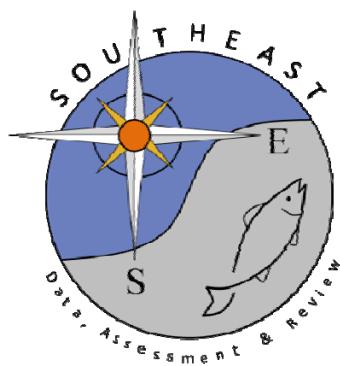


# **The Beaufort Assessment Model (BAM) with application to tilefish: mathematical description, implementation details, and computer code**

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The Beaufort Assessment Model (BAM) with application to tilefish:  
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## 1 Overview

The primary model in this assessment was the Beaufort assessment model (BAM), which applies a statistical catch-age formulation. The model was implemented with the AD Model Builder software (ADMB Foundation 2011), and its structure and equations are detailed herein. In essence, a statistical catch-age model simulates a population forward in time while including fishing processes (Quinn and Deriso 1999; Shertzer et al. 2008). Quantities to be estimated are systematically varied until characteristics of the simulated populations match available data on the real population. Statistical catch-age models share many attributes with ADAPT-style tuned and untuned VPAs.

The method of forward projection has a long history in fishery models. It was introduced by Pella and Tomlinson (1969) for fitting production models and then, among many applications, used by Fournier and Archibald (1982), by Deriso et al. (1985) in their CAGEAN model, and by Methot (1989; 2009) in his Stock Synthesis model. The catch-age model of this assessment is similar in structure to the CAGEAN and Stock Synthesis models. Versions of this assessment model have been used in previous SEDAR assessments of reef fishes in the U.S. South Atlantic, such as red porgy, black seabass, snowy grouper, gag grouper, greater amberjack, vermillion snapper, Spanish mackerel, red grouper, and red snapper, as well as in the previous tilefish benchmark (SEDAR 4).

## 2 Model configuration and equations

Model equations are detailed in Table 2.1, and AD Model Builder code is supplied in Appendix A. A general description of the assessment model follows.

**Stock dynamics** In the assessment model, new biomass was acquired through growth and recruitment, while abundance of existing cohorts experienced exponential decay from fishing and natural mortality. The population was assumed closed to immigration and emigration. The model included age classes 1 – 25+, where the oldest age class 25+ allowed for the accumulation of fish (i.e., plus group).

**Initialization** Initial (1962) abundance at age was estimated in the model as follows. First, the equilibrium age structure was computed for ages 1–25 based on natural and fishing mortality ( $F$ ), where  $F$  was set equal to a value that resulted in the 1962 biomass level equaling 90% of the unfished level. This was based on the assumption by the assessment workshop panel that the stock was lightly exploited prior to the 1960's.

**Natural mortality rate** The natural mortality rate ( $M$ ) was assumed constant over time, but decreasing with age. The form of  $M$  as a function of age was based on Lorenzen (1996). The Lorenzen (1996) approach inversely relates the natural mortality at age to mean weight at age  $W_a$  by the power function  $M_a = \alpha W_a^\beta$ , where  $\alpha$  is a scale parameter and  $\beta$  is a shape parameter. Lorenzen (1996) provided point estimates of  $\alpha$  and  $\beta$  for oceanic fishes, which were used for this assessment. As in previous SEDAR assessments, the Lorenzen estimates of  $M_a$  were rescaled to provide the same fraction of fish surviving from age-1 through the oldest observed age (40 yr) as would occur with constant  $M = 0.10$  from the DW. This approach using cumulative mortality is consistent with the findings of Hoenig (1983) and Hewitt and Hoenig (2005).

**Growth** Mean size at age of the population (total length, TL) was modeled with the von Bertalanffy equation, and weight at age (whole weight, WW) was modeled as a function of total length. Parameters of growth and conversions (TL-WW) were estimated by the DW and were treated as input to the assessment model. The von Bertalanffy parameter estimates from the DW were  $L_\infty = 825.1$ ,  $k = 0.189$ , and  $t_0 = -0.47$ . For fitting length composition data, the distribution of size at age was assumed normal with coefficient of variation (CV) estimated by the assessment model. A constant CV, rather than constant standard deviation, was suggested by the size at age data.

**Female maturity** Females were modeled to be fully mature at age 4 and the proportion mature at ages 1, 2, and 3 were estimated to be 0.1, 0.25, and 0.5 respectively (Table 2.1).

**Spawning stock** Spawning stock was modeled using mature female gonad weight measured at the time of peak spawning. For tilefish, peak spawning was considered to occur in May. In cases when reliable estimates of fecundity

are unavailable, spawning biomass, and in this case, female gonad weight, is commonly used as a proxy for population fecundity.

**Recruitment** Expected recruitment of age-1 fish was predicted from spawning stock using the Beverton–Holt spawner-recruit model. Annual variation in recruitment was assumed to occur with lognormal deviations for years 1976–2003 only. The start of recruitment residuals in 1976 was based on examination of a series of different starting years and the start of the age and length composition data that have information on year class strength. The ending year of estimated recruitment residuals (2003) is based on the age at full selection in the fisheries and the last year of age composition data.

Because the age at full selection for the tilefish fisheries generally occurs at age 7 and the last year of composition data in the model is 2010, the assessment panel agreed that recruitment deviations during 2004–2010 could not be reliably estimated.

**Landings** The model included time series of landings from three fleets: commercial longlines (1962–2010), commercial handlines (1962–2010), and general recreational (1981–2010). An “other” category in the reported landings was distributed by year between handlines and longlines based on the yearly ratio of handline to longline landings.

Landings were modeled with the Baranov catch equation (Baranov 1918) and were fitted in units of weight (1000 lb whole weight). The DW provided observed landings back to the first assessment year (1962) for each fleet except general recreational, because the MRFSS estimates started in 1981.

**Fishing Mortality** For each time series of landings, the assessment model estimated a separate full fishing mortality rate ( $F$ ). Age-specific rates were then computed as the product of full  $F$  and selectivity at age. Apical  $F$  was computed as the maximum of  $F$  at age summed across fleets.

**Selectivities** Selectivity curves applied to landings and CPUE series were estimated using a parametric approach. This approach applies plausible structure on the shape of the curves, and achieves greater parsimony than occurs with unique parameters for each age. Selectivity of landings from all fleets were modeled as flat-topped, using a two parameter logistic function. Selectivities of the fishery-dependent index was the same as that of the longline fleet. The MARMAP index was also modeled as a flat-topped, two parameter logistic function. However, a selectivity curve was not estimated for the recreational fleet due to low sample sizes and noisy composition data. Instead, the recreational selectivity was assumed to be equal to the commercial handline fishery, since both sectors use vertical hook and line.

Diffuse priors were used for estimating parameters of selectivity functions. These priors assumed normal distributions with CV = 1.0 and were intended to provide only weak information to help the optimization routine during model execution. Priors help by steering estimation away from parameter space with no response in the likelihood surface. Without these diffuse priors, it is possible during the optimization search that a selectivity parameter could become unimportant, for example if its bounds were set too wide and depending on values of other parameters. When this happens, the likelihood gradient with respect to the aimless parameter approaches zero even if the parameter is not at its globally best value. Diffuse priors help avoid that situation.

**Indices of abundance** The model was fit to two indices of relative abundance: MARMAP longline (binned years between 1985 and 2010) and commercial lines (1993–2010). The MARMAP index values were means of the binned years for both the observed and the predicted series. Predicted indices were conditional on selectivity of the corresponding fleet or survey and were computed from abundance or biomass (as appropriate) at the midpoint of the year.

**Catchability** In the BAM, catchability scales indices of relative abundance to estimated population abundance at large. Several options for time-varying catchability were implemented in the BAM following recommendations of the 2009 SEDAR procedural workshop on catchability (SEDAR Procedural Guidance 2009). In particular, the BAM allows for density dependence, linear trends, and random walk, as well as time-invariant catchability. Parameters for these models could be estimated or fixed based on *a priori* considerations. For the base model, the AW assumed

time-invariant catchability, following SEDAR 4. For a sensitivity run, however, the AW considered linearly increasing catchability with a slope of 2%, constant after 2003. Choice of the year 2003 was based on recommendations from fishermen regarding when the effects of Global Positioning Systems likely saturated in the southeast U.S. Atlantic (SEDAR 2009). This trend reflects the belief that catchability has generally increased over time as a result of improved technology (SEDAR Procedural Guidance 2009) and as estimated for reef fishes in the Gulf of Mexico (Thorson and Berkson 2010). The value of 2% has been found in other fisheries as well (Zhou et al. 2011). Another sensitivity run applied a random walk to catchability. This is notoriously difficult to estimate, often resulting in just an absorption of noise from the index. The random walk sensitivity run should not be considered a viable model run.

**Biological reference points** Biological reference points (benchmarks) were calculated based on maximum sustainable yield (MSY) estimates from the Beverton–Holt spawner-recruit model with bias correction (expected values in arithmetic space). Computed benchmarks included MSY, fishing mortality rate at MSY ( $F_{MSY}$ ), and spawning stock at MSY ( $SSB_{MSY}$ ). In this assessment, spawning stock measures total gonad weight of mature females. These benchmarks are conditional on the estimated selectivity functions and the relative contributions of each fleet's fishing mortality. The selectivity pattern used here was the effort-weighted selectivities at age, with effort from each fishery estimated as the full  $F$  averaged over the last three years of the assessment.

**Fitting criterion** The fitting criterion was a penalized likelihood approach in which observed landings were fit closely, and observed composition data and abundance indices were fit to the degree that they were compatible. Landings and index data were fitted using lognormal likelihoods. Length and age composition data were fitted using multinomial likelihoods.

