sel_age1_cr_logit; selpar_age1_cr_out(1,7)=set_sel_age1_cr;
selpar_age2_cr_out(8)=sel_age2_cr_logit; selpar_age2_cr_out(1,7)=set_sel_age2_cr;
selpar_age3_cr_out(8)=sel_age3_cr_logit; selpar_age3_cr_out(1,7)=set_sel_age3_cr;
selpar_age4_cr_out(8)=sel_age4_cr_logit; selpar_age4_cr_out(1,7)=set_sel_age4_cr;
selpar_age0_cr2_out(8)=sel_age0_cr2_logit; selpar_age0_cr2_out(1,7)=set_sel_age0_cr2;
selpar_age1_cr2_out(8)=sel_age1_cr2_logit; selpar_age1_cr2_out(1,7)=set_sel_age1_cr2;
selpar_age2_cr2_out(8)=sel_age2_cr2_logit; selpar_age2_cr2_out(1,7)=set_sel_age2_cr2;
selpar_age3_cr2_out(8)=sel_age3_cr2_logit; selpar_age3_cr2_out(1,7)=set_sel_age3_cr2;
selpar_age4_cr2_out(8)=sel_age4_cr2_logit; selpar_age4_cr2_out(1,7)=set_sel_age4_cr2;
selpar_l50_gill_out(8)=selpar_l50_gill; selpar_l50_gill_out(1,7)=set_selpar_l50_gill;
selpar_slope_gill_out(8)=selpar_slope_gill; selpar_slope_gill_out(1,7)=set_selpar_slope_gill;
log_q_gill_out(8)=log_q_gill; log_q_gill_out(1,7)=set_log_q_gill;
log_q_seine_out(8)=log_q_seine; log_q_seine_out(1,7)=set_log_q_seine;
M_constant_out(8)=M_constant; M_constant_out(1,7)=set_M_constant;
log_avg_F_cr_out(8)=log_avg_F_cr; log_avg_F_cr_out(1,7)=set_log_avg_F_cr;

#include "gm_make_Robject-001.cxx" // write the S-compatible report
} //endl last phase loop

```

## Appendix B Data inputs for the Beaufort Assessment Model

|       |       |       |       |       |
|-------|-------|-------|-------|-------|
| 0.000 | 0.559 | 0.384 | 0.050 | 0.007 |
| 0.001 | 0.666 | 0.292 | 0.037 | 0.004 |
| 0.000 | 0.494 | 0.437 | 0.060 | 0.007 |
| 0.000 | 0.351 | 0.622 | 0.026 | 0.001 |
| 0.000 | 0.391 | 0.550 | 0.055 | 0.004 |
| 0.000 | 0.544 | 0.403 | 0.046 | 0.007 |
| 0.000 | 0.392 | 0.563 | 0.041 | 0.004 |
| 0.000 | 0.544 | 0.386 | 0.067 | 0.003 |
| 0.000 | 0.362 | 0.564 | 0.062 | 0.012 |
| 0.000 | 0.250 | 0.672 | 0.074 | 0.005 |
| 0.000 | 0.317 | 0.573 | 0.107 | 0.003 |
| 0.000 | 0.362 | 0.571 | 0.064 | 0.003 |
| 0.000 | 0.560 | 0.353 | 0.080 | 0.008 |
| 0.019 | 0.394 | 0.541 | 0.043 | 0.003 |
| 0.000 | 0.459 | 0.470 | 0.065 | 0.006 |
| 0.000 | 0.463 | 0.510 | 0.024 | 0.004 |
| 0.000 | 0.266 | 0.683 | 0.044 | 0.006 |
| 0.000 | 0.126 | 0.731 | 0.129 | 0.013 |
| 0.000 | 0.529 | 0.404 | 0.061 | 0.006 |
| 0.007 | 0.634 | 0.317 | 0.037 | 0.007 |

```
#####
##### LA gill net index#####
#Starting and ending years of LA gill net index
1988
2011
#Observed index and assumed CVs
0.27 0.21 0.24 0.25 0.22 0.41 0.84 0.55 0.67 1.24 0.94 0.80 1.00 1.34 0.99 1.02 0.90 1.24 1.18 0.86 3.52 2.64 0.75 1.93
0.05 0.04 0.10 0.10 0.11 0.13 0.16 0.15 0.15 0.14 0.13 0.13 0.13 0.13 0.13 0.13 0.14 0.13 0.12 0.13 0.12 0.11 0.14 0.13
```