The model includes the capability for each component of the likelihood to be weighted by user-supplied values (for instance, to give more influence to stronger data sources). For data components, these weights were applied by either adjusting CVs (lognormal components) or adjusting effective sample sizes (multinomial components). In this application to tilefish, CVs of landings (in arithmetic space) were assumed equal to 0.05, to achieve a close fit to these time series yet allowing some imprecision. In practice, the small CVs are a matter of computational convenience, as they help achieve the desired result of close fits to the landings, while avoiding having to solve the Baranov equation iteratively (which is complex when there are multiple fisheries). Weights on other data components (indices, age/length compositions) were adjusted iteratively, starting from initial weights as follows. The CVs of indices were set equal to the values estimated by the DW. Effective sample sizes of the multinomial components were assumed equal to the number of trips sampled annually, rather than the number of fish measured, reflecting the belief that the basic sampling unit occurs at the level of trip. These initial weights were then adjusted until standard deviations of normalized residuals were near 1.0 (SEDAR25-RW04, SEDAR25-RW06). The weight on the commercial longline index was then adjusted upward to a value of 3 (SEDAR25-RW06), in accordance with the principle that abundance data should be given primacy (Francis 2011). A range of weights for the commercial longline index component were considered (ranging from 1.0 to 6.0) before the final 3.0 weight was selected by the AW panel.

In addition, the compound objective function included several penalties or prior distributions, applied to CV of growth (based on the empirical estimate), selectivity parameters, and recruitment standard deviation based on Beddington and Cooke (1983) and Mertz and Myers (1996)]. Penalties or priors were applied to maintain parameter estimates near reasonable values, and to prevent the optimization routine from drifting into parameter space with negligible gradient in the likelihood.

**Model testing** Experiments with a reduced model structure indicated that parameters estimated from the BAM were unbiased and could be recovered from simulated data. Further, the general model structure has been through multiple SEDAR reviews. As an additional measure of quality control, tilefish code and input data were examined for accuracy by multiple analysts. This combination of testing and verification procedures suggest that the assessment model is implemented correctly and can provide an accurate assessment of tilefish stock dynamics.

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*Table 2.1. General definitions, input data, population model, and negative log-likelihood components of the statistical catch-age model applied to tilefish. Hat notation ( $\hat{}$ ) indicates parameters estimated by the assessment model, and breve notation ( $\breve{}$ ) indicates estimated quantities whose fit to data forms the objective function.*

Quantity	Symbol	Description or definition
<b>General Definitions</b>		
Index of years	$y$	$y \in \{1962 \dots 2010\}$
Index of ages	$a$	$a \in \{1, 2 \dots A\}$ , where $A = 25^+$
Index of length bins	$l$	$l \in \{1, 2 \dots 23\}$
Length bins	$l'$	$l' \in \{340, 370, \dots, 1150\text{mm}\}$ , with midpoint of 30mm bin used to match length compositions. Largest 5 length bins treated as a plus group, but retained for weight calculations.
Index of fisheries	$f$	$f \in \{1, 2, 3\}$ where 1 = commercial longlines, 2 = commercial handlines, 3 = recreational
Index of CPUE	$u$	$u \in \{1, 2\}$ where 1 = MARMAP longline, 2 = commercial logbook
Conversion factor for whole to gutted weight	$b$	$b = 1.05893$
<b>Input Data</b>		
Observed length compositions	$p_{(f,u),l,y}^\lambda$	Proportional contribution of length bin $l$ in year $y$ to fishery $f$ (landings) or index $u$
Observed age compositions	$p_{(f,u),a,y}^\alpha$	Proportional contribution of age class $a$ in year $y$ to fishery $f$ or index $u$ .
Ageing error matrix	$\mathcal{E}$	Estimated from multiple readers ageing the same otoliths.
Length comp. sample sizes	$n_{(f,u),y}^\lambda$	Effective number of length samples collected in year $y$ from fishery $f$ or index $u$
Age comp. sample sizes	$n_{(f,u),y}^\alpha$	Effective number of age samples collected in year $y$ from fishery $f$ or index $u$
Observed landings	$L_{f,y}$	Reported landings in year $y$ from fishery $f$ . Commercial $L$ in 1000 lb gutted weight, and recreational $L$ in 1000 lb whole weight.
CVs of landings	$c_{f,y}^L$	Assumed 0.05 in arithmetic space
Observed abundance indices	$U_{u,y}$	$u = 1$ , MARMAP longline (numbers), $y \in \{1985, 1998, 2002, 2006, 2010\}$ $u = 2$ , Commercial longline logbook (weight), $y \in \{1981 \dots 2010\}$
CVs of abundance indices	$c_{u,y}^U$	$u = \{1, 2\}$ as above. Annual values estimated from delta-lognormal GLM. Each time series was scaled to its mean
Natural mortality rate	$M_a$	Function of weight at age ( $w_a$ ): $M_a = \alpha w_a^\beta$ , with estimates of $\alpha$ and $\beta$ from Lorenzen (1996). Lorenzen $M_a$ then rescaled based on Hoenig estimate.
<b>Population Model</b>		
Proportion female at age	$\rho_a$	Considered constant (50:50) across years and ages
Proportion females mature at age	$m_a$	Logistic increase with age; assumed constant across years

Table 2.1. (continued)

Quantity	Symbol	Description or definition
Spawning date	$t_{\text{spawn}}$	Fraction denoting the proportional time of year when spawning occurs. Set to 0.42 for tilefish by assuming peak spawning occurs in the end of May.
Mean length at age	$l_a$	Total length (midyear); $l_a = L_\infty(1 - \exp[-K(a - t_0 + 0.5)])$ where $K$ , $L_\infty$ , and $t_0$ are parameters estimated by the DW
CV of $l_a$	$\hat{c}_a^\lambda$	Estimated coefficient of variation of growth, assumed constant across ages
SD of $l_a$	$\sigma_a^\lambda$	Standard deviation of growth, assumed constant across ages.
Age-length conversion of population	$\psi_{a,l}^u$	$\psi_{a,l}^u = \frac{1}{\sqrt{2\pi}(\sigma_a^\lambda)} \frac{\exp[-(l'_l - l_a)^2]}{(2(\sigma_a^\lambda)^2)}$ , the Gaussian density function. Matrix $\psi^u$ is rescaled to sum to one within ages, with the largest size a plus group. This matrix is constant across years and is used only to match length comps of fishery independent indices.
Age-length conversion of landings	$\psi_{f,a,l,y}^L$	$\psi_{f,a,l,y}^L = \psi_{a,l}^u$
Mean length at age of landings	$\xi_{(f),a,y}^L$	Mean length at age from $\psi_{f,a,y}^L$ for landings.
Individual weight at age of population	$w_a$	Computed from length at age by $w_a = \theta_1 l_a^{\theta_2}$ where $\theta_1$ and $\theta_2$ are parameters from the DW
Gonad weight at age of individuals	$g_a$	Computed from weight at age by $g_a = \varpi_1 w_a^{\varpi_2}$ where $\varpi_1$ and $\varpi_2$ are parameters from the DW
Individual weight at age of landings	$w_{(f),a,y}^L$	Computed from length at age by $w_{(f),a,y}^L = \theta_1 (\xi_{(f),a,y}^L)^{\theta_2}$
Fishery and index selectivities	$s_{(f,u),a}$	$s_{(f,u),a} = \frac{1}{1 + \exp[-\hat{\eta}_{(f,u)}(a - \hat{\alpha}_{(f,u)})]}$ where $\hat{\eta}_{(f,u)}$ and $\hat{\alpha}_{(f,u)}$ are estimated parameters. Not all parameters were estimated for each fishery or index; some parameters were fixed as described in the text. For instance, the selectivity of the commercial logbook index was assumed equal to that of commercial longlines. Commercial line selectivity was used as a proxy for the recreational fleet.
Fishing mortality rate of landings	$F_{f,a,y}$	$F_{f,a,y} = s_{f,a,y} \hat{F}_{f,y}$ where $\hat{F}_{f,y}$ is an estimated fully selected fishing mortality rate by fishery
Total fishing mortality rate	$F_{a,y}$	$F_{a,y} = \sum_f F_{f,a,y}$
Total mortality rate	$Z_{a,y}$	$Z_{a,y} = M_a + F_{a,y}$
Apical F	$F_y$	$F_y = \max(F_{a,y})$

Table 2.1. (continued)

Quantity	Symbol	Description or definition
Abundance at age	$N_{a,y}$	$N_{1,1962} = \frac{\hat{R}_0(0.8\zeta h\phi_{init} - 0.2\phi_0(1-\hat{h}))}{(\hat{h}-0.2)\phi_{init}}$ <p><math>\hat{N}_{1+,1962}</math> equilibrium conditions expected given assumptions about initial fishing mortality (described below)</p> $N_{0,y+1} = \frac{0.8\hat{R}_0\hat{h}S_y}{0.2\phi_0\hat{R}_0(1-\hat{h}) + (\hat{h}-0.2)S_y} \exp(\hat{R}_{y+1}) \text{ for } y \geq 1962$ $N_{a+1,y+1} = N_{a,y} \exp(-Z_{a,y}) \quad \forall a \in (0 \dots A-1)$ $N_{A,y} = N_{A-1,y-1} \frac{\exp(-Z_{A-1,y-1})}{1 - \exp(-Z_{A,y-1})}$ <p><math>\hat{R}_0</math> (asymptotic maximum recruitment) is an estimated parameter of the spawner-recruit curve, and <math>\hat{R}_y</math> are estimated annual recruitment deviations in log space. The bias correction is <math>\zeta = \exp(\widehat{\sigma_R}^2/2)</math>, where <math>\widehat{\sigma_R}^2</math> is the estimated variance of recruitment deviations.</p> <p>In the SEDAR-25 baserun, <math>h = 0.84</math> was a fixed parameter. Quantities <math>\phi_0</math>, <math>\phi_{init}</math>, and <math>S_y</math> are described below.</p>
Abundance at age (mid-year)	$N'_{a,y}$	Used to match indices of abundance $N'_{a,y} = N_{a,y} \exp(-Z_{a,y}/2)$
Abundance at age at time of spawning	$N''_{a,y}$	Assumed in May to correspond with peak spawning $N''_{a,y} = \exp(-t_{spawn} Z_{a,y}) N_{a,y}$
Unfished abundance at age per recruit at time of spawning	$NPR_a$	$NPR_0 = 1 \times \exp(-t_{spawn} M_0)$ $NPR_{a+1} = NPR_a \exp[-(M_a(1-t_{spawn}) + M_{a+1}t_{spawn})] \quad \forall a \in (0 \dots A-1)$ $NPR_A = \frac{NPR_{A-1} \exp[-(M_{A-1}(1-t_{spawn}) + M_A t_{spawn})]}{1 - \exp(-M_A)}$
Initial abundance at age per recruit at time of spawning	$NPR_a^{init}$	Same calculations as for $NPR_a$ , but including fishing mortality (see $Z^{init}$ below).
Unfished spawning biomass per recruit	$\phi_0$	$\phi_0 = \sum_{a=0}^A NPR_a \rho_a m_a g_a$ <p>In units of mature female gonad weight.</p>
Initial spawning biomass per recruit	$\phi_{init}$	$\phi_{init} = \sum_{a=0}^A NPR_a^{init} \rho_a m_a g_a$ <p>In units of mature female gonad weight.</p>
Spawning biomass	$S_y$	$\sum_{a=1}^A N''_{a,y} \rho_a m_a g_a$ <p>Also referred to as spawning biomass in units of total mature female gonad weight.</p>
Initialization mortality at age	$Z_a^{init}$	$Z_a^{init} = M_a + s_a^{init} F^{init}$ <p>where <math>F^{init}</math> is an initialization <math>F</math> assumed to be that required to match a 10% depletion from virgin conditions in 1962. <math>s_a^{init}</math> is set to the commercial line selectivity. In the SEDAR-25 baserun, <math>F^{init} = 0.01</math> was fixed.</p>
Initial equilibrium abundance at age	$N_a^{equil}$	Equilibrium age structure given $Z_a^{init}$
Population biomass	$B_y$	$B_y = \sum_a N_{a,y} w_a$
Landings at age in numbers	$L'_{f,a,y}$	$L'_{f,a,y} = \frac{F_{f,a,y}}{Z_{a,y}} N_{a,y} [1 - \exp(-Z_{a,y})]$
Landings at age in whole weight	$L''_{f,a,y}$	$L''_{f,a,y} = w_{f,a,y}^L L'_{f,a,y}$

Table 2.1. (continued)

Quantity	Symbol	Description or definition
Landings at age in gutted weight	$L''_{f,a,y}$	$L''_{f,a,y} = bL''_{f,a,y}$
Index catchability	$q_{u,y}$	<p><math>q_{u,1993} = \hat{q}_u^0 f(\text{density})</math></p> <p><math>q_{u,y+1} = q_{u,y} f_y(\text{trend}) f_y(\text{random}) f_y(\text{density})</math> for <math>y \geq 1993</math></p> <p>Here, <math>f_y(\text{density}) = (B'_0)^{\hat{\psi}} (B'_y)^{-\hat{\psi}}</math>, where <math>\hat{\psi}</math> is a parameter to be estimated, <math>B'_y = \sum_{a=a'}^A B_{a,y}</math> is annual biomass above some threshold age <math>a'</math>, and <math>B'_0</math> is virgin biomass for ages <math>a'</math> and greater. In practice, <math>a'</math> should be set high enough to give a reasonable summary of exploitable biomass. The function <math>f(\text{trend})</math> provides a model for linear trend (slope of <math>\beta_q</math>) in catchability from the start of the index until 2003, where technology effects were thought to saturate (see SEDAR 19 DW report). For example, for an index that starts in 1993, <math>f_y(\text{trend})</math> follows,</p> $f_y(\text{trend}) = \begin{cases} 1.0 & : y = 1993 \\ f_{y-1}(\text{trend}) * (y - 1993)\beta_q & : 1993 < y \leq 2003 \\ f_{2003}(\text{trend}) & : 2003 < y \end{cases}$ <p>Finally, <math>f_y(\text{random}) = \exp(\epsilon_{u,y})</math> are lognormal catchability deviations which allow for a random walk in catchability when penalties are placed on the <math>\epsilon_{u,y}</math> (see “Objective Function”). In practice, the catchability function <math>f_y(\text{trend})</math> was used as described for the SEDAR-25 tilefish assessment. Density dependence and random walks were not applied in the baserun.</p>
Predicted landings	$\check{L}_{f,y}$	$\check{L}_{f,y} = \begin{cases} \sum_a L''_{f,a,y} & : f = 1, 2 \\ \sum_a L''_{f,a,y} & : f = 3 \end{cases}$
Predicted length compositions of fishery independent data	$\check{p}_{u,l,y}^\lambda$	$\check{p}_{u,l,y}^\lambda = \frac{\sum_a \psi_{a,l} s_{u,a,y} N'_{a,y}}{\sum_a s_{u,a,y} N'_{a,y}}$
Predicted length compositions of landings	$\check{p}_{f,l,y}^\lambda$	$\check{p}_{f,l,y}^\lambda = \frac{\sum_a \psi_{f,a,l,y}^L L'_{f,a,y}}{\sum_a L'_{f,a,y}}$
Predicted age compositions	$\check{p}_{(f,u),a,y}^\alpha$	$\check{p}_{(f,u),a,y}^\alpha = \frac{L'_{(f,u),a,y}}{\sum_a L'_{(f,u),a,y}}$
Predicted CPUE	$\check{U}_{u,y}$	$\check{U}_{u,y} = \begin{cases} \hat{q}_{u,y} \sum_a N'_{a,y} s_{u,a} & : u = 1 \\ \hat{q}_{u,y} \sum_a w_{u,a,y}^L N'_{a,y} s_{u,a} & : u = 2 \end{cases}$

where  $y'$  corresponds to the years used as means of the binned index.  $s_{u,a}$  is the selectivity of the relevant fishery in the year corresponding to  $y$ .

Table 2.1. (continued)

Quantity	Symbol	Description or definition
<b>Objective Function</b>		
Multinomial compositions length	$\Lambda_1$	$\Lambda_1 = - \sum_{f,u} \sum_y \left[ \omega_{(f,u)}^\lambda n_{(f,u),y}^\lambda \sum_l (p_{(f,u),l,y}^\lambda + x) \log \left( \frac{(\check{p}_{(f,u),l,y}^\lambda + x)}{(p_{(f,u),l,y}^\lambda + x)} \right) \right]$ <p>where <math>\omega_{(f,u)}^\lambda</math> is a preset weight (selected by iterative re-weighting) and <math>x = 1e-5</math> is an arbitrary value to avoid log zero. The denominator of the log is a scaling term. Bins are 30 mm wide.</p>
Multinomial age compositions	$\Lambda_2$	$\Lambda_2 = - \sum_{f,u} \sum_y \left[ \omega_{(f,u)}^\alpha n_{(f,u),y}^\alpha \sum_a (p_{(f,u),a,y}^\alpha + x) \log \left( \frac{(\check{p}_{(f,u),a,y}^\alpha + x)}{(p_{(f,u),a,y}^\alpha + x)} \right) \right]$ <p>where <math>\omega_{(f,u)}^\alpha</math> is a preset weight (selected by iterative re-weighting) and <math>x = 1e-5</math> is an arbitrary value to avoid log zero. The denominator of the log is a scaling term.</p>
Lognormal landings	$\Lambda_3$	$\Lambda_3 = \sum_f \sum_y \frac{\left[ \log((L_{f,y} + x) / (\check{L}_{f,y} + x)) \right]^2}{2(\sigma_{f,y}^L)^2}$ <p>where <math>x = 1e-5</math> is an arbitrary value to avoid log zero or division by zero. Here, <math>\sigma_{f,y}^L = \sqrt{\log(1 + (c_{f,y}^L / \omega_f^L)^2)}</math>, with <math>\omega_f^L = 1</math> a preset weight.</p>
Lognormal CPUE	$\Lambda_4$	$\Lambda_4 = \sum_u \sum_y \frac{\left[ \log((U_{u,y} + x) / (\check{U}_{u,y} + x)) \right]^2}{2(\sigma_{u,y}^U)^2}$ <p>where <math>x = 1e-5</math> is an arbitrary value to avoid log zero or division by zero. Here, <math>\sigma_{u,y}^U = \sqrt{\log(1 + (c_{u,y}^U / \omega_u^U)^2)}</math>, with <math>\omega_u^U = 1</math> a preset weight.</p>
Lognormal recruitment deviations	$\Lambda_5$	$\Lambda_5 = \omega_5 \left[ \frac{[R_{1976} + (\hat{\sigma}_R^2/2)]^2}{2\hat{\sigma}_R^2} + \sum_{y>1976} \frac{[(R_y - \hat{\varrho}R_{y-1}) + (\hat{\sigma}_R^2/2)]^2}{2\hat{\sigma}_R^2} + n \log(\sigma_R) \right]$ <p>where <math>R_y</math> are recruitment deviations in log space, <math>n</math> is the number of years, <math>\omega_5 = 1</math> is a preset weight, <math>\hat{\varrho}</math> is the first-order autocorrelation, and <math>\hat{\sigma}_R^2</math> is the estimated recruitment variance (<math>\varrho = 0</math> in the SEDAR-25 base run).</p>
Additional constraint on early recruitment deviations	$\Lambda_6$	$\Lambda_6 = \omega_6 \left[ \frac{[R_{1976} + (\hat{\sigma}_R^2/2)]^2}{2\hat{\sigma}_R^2} + \sum_{y=1977}^{Y_1} \frac{[(R_y - \hat{\varrho}R_{y-1}) + (\hat{\sigma}_R^2/2)]^2}{2\hat{\sigma}_R^2} + n \log(\sigma_R) \right]$ <p>where <math>Y_1</math> is the last year to apply this additional penalty and <math>\omega_6</math> is a preset weight, with <math>\omega_6=0.0</math> for the SEDAR-25 tilefish base run.</p>
Additional constraint on final recruitment deviations	$\Lambda_7$	$\Lambda_7 = \omega_7 \left[ \sum_{y=Y_2}^Y \frac{[(R_y - \hat{\varrho}R_{y-1}) + (\hat{\sigma}_R^2/2)]^2}{2\hat{\sigma}_R^2} + n \log(\sigma_R) \right]$ <p>where <math>Y_2</math> is the first year to apply this additional penalty, <math>Y</math> is the terminal year, and <math>\omega_7</math> is a preset weight, with <math>\omega_7=0.0</math> for the SEDAR-25 tilefish base run.</p>
Penalty on random walk on catchability	$\Lambda_8$	$\Lambda_8 = \omega_8 \sum_u \sum_y \frac{\epsilon_{u,y}^2}{2(\sigma_u^q)^2}$ <p>where <math>\omega_8</math> is a preset weight and <math>\sigma_u^q</math> is a control variable input by the user defining the standard deviation of the random walk process. As <math>\sigma_u^q</math> increases, one essentially estimates each deviation as a free parameter, while values close to zero allow little variation in annual catchability. A random walk on catchability was not used for the SEDAR-25 tilefish baserun, thus <math>\omega_8=0.0</math>.</p>
Penalty on initial age structure	$\Lambda_9$	$\Lambda_9 = N_a^{eq}$ <p>where <math>N_a^{eq}</math> is the equilibrium age structure given the initial <math>F</math>, as defined previously.</p>