```
#Number and vector of years of length compositions for gill net survey
16
1996 1997 1998 1999 2000 2001 2002 2003 2004 2005 2006 2007 2008 2009 2010 2011
#sample size of gill net survey length comp data by year (first row observed Ntrips, second row Nfish)
009 236 246 231 266 219 241 247 231 234 297 253 277 308 193 248
2388 3386 3059 2913 4236 3542 3131 3297 2851 3659 4588 3301 5794 5782 2377 4222
#gill net length composition samples (year,length,bin 1 cm)
0.01 0.01 0.01 0.02 0.07 0.15 0.16 0.09 0.11 0.11 0.08 0.05 0.05 0.04 0.03
0.00 0.01 0.00 0.01 0.06 0.13 0.14 0.11 0.1 0.13 0.09 0.07 0.07 0.03 0.03
0.00 0.01 0.01 0.02 0.06 0.17 0.19 0.11 0.11 0.12 0.07 0.04 0.03 0.02 0.02
0.00 0.01 0.01 0.03 0.07 0.16 0.14 0.1 0.11 0.11 0.08 0.06 0.06 0.03 0.02
0.00 0.00 0.01 0.02 0.08 0.14 0.11 0.07 0.07 0.12 0.12 0.08 0.08 0.06 0.04
0.01 0.01 0.01 0.03 0.06 0.13 0.11 0.08 0.13 0.14 0.08 0.06 0.07 0.05 0.06
0.00 0.01 0.01 0.03 0.08 0.14 0.14 0.08 0.08 0.11 0.09 0.06 0.07 0.06 0.05
0.00 0.01 0.01 0.03 0.09 0.19 0.19 0.1 0.1 0.13 0.07 0.02 0.02 0.02 0.01
0.00 0.01 0.02 0.04 0.11 0.18 0.17 0.11 0.1 0.08 0.07 0.04 0.04 0.02 0.01
0.00 0.01 0.01 0.03 0.06 0.14 0.18 0.12 0.13 0.13 0.08 0.04 0.04 0.02 0.00
0.01 0.01 0.01 0.02 0.08 0.16 0.16 0.15 0.1 0.1 0.08 0.05 0.04 0.02 0.01
0.01 0.01 0.01 0.02 0.04 0.13 0.17 0.15 0.14 0.13 0.07 0.04 0.03 0.02 0.01
0.00 0.01 0.01 0.02 0.04 0.12 0.14 0.1 0.12 0.15 0.11 0.08 0.06 0.03 0.02
0.00 0.01 0.01 0.02 0.04 0.08 0.13 0.12 0.11 0.13 0.12 0.07 0.07 0.05 0.03
0.00 0.01 0.01 0.03 0.07 0.14 0.12 0.09 0.09 0.11 0.1 0.08 0.06 0.05 0.03
0.00 0.01 0.02 0.03 0.09 0.17 0.16 0.09 0.07 0.11 0.1 0.06 0.05 0.02 0.01
```

```
#####
#####Seine survey index#####
#Starting and ending years of the seine survey index
1996
2010
#Observed CPUE and assumed CVs
1.22 0.44 0.98 0.77 0.33 0.67 0.89 1.09 0.72 1.50 0.62 0.76 0.46 1.56 2.97
0.20 0.19 0.20 0.20 0.23 0.20 0.19 0.18 0.20 0.21 0.21 0.19 0.21 0.20 0.20
```



```
2
#Random walk switch:Integer value (choose estimation phase, negative value turns it off)
-3
#Variance (sd^2) of fishery dependent random walk catchabilities (0.03 is near the sd=0.17 of Wilberg and Bence
0.03
0.03
0.03

#Tuning F (not applied in last phase of optimization)
0.2
#Year for tuning F
2011

##threshold sample sizes for length comps (set to 99999.0 if sel is fixed)
1.0 #gill net

#threshold sample sizes (greater than or equal to) for age comps
1.0 #commerical reduction

#Ageing error matrix (columns are true age 0-4+, rows are ages as read for age comps: columns should sum to one)
1.00 0.00 0.00 0.00 0.00
0.00 1.00 0.11 0.00 0.00
0.00 0.00 0.78 0.16 0.00
0.00 0.00 0.11 0.68 0.17
0.00 0.00 0.00 0.16 0.83

999 #end of data file flag
```