Table 2.1. (continued)

Quantity	Symbol	Description or definition
Prior distributions and penalties	$\Lambda_{10}$	is the sum of penalty terms used to implement prior distributions on several parameters. Normal priors were applied to $\widehat{\sigma}_R$ , $\widehat{c}_a^\lambda$ , $\widehat{\eta}_{(f,u)}$ , and $\widehat{\alpha}_{(f,u)}$ . Normal distributions required a value to describe variance. Empirical estimates of standard deviation were available and therefore used for $c_a^\lambda$ and $\sigma_R$ . All other normal priors assumed CV=0.5 (i.e., diffuse priors).
Apical $F$ penalty	$\Lambda_{11}$	$\Lambda_{11} = \begin{cases} 0 & : F_{apex} < 1 \\ \omega_{11} \times \exp^{\sqrt{(F_{apex}-1)}} - 1 & : F_{apex} > 1 \end{cases}$ where $\omega_{11} = 10$ .
Total objective function	$\Lambda$	$\Lambda = \sum_{i=1}^{11} \Lambda_i$ Objective function minimized by the assessment model

## **Appendix A AD Model Builder code to implement the Beaufort Assessment Model**

```

#####
##Commercial handline fishery
// Landings (1000 lb gutted weight)
init_int styr_ch_L;
init_int endyr_ch_L;
init_vector obs_ch_L(styr_ch_L,endyr_ch_L);
init_vector ch_L_cv(styr_ch_L,endyr_ch_L); //vector of CV of landings by year
// Length Compositions (3 cm bins, data from handline)
init_int nyr_ch_lenc;
init_ivector yrs_ch_lenc(1,nyr_ch_lenc);
init_vector nsamp_ch_lenc(1,nyr_ch_lenc);
init_matrix obs_ch_lenc(1,nyr_ch_lenc,1,nlenbins);
// Age Compositions (data from handline)
init_int nyr_ch_agec;
init_ivector yrs_ch_agec(1,nyr_ch_agec);
init_vector nsamp_ch_agec(1,nyr_ch_agec);
init_matrix obs_ch_agec(1,nyr_ch_agec,1,nages);

#####
#####Recreational (all sectors) fishery #####
// Landings (1000 fish)
init_int styr_ra_L;
init_int endyr_ra_L;
init_vector obs_ra_L(styr_ra_L,endyr_ra_L);
init_vector ra_L_cv(styr_ra_L,endyr_ra_L);
// Length Compositions (3 cm bins) of landings
init_int nyr_ra_lenc;
init_ivector yrs_ra_lenc(1,nyr_ra_lenc);
init_vector nsamp_ra_lenc(1,nyr_ra_lenc);
init_matrix obs_ra_lenc(1,nyr_ra_lenc,1,nlenbins);

#####
##### MARMAP Longline data #####
//CPUE
init_int nyr_mm_cpue;
init_ivector yrs_mm_cpue(1,nyr_mm_cpue); //middle year in group of years to be combined
init_vector obs_mm_cpue(1,nyr_mm_cpue); //Observed CPUE
init_vector mm_cpue_cv(1,nyr_mm_cpue); //CV of cpue
// Length Compositions (3 cm bins)
//init_int nyr_mm_lenc;
//init_ivector yrs_mm_lenc(1,nyr_mm_lenc); //middle year in group of years to be combined
//init_vector nsamp_mm_lenc(1,nyr_mm_lenc);
//init_matrix obs_mm_lenc(1,nyr_mm_lenc,1,nlenbins);
// Age Compositions (data from MARMAP)
init_int nyr_mm_agec;
init_ivector yrs_mm_agec(1,nyr_mm_agec); //middle year in group of years to be combined
init_vector nsamp_mm_agec(1,nyr_mm_agec);
init_matrix obs_mm_agec(1,nyr_mm_agec,1,nages);

#####
#####Parameter values and initial guesses #####
#####
// Von Bert parameters in TL mm all fish
init_number set_Linf;
init_number set_K;
init_number set_t0;
// Von Bert parameters in TL mm females only
init_number set_Linf_f;
init_number set_K_f;
init_number set_t0_f;
//Standard errors of von bert params all fish
init_number set_Linf_se;
init_number set_K_se;
init_number set_t0_se;
//CV of length at age and its standard error all fish
init_number set_len_cv;
init_number set_len_cv_se;
//TL(mm)-weight(whole weight in mt) relationship: W=aL^b
init_number wgtpar_a;
init_number wgtpar_b;
//weight(whole weight)-gonad weight (units=g) relationship: GW=a+b*W
init_number gwtgtpar_a;
init_number gwtgtpar_b;
//gutted weight to whole weight conversion factor
init_number gut2whole;
//Female maturity and proportion female at age
init_vector maturity_f_obs(1,nages); //proportion females mature at age
init_vector prop_f_obs(1,nages); //proportion female at age

init_number spawn_time_frac; //time of year of peak spawning, as a fraction of the year
// Natural mortality
init_vector set_M(1,nages); //age-dependent: used in model
init_number set_M_constant; //age-independent: used only for MSST and to scale age dependent M, prior if M is estimated
init_number set_M_constant_se; //SE of age-independent M, used in prior, if M is estimated
init_number max_obs_age; //max observed age, used to scale M

//Spawner-recruit parameters (Initial guesses or fixed values)
init_number set_stEEP; //recruitment steepness
init_number set_stEEP_se; //SE of recruitment steepness
init_number set_log_R0; //recruitment R0
init_number set_R_autocorr; //recruitment autocorrelation
init_number set_rec_sigma; //recruitment standard deviation in log space
init_number set_rec_sigma_se; //SE of recruitment standard deviation in log space

//Initial guesses or fixed values of estimated selectivity parameters

init_number set_selpar_L50_cl;
init_number set_selpar_slope_cl;
//init_number set_selpar_L502_cl;
//init_number set_selpar_slope2_cl;
//init_number set_selpar_min_cl;
//init_number set_selpar_afull_cl;
//init_number set_selpar_peak_cl;
//init_number set_selpar_top_cl;
//init_number set_selpar_ascwid_cl;
//init_number set_selpar_decwid_cl;

```

```

//init_number set_selpar_init_cL;
//init_number set_selpar_final_cL;

//init_number set_selpar_L50_cL2;
//init_number set_selpar_slope_cL2;

init_number set_selpar_L50_cH;
init_number set_selpar_slope_cH;
//init_number set_selpar_L502_cH;
//init_number set_selpar_slope2_cH;
//init_number set_selpar_min_cH;
//init_number set_selpar_aufull_cH;
//init_number set_selpar_peak_cH;
//init_number set_selpar_top_cH;
//init_number set_selpar_ascwid_cH;
//init_number set_selpar_decwid_cH;
//init_number set_selpar_init_cH;
//init_number set_selpar_final_cH;

init_number set_selpar_L50_rA;
init_number set_selpar_slope_rA;
//init_number set_selpar_L502_rA;
//init_number set_selpar_slope2_rA;
//init_number set_selpar_min_rA;
//init_number set_selpar_aufull_rA;
//init_number set_selpar_peak_rA;
//init_number set_selpar_top_rA;
//init_number set_selpar_ascwid_rA;
//init_number set_selpar_decwid_rA;
//init_number set_selpar_init_rA;
//init_number set_selpar_final_rA;

init_number set_selpar_L50_mm;
init_number set_selpar_slope_mm;
//init_number set_selpar_L502_mm;
//init_number set_selpar_slope2_mm;
//init_number set_selpar_min_mm;
//init_number set_selpar_aufull_mm;
//init_number set_selpar_peak_mm;
//init_number set_selpar_top_mm;
//init_number set_selpar_ascwid_mm;
//init_number set_selpar_decwid_mm;
//init_number set_selpar_init_mm;
//init_number set_selpar_final_mm;

----weights for likelihood components-----
init_number set_w_L;
init_number set_w_lc_cL;
init_number set_w_lc_cH;
init_number set_w_lc_rA;
//init_number set_w_lc_mm;
init_number set_w_ac_cL;
init_number set_w_ac_cH;
init_number set_w_ac_mm;
init_number set_w_l_mm;
init_number set_w_l_cL;
init_number set_w_rec;           //for fitting S-R curve
init_number set_w_rec_early;    //additional constraint on early years recruitment
init_number set_w_rec_end;      //additional constraint on ending years recruitment
init_number set_w_fullF;        //penalty for any Fapex>3 (removed in final phase of optimization)
init_number set_w_Ftune;         //weight applied to tuning F (removed in final phase of optimization)
//init_number set_w_cvlen_dev;   //penalty on cv deviations at age
//init_number set_w_cvlen_diff;  //penalty on first difference of cv deviations at age

-----index catchability-----
init_number set_logq_mm;        //catchability coefficient (log) for MARMAP longline CPUE index
init_number set_logq_cL;         //catchability coefficient (log) for commercial logbook CPUE index

//rate of increase on q
init_int set_q_rate_phase;     //value sets estimation phase of rate increase, negative value turns it off
init_number set_q_rate;
//density dependence on fishery q's
init_int set_q_DD_phase;       //value sets estimation phase of random walk, negative value turns it off
init_number set_q_DD_beta;      //value of 0.0 is density independent
init_number set_q_DD_beta_se;
init_int set_q_DD_stage;        //age to begin counting biomass, should be near full exploitation

//random walk on fishery q's
init_int set_q_RW_phase;        //value sets estimation phase of random walk, negative value turns it off
init_number set_q_RW_cL_var;    //assumed variance of RW q

-----F's-----
init_number set_log_avg_F_cL;
init_number set_log_avg_F_cH;
init_number set_log_avg_F_rA;
init_number set_F_init;          //initial F, scaled by F_init_ratio

//Tune Fapex (tuning removed in final year of optimization)
init_number set_Ftune;
init_int set_Ftune_yr;

//threshold sample sizes for length comps
init_number minSS_cL_lenc;
init_number minSS_cH_lenc;
init_number minSS_rA_lenc;
//init_number minSS_mm_lenc;

//threshold sample sizes for age comps
init_number minSS_cL_agec;
init_number minSS_cH_agec;
init_number minSS_mm_agec;

//ageing error matrix (columns are true ages, rows are ages as read for age comps: columns should sum to one)
init_matrix age_error(1,nages,1,nages);

```



```

matrix ErrorFree_ch_agec(1,nyr_ch_agec,1,nages);
matrix pred_mm_agec(1,nyr_mm_agec,1,nages);
matrix ErrorFree_mm_agec(1,nyr_mm_agec,1,nages);

//effective sample size applied in multinomial distributions
vector nsamp_cl_lenc_allyr(styr,endyr);
vector nsamp_ch_lenc_allyr(styr,endyr);
vector nsamp_A_lenc_allyr(styr,endyr);
//vector nsamp_mm_lenc_allyr(styr,endyr);
vector nsamp_cl_agec_allyr(styr,endyr);
vector nsamp_ch_agec_allyr(styr,endyr);
vector nsamp_mm_agec_allyr(styr,endyr);

//Computed effective sample size for output (not used in fitting)
vector neff_cl_lenc_allyr_out(styr,endyr);
vector neff_ch_lenc_allyr_out(styr,endyr);
vector neff_ra_lenc_allyr_out(styr,endyr);
//vector neff_mm_lenc_allyr_out(styr,endyr);
vector neff_cl_agec_allyr_out(styr,endyr);
vector neff_ch_agec_allyr_out(styr,endyr);
vector neff_mm_agec_allyr_out(styr,endyr);

//-----Population-----
matrix N(styr,endyr+1,1,nages); //Population numbers by year and age at start of yr
matrix N_ndyr(styr,endyr,1,nages); //Population numbers by year and age at mdpt of yr: used for comps and cpue
matrix N_spawn(styr,endyr,1,nages); //Population numbers by year and age at peaking spawning: used for SSB
//init_bounded_vector log_Nage_dev(2,nages,-5,3,1); //log deviations on initial abundance at age
vector log_Nage_dev(2,nages);
vector log_Nage_dev_output(1,nages); //used in output. equals zero for first age
matrix B(styr,endyr+1,1,nages); //Population biomass by year and age at start of yr
vector totB(styr,endyr+1); //Total biomass by year
vector totN(styr,endyr+1); //Total abundance by year
vector SSB(styr,endyr); //Total spawning biomass by year (total mature female gonad weight)
vector MatFemb(styr,endyr); //Total spawning biomass by year (total mature female biomass)
vector rec(styr,endyr+1); //Recruits by year
vector prop_f(1,nages); //Proportion female by age
vector maturity_f(1,nages); //Proportion of female mature at age
vector reprod(1,nages); //vector used to compute spawning biomass (total mature female gonad weight)
vector reprod2(1,nages); //vector used to compute mature female biomass

//----Stock-Recruit Function (Beverton-Holt, steepness parameterization)-----
init_bounded_number log_R0(8,18,1); //log(virgin Recruitment)
//number log_R0;
number RO; //virgin recruitment
init_bounded_number steep(0.21,0.991,-3); //steepness
//number steep; //uncomment to fix steepness, comment line directly above
init_bounded_number rec_sigma(0.2,1.2,4); //sd recruitment residuals
number rec_sigma_sq; //square of rec_sigma
number rec_logL_add; //additive term in -logL term

init_bounded_dev_vector log_rec_dev(styr_rec_dev,endyr_rec_dev,-5,5,3); //log recruitment deviations
//init_bounded_vector log_rec_historic(styr+1,styr_rec_dev-1,-5,5,3); //log recruitment deviations early period
//vector log_rec_dev(styr_rec_dev,endyr);
vector log_rec_dev_output(styr,endyr+1); //used in output. equals zero except for yrs in log_rec_dev
//vector log_rec_historic_dev_output(styr,endyr+1); //used in output. equals zero except for yrs in log_rec_dev

number var_rec_dev; //variance of log recruitment deviations, from yrs with unconstrained S-R(XXXX-XXXX)
number sigma_rec_dev; //sample SD of log residuals (may not equal rec_sigma)

number BiasCor; //Bias correction in equilibrium recruits
init_bounded_number R_autocorr(-1.0,1.0,-4); //autocorrelation in SR
number S0; //equal to spr_FO*RO = virgin SSB
number B0; //equal to bpr_FO*RO = virgin B
number R1; //Recruits in styr
number R_virgin; //unfinished recruitment with bias correction
vector SdS0(styr,endyr); //SSB / virgin SSB

//-----Selectivity-----
//-----Commercial longline-----
matrix sel_CL(styr,endyr,1,nages);
init_bounded_number selpar_L50_CL(1.0,10.0,2);
init_bounded_number selpar_slope_CL(0.5,12.0,2);
//init_bounded_number selpar_L502_CL(4.0,15.0,-3);
//init_bounded_number selpar_slope2_CL(0.1,5.0,-3);
//init_bounded_number selpar_min_CL(0.0,1.0,-3);
//init_bounded_number selpar_afull_CL(4.0,8.0,-3); //location in age vector (=age only if age1=1) for joining ascending and descending curves
//init_bounded_number selpar_peak_CL(0.0,19.8,2);
//init_bounded_number selpar_top_CL(-5,3,4);
//init_bounded_number selpar_ascwid_CL(-4,12,4);
//init_bounded_number selpar_decwid_CL(-2,6,-4);
//init_bounded_number selpar_init_CL(-15,5,-4);
//init_bounded_number selpar_final_CL(-5,5,-4);

//init_bounded_number selpar_L50_CL2(4.0,12.0,2);
//init_bounded_number selpar_slope_CL2(0.5,12.0,2);

//-----Commercial handline-----
matrix sel_CH(styr,endyr,1,nages);
init_bounded_number selpar_L50_CH(1.0,10.0,2);
init_bounded_number selpar_slope_CH(0.5,12.0,2);
//init_bounded_number selpar_L502_CH(2.0,10.0,-3);
//init_bounded_number selpar_slope2_CH(0.1,5.0,-3);
//init_bounded_number selpar_min_CH(0.0,1.0,-3);
//init_bounded_number selpar_afull_CH(4.0,8.0,-3); //location in age vector (=age only if age1=1) for joining ascending and descending curves
//init_bounded_number selpar_peak_CH(0.0,19.8,2);
//init_bounded_number selpar_top_CH(-5,3,2);
//init_bounded_number selpar_ascwid_CH(-4,12,4);
//init_bounded_number selpar_decwid_CH(-2,6,-4);
//init_bounded_number selpar_init_CH(-15,5,-4);
//init_bounded_number selpar_final_CH(-5,5,-4);

```

```

//Recreational-----
matrix sel_ra(styr,endyr,1,nages);
init_bounded_number selpar_l50_ra(1.0,10.0,-2);
init_bounded_number selpar_slope_ra(0.5,12.0,-2);
//init_bounded_number selpar_l502_ra(2.0,10.0,-3);
//init_bounded_number selpar_slope2_ra(0.1,5.0,-3);
//init_bounded_number selpar_min_ra(0.0,1.0,-3);
//init_bounded_number selpar_afull_ra(4.0,8.0,-3); //location in age vector (=age only if age!=1) for joining ascending and descending curves
//init_bounded_number selpar_peak_ra(0.0,19.8,2);
//init_bounded_number selpar_top_ra(-5,3,2);
//init_bounded_number selpar_ascwid_ra(-4,12,4);
//init_bounded_number selpar_decwid_ra(-2,6,-4);
//init_bounded_number selpar_init_ra(-15,5,-4);
//init_bounded_number selpar_final_ra(-5,5,-4);

/////MARMAP selectivity-----
matrix sel_mm(styr,endyr,1,nages);
init_bounded_number selpar_l50_mm(1.0,10.0,2);
init_bounded_number selpar_slope_mm(0.5,12.0,2);
//init_bounded_number selpar_l502_mm(2.5,15.0,-3);
//init_bounded_number selpar_slope2_mm(0.1,12.0,-3);
//init_bounded_number selpar_min_mm(0.0,1.0,-3);
//init_bounded_number selpar_afull_mm(4.0,8.0,-3); //location in age vector (=age only if age!=1) for joining ascending and descending curves
//init_bounded_number selpar_peak_mm(0.0,19.8,2);
//init_bounded_number selpar_top_mm(-5,3,2);
//init_bounded_number selpar_ascwid_mm(-4,12,4);
//init_bounded_number selpar_decwid_mm(-2,6,-4);
//init_bounded_number selpar_init_mm(-15,5,-4);
//init_bounded_number selpar_final_mm(-5,5,-4);

//Weighted total selectivity-----
//effort-weighted, recent selectivities
vector sel_wgted_l(i,nages); //toward landings
vector sel_wgted_tot(i,nages); //toward Z, landings plus deads discards

//-----
//-----CPUE Predictions-----
vector pred_mm_cpue(i,nyr_mm_cpue); //predicted MARMAP U
matrix N_mm(i,nyr_mm_cpue,1,nages); //used to compute MARMAP CPUE index
vector pred_mm_cpue_allyr(styr,endyr); // used for graphing purposes, fills in consec years
vector obs_mm_cpue_allyr(styr,endyr); // used for graphing purposes, fills in consec years
vector mm_cpue_cv_allyr(styr,endyr); // used for graphing purposes, fills in consec years
vector pred_cl_cpue(styr_cl_cpue,endyr_cl_cpue); //predicted CL U (pounds/hook-hour)
matrix N_cl(styr_cl_cpue,1,nages); //used to compute CL index

//---Catchability (CPUE q's)-----
init_bounded_number log_q_cl(-14,-4,1);
init_bounded_number log_q_mm(-14,-4,1);
init_bounded_number q_rate(0.001,0.1,set_q_rate_phase);
//number q_rate;
vector q_rate_fcn_cl(styr_cl_cpue,endyr_cl_cpue); //increase due to technology creep (saturates in 2003)

init_bounded_number q_DD_beta(0.1,0.9,set_q_DD_phase);
//number q_DD_beta;
vector q_DD_fcn(styr,endyr); //density dependent function as a multiple of q (scaled a la Katsukawa and Matsuda. 2003)
number BO_q_DD; //BO of ages q_DD_age plus
vector B_q_DD(styr,endyr); //annual biomass of ages q_DD_age plus

init_bounded_vector q_RW_log_dev_cL(styr_cl_cpue,endyr_cl_cpue,-3.0,3.0,set_q_RW_phase);

vector q_cL(styr_cl_cpue,endyr_cl_cpue);
number q_mm;

//-----
//--Landings in numbers (total or 1000 fish) and in wgt (kib)-----
matrix L_CL_num(styr,endyr,1,nages); //landings (numbers) at age
matrix L_CL_klb(styr,endyr,1,nages); //landings (1000 lb whole weight) at age
vector pred_cl_L_knum(styr,endyr); //yearly landings in 1000 fish summed over ages
vector pred_cl_L_klb(styr,endyr); //yearly landings in 1000 lb summed over ages

matrix L_CH_num(styr,endyr,1,nages); //landings (numbers) at age
matrix L_CH_klb(styr,endyr,1,nages); //landings (1000 lb whole weight) at age
vector pred_ch_L_knum(styr,endyr); //yearly landings in 1000 fish summed over ages
vector pred_ch_L_klb(styr,endyr); //yearly landings in 1000 lb summed over ages

matrix L_RA_num(styr,endyr,1,nages); //landings (numbers) at age
matrix L_RA_klb(styr,endyr,1,nages); //landings (1000 lb whole weight) at age
vector pred_ra_L_knum(styr,endyr); //yearly landings in 1000 fish summed over ages
vector pred_ra_L_klb(styr,endyr); //yearly landings in 1000 lb summed over ages
vector obs_RA_L_klb(styr,endyr); //yearly landings observed, perhaps adjusted for multiplicative bias

matrix L_total_num(styr,endyr,1,nages); //total landings in number at age
matrix L_total_klb(styr,endyr,1,nages); //landings in klb at age
vector L_total_knum_yr(styr,endyr); //total landings in 1000 fish by yr summed over ages
vector L_total_klb_yr(styr,endyr); //total landings (klb) by yr summed over ages

//----MSY calcs-----
number F_CL_prop; //proportion of F_sum attributable to hal, last X*selpar_n_yrs_wgted yrs, used for avg body weights
number F_CH_prop; //proportion of F_sum attributable to diving, last X yrs
number F_RA_prop; //proportion of F_sum attributable to headboat, last X yrs
number F_temp_sum; //sum of geom mean Fsum's in last X yrs, used to compute F_fishery_prop

vector F_end(i,nages);
vector F_end_L(i,nages);
number F_end_apex;

number SSB_msy_out; //SSB (total mature biomass) at msy
number F_msy_out; //F at msy
number msy_klb_out; //max sustainable yield (1000 lb)
number msy_knum_out; //max sustainable yield (1000 fish)
number B_msy_out; //total biomass at MSY
number R_msy_out; //equilibrium recruitment at F=Fmsy
number spr_msy_out; //spr at F=Fmsy

```

```

vector N_age_msy(1,nages);           //numbers at age for MSY calculations: beginning of yr
vector N_age_msy_mdyr(1,nages);     //numbers at age for MSY calculations: mdpt of yr
vector L_age_msy(1,nages);          //catch at age for MSY calculations
vector Z_age_msy(1,nages);          //total mortality at age for MSY calculations
vector F_L_age_msy(1,nages);        //fishing mortality landings (not discards) at age for MSY calculations
vector F_msy(1,n_iter_msy);         //values of full F to be used in equilibrium calculations
vector spr_msy(1,n_iter_msy);       //reproductive capacity-per-recruit values corresponding to F values in F_msy
vector R_eq(1,n_iter_msy);          //equilibrium recruitment values corresponding to F values in F_msy
vector L_eq_klb(1,n_iter_msy);      //equilibrium landings(klb) values corresponding to F values in F_msy
vector L_eq_knum(1,n_iter_msy);     //equilibrium landings(1000 fish) values corresponding to F values in F_msy
vector SSB_eq(1,n_iter_msy);        //equilibrium reproductive capacity values corresponding to F values in F_msy
vector B_eq(1,n_iter_msy);          //equilibrium biomass values corresponding to F values in F_msy
vector D_eq_klb(1,n_iter_msy);      //equilibrium discards (klb) corresponding to F values in F_msy
vector D_eq_knum(1,n_iter_msy);     //equilibrium discards (1000s) corresponding to F values in F_msy

vector PdF_msy(styr,endyr);
vector SdSSB_msy(styr,endyr);
number SdSSB_msy_end;
number PdF_msy_end;
number PdF_msy_end_mean;           //geometric mean of last 3 yrs

vector wgt_wgted_L_klb(1,nages);   //fishery-weighted average weight at age of landings
number wgt_wgted_L_denom;          //used in intermediate calculations

number iter_inc_msy;               //increments used to compute msy, equals 1/(n_iter_msy-1)

//-----Mortality-----

// Stuff immediately below used only if M is estimated
// //init_bounded_number M_constant(0.1,0.2,1);           //age-independent: used only for MSST
// vector Mscale_ages(1,max_obs_age);
// vector Mscale_len(1,max_obs_age);
// vector Mscale_wgt_g(1,max_obs_age);
// vector M_lorenzen(1,max_obs_age);
// number cum_surv_1plus;

vector M(1,nages);                //age-dependent natural mortality
number M_constant;                //age-independent: used only for MSST

matrix F(styr,endyr,1,nages);      //Full fishing mortality rate by year
vector Fsum(styr,endyr);          //Max across ages, fishing mortality rate by year (may differ from Fsum bc of dome-shaped sel
// sdreport_vector fullF_sd(styr,endyr);
matrix Z(styr,endyr,1,nages);

init_bounded_number log_avg_F_cl(-10,0,0,1);
init_bounded_dev_vector log_F_dev_cl(styr_cl_L,endyr_cl_L,-10.0,10.0,2);
matrix F_CL(styr,endyr,1,nages);
vector F_CL_out(styr,endyr); //used for intermediate calculations in fcn get_mortality
number log_F_dev_init_cl;
number log_F_dev_end_cl;

init_bounded_number log_avg_F_ch(-10,0,0,1);
init_bounded_dev_vector log_F_dev_ch(styr_ch_L,endyr_ch_L,-10.0,10.0,2);
matrix F_CH(styr,endyr,1,nages);
vector F_CH_out(styr,endyr); //used for intermediate calculations in fcn get_mortality
number log_F_dev_init_ch;
number log_F_dev_end_ch;

init_bounded_number log_avg_F_ra(-15.0,0,0,1);
init_bounded_dev_vector log_F_dev_ra(styr_ra_L,endyr_ra_L,-10.0,10.0,2);
matrix F_RA(styr,endyr,1,nages);
vector F_RA_out(styr,endyr); //used for intermediate calculations in fcn get_mortality
number log_F_dev_init_ra;
number log_F_dev_end_ra;

init_bounded_number F_init(0.01,0.9,-4);
//number F_init_ratio; //scales initial F, which is read in as a fixed value
vector sel_initial(1,nages); //initial selectivity (a combination of for-hire and commercial selectivities)

//--Per-recruit stuff--
vector N_age_spr(1,nages);         //numbers at age for SPR calculations: beginning of year
vector N_age_spr_mdyr(1,nages);    //numbers at age for SPR calculations: midyear
vector L_age_spr(1,nages);          //catch at age for SPR calculations
vector Z_age_spr(1,nages);          //total mortality at age for SPR calculations
vector spr_static(styr,endyr);     //vector of static SPR values by year
vector F_L_age_spr(1,nages);        //fishing mortality of landings (not discards) at age for SPR calculations
vector F_spr(1,n_iter_spr);         //values of full F to be used in per-recruit calculations
vector spr_spr(1,n_iter_spr);       //reproductive capacity-per-recruit values corresponding to F values in F_spr
vector L_spr(1,n_iter_spr);         //landings(lb)-per-recruit (ypr) values corresponding to F values in F_spr

vector N_spr(1,nages);             //Used to compute spr at F=0: at time of peak spawning
vector N_bpr_F0(1,nages);          //Used to compute bpr at F=0: at start of year
vector N_spr_initial(1,nages);     //Initial spawners per recruit at age given initial F
vector N_initial_eq(1,nages);       //Initial equilibrium abundance at age
vector F_initial(1,nages);          //Initial F at age
vector Z_initial(1,nages);          //Initial Z at age
number spr_initial;                //Initial spawners per recruit
number spr_F0;                    //Spawning biomass per recruit at F=0
number bpr_F0;                    //Biomass per recruit at F=0

number iter_inc_spr;               //increments used to compute msy, equals max_F_spr_msy/(n_iter_spr-1)

//-----Objective function components-----
number v_L;
number v_lc_cl;
number v_lc_ch;
number v_lc_ra;
//number v_lc_mm;
number v_ac_cl;
number v_ac_ch;
number v_ac_mm;
number v_l_mm;

```

```

number w_I_cL;
number w_rec;
number w_rec_early;
number w_rec_end;
number w_fullf;
number w_Ftune;
// number w_cvlen_dev;
// number w_cvlen_diff;

number f_cL_cpue;
number f_mm_cpue;

number f_cL_L;
number f_CH_L;
number f_RA_L;

number f_cL_lenc;
number f_CH_lenc;
number f_RA_lenc;
//number f_mm_lenc;

number f_cL_agec;
number f_CH_agec;
number f_mm_agec;

number f_cL_RW_cpue; //random walk component of indices

//Penalties and constraints. Not all are used.
number f_rec_dev; //weight on recruitment deviations to fit S-R curve
number f_rec_dev_early; //extra weight on deviations in first recruitment stanza
number f_rec_dev_end; //extra weight on deviations in first recruitment stanza
number f_rec_historic_dev; //extra weight on deviations in first recruitment stanza
number f_Ftune; //penalty for tuning F in Ftune yr. Not applied in final optimization phase.
number f_fullf_constraint; //penalty for Fapex>X
// number f_cvlen_dev_constraint; //deviation penalty on cv's of length at age
// number f_cvlen_diff_constraint; //first diff penalty on cv's of length at age
number f_priors; //prior information on parameters

//init_number xdum;
objective_function_value fval;
number fval_data;

//--Dummy variables ----
number denom; //denominator used in some calculations
number numer; //numerator used in some calculations

//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
INITIALIZATION_SECTION

//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
GLOBALS_SECTION
#include "admodel.h" // Include AD class definitions
#include "admb2r.cpp" // Include S-compatible output functions (needs preceding)

//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
RUNTIME_SECTION
maximum_function_evaluations 1000, 2000, 3000, 10000;
convergence_criteria 1e-2, 1e-2, 1e-3, 1e-4;

//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
//##--><>--><>--><>--><>--><>--><>--><>--><>--><>--><>-->
PRELIMINARY_CALCS_SECTION

// Set values of fixed parameters or set initial guess of estimated parameters
Linf=set_Linf;
Kset_K;
t0=set_t0;
Linf_f=set_Linf_f;
K_f=set_K_f;
t0_f=set_t0_f;
len_cv_val=set_len_cv;

M=set_M;
M_constant=set_M_constant;
// for (iage=1;iage<=max_obs_age;iage++){Mscale_ages(iage)=iage;}

steep=set_stEEP;
R_autocorr=set_R_autocorr;
rec_sigma=set_rec_sigma;

log_q_mm=set_logq_mm;
log_q_cl=set_logq_cl;
q_rate=set_q_rate;
q_rate_fcn_CL=1.0;
q_DD_beta=set_q_DD_beta;
q_DD_fcn=1.0;
q_RW_log_dev_CL.initialize();

if (set_q.rate_phase<0 & q_rate!=0.0)
{
    for (iyear=styr_cL_cpue; iyear<=endyr_cL_cpue; iyear++)
    {
        if (iyear>styr_cL_cpue & iyear <=2003)
            //q_rate_fcn_CL(iyear)=(1.+q_rate)*q_rate_fcn_CL(iyear-1); //compound
            q_rate_fcn_CL(iyear)=(1.+(iyear-styr_cL_cpue)*q_rate)*q_rate_fcn_CL(styr_cL_cpue); //linear
        }
        if (iyear>2003) {q_rate_fcn_CL(iyear)=q_rate_fcn_CL(iyear-1);}
    }
} //end q_rate conditional

w_L=set_w_L;
w_lc_cL=set_w_lc_cL;

```

```

w_lc_CH=set_w_lc_CH;
w_lc_rA=set_w_lc_rA;
//w_lc_mm=set_w_lc_mm;
w_ac_CL=set_w_ac_CL;
w_ac_CH=set_w_ac_CH;
w_ac_mm=set_w_ac_mm;
w_I_mm=set_w_I_mm;
w_I_CL=set_w_I_CL;
w_rec=set_w_rec;
w_fullF=set_w_fullF;
w_rec_early=set_w_rec_early;
w_rec_end=set_w_rec_end;
w_Ftune=set_w_Ftune;
// w_cvlen_dev=set_w_cvlen_dev;
// w_cvlen_diff=set_w_cvlen_diff;

log_avg_F_CL=set_log_avg_F_CL;
log_avg_F_CH=set_log_avg_F_CH;
log_avg_F_rA=set_log_avg_F_rA;
F_init=set_F_init;

log_RO=set_log_RO;

selpar_L50_CL=set_selpar_L50_CL;
selpar_slope_CL=set_selpar_slope_CL;
//selpar_L502_CL=set_selpar_L502_CL;
//selpar_slope2_CL=set_selpar_slope2_CL;
//selpar_min_CL=set_selpar_min_CL;
//selpar_afull_CL=set_selpar_afull_CL;
//selpar_peak_CL=set_selpar_peak_CL;
//selpar_top_CL=set_selpar_top_CL;
//selpar_ascwid_CL=set_selpar_ascwid_CL;
//selpar_decwid_CL=set_selpar_decwid_CL;
//selpar_init_CL=set_selpar_init_CL;
//selpar_final_CL=set_selpar_final_CL;
//selpar_L50_CL2=set_selpar_L50_CL2;
//selpar_slope_CL2=set_selpar_slope_CL2;

selpar_L50_CH=set_selpar_L50_CH;
selpar_slope_CH=set_selpar_slope_CH;
//selpar_L502_CH=set_selpar_L502_CH;
//selpar_slope2_CH=set_selpar_slope2_CH;
//selpar_min_CH=set_selpar_min_CH;
//selpar_afull_CH=set_selpar_afull_CH;
//selpar_peak_CH=set_selpar_peak_CH;
//selpar_top_CH=set_selpar_top_CH;
//selpar_ascwid_CH=set_selpar_ascwid_CH;
//selpar_decwid_CH=set_selpar_decwid_CH;
//selpar_init_CH=set_selpar_init_CH;
//selpar_final_CH=set_selpar_final_CH;

selpar_L50_rA=set_selpar_L50_rA;
selpar_slope_rA=set_selpar_slope_rA;
//selpar_L502_rA=set_selpar_L502_rA;
//selpar_slope2_rA=set_selpar_slope2_rA;
//selpar_min_rA=set_selpar_min_rA;
//selpar_afull_rA=set_selpar_afull_rA;
//selpar_peak_rA=set_selpar_peak_rA;
//selpar_top_rA=set_selpar_top_rA;
//selpar_ascwid_rA=set_selpar_ascwid_rA;
//selpar_decwid_rA=set_selpar_decwid_rA;
//selpar_init_rA=set_selpar_init_rA;
//selpar_final_rA=set_selpar_final_rA;

selpar_L50_mm=set_selpar_L50_mm;
selpar_slope_mm=set_selpar_slope_mm;
//selpar_L502_mm=set_selpar_L502_mm;
//selpar_slope2_mm=set_selpar_slope2_mm;
//selpar_min_mm=set_selpar_min_mm;
//selpar_afull_mm=set_selpar_afull_mm;
//selpar_peak_mm=set_selpar_peak_mm;
//selpar_top_mm=set_selpar_top_mm;
//selpar_ascwid_mm=set_selpar_ascwid_mm;
//selpar_decwid_mm=set_selpar_decwid_mm;
//selpar_init_mm=set_selpar_init_mm;
//selpar_final_mm=set_selpar_final_mm;

sqrt2pi=sqrt(2.*3.14159265);
g2mt=0.000001;           //conversion of grams to metric tons
g2kg=0.001;               //conversion of grams to kg
mt2klb=2.20462;          //conversion of metric tons to 1000 lb
mt2lb=mt2klb*1000.0;     //conversion of metric tons to lb
g2klb=g2mt*mt2klb;       //conversion of grams to 1000 lb
dzero=0.00001;
huge_number=1.0e+10;

SSB_msy_out=0.0;

iter_inc_msy=max_F_spr_msy/(n_iter_msy-1);
iter_inc_spr=max_F_spr_msy/(n_iter_spr-1);

maturity_f=maturity_f_obs;
prop_f=prop_f_obs;

lenbins_all(1,nlenbins)=lenbins(1,nlenbins);
for (iyear=1;iyear<=nlenbins_plus; iyear++) {lenbins_all(nlenbins+iyear)=lenbins_plus(iyear);}

//Fill in sample sizes of comps, possibly sampled in nonconsec yrs
//Used primarily for output in R object

nsamp_CL_lenc_allyr=missing; // "missing" defined in admbr2.cpp
nsamp_CH_lenc_allyr=missing;
nsamp_R_A_lenc_allyr=missing;
//nsamp_MM_lenc_allyr=missing;

```



```

get_weight_at_age_landings();
//cout << "got weight at age of landings" << endl;
get_spr_F0();
//cout << "got F0 spr" << endl;
get_selectivity();
//cout << "got selectivity" << endl;
get_mortality();
//cout << "got mortalities" << endl;
get_bias_corr();
//cout << "got recruitment bias correction" << endl;
get_numbers_at_age();
//cout << "got numbers at age" << endl;
get_landings_numbers();
//cout << "got catch at age" << endl;
get_landings_wgt();
//cout << "got landings" << endl;
get_catchability_fcns();
//cout << "got catchability_fcns" << endl;
get_indices();
//cout << "got indices" << endl;
get_length_comps();
//cout << "got length comps" << endl;
get_age_comps();
//cout << "got age comps" << endl;
evaluate_objective_function();
//cout << "objective function calculations complete" << endl;

FUNCTION get_length_weight_at_age
//compute mean length (mm) and weight (whole) at age
meanlen_TL=Linf*(1.0-mfexp(-K*(agebins-t0+0.5))); //total length in mm
wgt_mt=wgtpar_a*pow(meanlen_TL,wgtpar_b); //wgt in mt
wgt_g=wgt_mt/g2mt; //wgt in grams
wgt_kg=2kg*wgt_g; //wgt in kilograms
wgt_klb=wgt_mt/g2lb*wgt_mt; //1000 lb of whole wgt
wgt_lb=wgt_mt*2lb*wgt_mt; //1000 lb of whole wgt
meanlen_TL_f=Linf_f*(1.0-mfexp(-K_f*(agebins-t0_f+0.5))); //total length in mm
wgt_mt_f=wgtpar_a*pow(meanlen_TL_f,wgtpar_b); //wgt in mt
wgt_g_f=wgt_mt_f/g2mt; //wgt in grams
wgt_kg_f=2kg*wgt_g_f; //wgt in kilograms
wgt_klb_f=wgt_mt_f*2lb*wgt_mt_f; //1000 lb of whole wgt
wgt_lb_f=wgt_mt_f*2lb*wgt_mt_f; //1000 lb of whole wgt
//gonad_wgt_mt=g2mt*(gwtpar_a+gwtpar_b*wgt_g_f); //gonad wgt in mt
gonad_wgt_mt=g2mt*mfexp((gwtpar_a+gwtpar_b)*log(wgt_g_f)); //gonad wgt in mt
for (iage=1;iage<=nages;iage++)
{
    if(gonad_wgt_mt(iage)<0){gonad_wgt_mt(iage)=0;}
}

FUNCTION get_reprod
//reprod is product of stuff going into reproductive capacity calcs
reprod=elem_prod(elem_prod(prop_f,maturity_f),gonad_wgt_mt);
reprod2=elem_prod(elem_prod(prop_f,maturity_f),wgt_mt_f);

FUNCTION get_length_at_age_dist
//compute matrix of length at age, based on the normal distribution

for (iage=1;iage<=nages;iage++)
{
    //len_cv(iage)=mfexp(log_len_cv+log_len_cv_dev(iage));
    len_cv(iage)=len_cv_val;
    len_sd(iage)=meanlen_TL(iage)*len_cv(iage);

    //len_cv(iage)=len_cv_max-(len_cv_max-len_sd)/(1.0+mfexp(-len_cv_slope*(iage-len_cv_a50)));
    for (ilen=1;ilen<=nlenbins_all;ilen++)
    { lenprob_all(iage,ilen)=(mfexp(-(square(lenbins_all(ilen))-meanlen_TL(iage))/
    (2.*square(len_sd(iage)))))/(sqrt2pi*len_sd(iage)));
    }

    lenprob_all(iage)/=sum(lenprob_all(iage)); //standardize to approximate integration and to account for truncated normal (i.e., no sizes<smallest)

    for (ilen=1;ilen<=nlenbins;ilen++) {lenprob(iage,ilen)=lenprob_all(iage,ilen);}
    for (ilen=nlenbins+1;ilen<=nlenbins_all;ilen++) {lenprob(iage)(nlenbins)=lenprob(iage)(nlenbins)+lenprob_all(iage)(ilen);
    } //plus group
}
//fishery specific length probs, assumed normal prior to size limits

lenprob_cl=lenprob;
lenprob_ch=lenprob;
lenprob_r=lenprob;
//lenprob_mm=lenprob;

lenprob_cl_all=lenprob_all;
lenprob_ch_all=lenprob_all;
lenprob_r_all=lenprob_all;
//lenprob_mm_all=lenprob_all;

FUNCTION get_weight_at_age_landings
for (iyear=styr; iyear<=endyr; iyear++)
{
    len_CL_mm(iyear)=meanlen_TL;
    gutwt_CL_klb(iyear)=wgt_klb/gut2whole;
    len_CH_mm(iyear)=meanlen_TL;
    gutwt_CH_klb(iyear)=wgt_klb/gut2whole;
    len_RA_mm(iyear)=meanlen_TL;
    wgt_RA_klb(iyear)=wgt_klb;
    len_MM_mm(iyear)=meanlen_TL;
    wgt_MM_klb(iyear)=wgt_klb;
}

FUNCTION get_spr_F0

```

```

//at mdyr, apply half this yr's mortality, half next yr's
N_spr_F0(i)=1.0*exp(-1.0*M(i)*spawn_time_frac); //at peak spawning time
N_bpr_F0(i)=1.0; //at start of year
for (iage=2; iage==nages; iage++)
{
  //N_spr_F0(iage)=N_spr_F0(iage-1)*mfexp(-1.0*(M(iage-1));
  N_spr_F0(iage)=N_spr_F0(iage-1)*mfexp(-1.0*(M(iage-1)*(1.0-spawn_time_frac) + M(iage)*spawn_time_frac));
  N_bpr_F0(iage)=N_bpr_F0(iage-1)*mfexp(-1.0*(M(iage-1)));
}
N_spr_F0(nages)=N_spr_F0(nages)/(1.0-mfexp(-1.0*M(nages))); //plus group (sum of geometric series)
N_bpr_F0(nages)=N_bpr_F0(nages)/(1.0-mfexp(-1.0*M(nages)));

spr_F0=sum(elem_prod(N_spr_F0,reprod));
bpr_F0=sum(elem_prod(N_bpr_F0,wgt_mt));

FUNCTION get_selectivity
for (iyear=styr; iyear<=endyr; iyear++)
{
  //sel_cL(iyear)=logistic_joint(agebins, selpar_L50_cL, selpar_slope_cL, selpar_L502_cL, selpar_slope2_cL, selpar_min_cL, selpar_afull_cL);
  //sel_ch(iyear)=logistic_joint(agebins, selpar_L50_ch, selpar_slope_ch, selpar_L502_ch, selpar_slope2_ch, selpar_min_ch, selpar_afull_ch);
  //sel_rA(iyear)=logistic_joint(agebins, selpar_L50_rA, selpar_slope_rA, selpar_L502_rA, selpar_slope2_rA, selpar_min_rA, selpar_afull_rA);
  //sel_mm(iyear)=logistic_joint(agebins, selpar_L50_mm, selpar_slope_mm, selpar_L502_mm, selpar_slope2_mm, selpar_min_mm, selpar_afull_mm);

  sel_cL(iyear)=logistic(agebins, selpar_L50_cL, selpar_slope_cL);
  //if(iyear>endyr_period){sel_cL(iyear)=logistic(agebins, selpar_L50_cL2, selpar_slope_cL2);}
  sel_ch(iyear)=logistic(agebins, selpar_L50_ch, selpar_slope_ch);
  //sel_rA(iyear)=logistic(agebins, selpar_L50_rA, selpar_slope_rA);
  sel_mm(iyear)=logistic(agebins, selpar_L50_mm, selpar_slope_mm);

  //sel_cL(iyear)=gaussian_double(agebins, selpar_peak_cL, selpar_top_cL, selpar_ascwid_cL, selpar_decwid_cL, selpar_init_cL, selpar_final_cL);
  //sel_ch(iyear)=gaussian_double(agebins, selpar_peak_ch, selpar_top_ch, selpar_ascwid_ch, selpar_decwid_ch, selpar_init_ch, selpar_final_ch);
  //sel_rA(iyear)=gaussian_double(agebins, selpar_peak_rA, selpar_top_rA, selpar_ascwid_rA, selpar_decwid_rA, selpar_init_rA, selpar_final_rA);
  //sel_mm(iyear)=gaussian_double(agebins, selpar_peak_mm, selpar_top_mm, selpar_ascwid_mm, selpar_decwid_mm, selpar_init_mm, selpar_final_mm);
}

sel_initial=sel_cL(styr);
sel_rA=sel_ch;

FUNCTION get_mortality
Fsum.initialize();
Fapex.initialize();
F.initialize();
//initialization F is avg from first 2 yrs of observed landings (3 yr average typically preferable, but not so here)
log_F_dev_init_cL=sum(log_F_dev_cl(styr_cL_L,(styr_cL_L+1))/2.0;
log_F_dev_init_ch=sum(log_F_dev_ch(styr_ch_L,(styr_ch_L+1))/2.0;
log_F_dev_init_rA=sum(log_F_dev_rA(styr_rA_L,(styr_rA_L+1))/2.0;

for (iyear=styr; iyear<=endyr; iyear++)
{
  //-----
  if(iyear>styr_cL_L & iyear<=endyr_cL_L)
  { F_cL_out(iyear)=mfexp(log_avg_F_cL*log_F_dev_cL(iyear)); //}
  // if (iyear<styr_cL_L){F_cL_out(iyear)=mfexp(log_avg_F_cL+log_F_dev_init_cL);}
  F_cL(iyear)=sel_cL(iyear)*F_cL_out(iyear);
  Fsum(iyear)+=F_cL_out(iyear);

}

//-----
if(iyear>styr_ch_L & iyear<=endyr_ch_L)
{ F_ch_out(iyear)=mfexp(log_avg_F_ch*log_F_dev_ch(iyear)); //}
// if (iyear<styr_ch_L){F_ch_out(iyear)=0.0;}
F_ch(iyear)=sel_ch(iyear)*F_ch_out(iyear);
Fsum(iyear)+=F_ch_out(iyear);

}

//-----
if(iyear>styr_rA_L & iyear<=endyr_rA_L)
{ F_rA_out(iyear)=mfexp(log_avg_F_rA*log_F_dev_rA(iyear)); //}
// if (iyear<styr_rA_L){F_rA_out(iyear)=mfexp(log_avg_F_rA+log_F_init_rA);}
F_rA(iyear)=sel_rA(iyear)*F_rA_out(iyear);
Fsum(iyear)+=F_rA_out(iyear);

}

//Total F at age
F(iyear)=F_cL(iyear); //first in additive series (NO +=)
F(iyear)+=F_ch(iyear);
F(iyear)+=F_rA(iyear);

Fapex(iyear)=max(F(iyear));
Z(iyear)=M+(iyear);
} //end iyear

FUNCTION get_bias_corr
//may exclude last BiasCor_exclude_yrs yrs bc constrained or lack info to estimate
var_rec_dev=norm2(log_rec_dev(styr_rec_dev,(endyr-BiasCor_exclude_yrs))- //sum(log_rec_dev(styr_rec_dev,(endyr-BiasCor_exclude_yrs)))
// (nyears_rec-BiasCor_exclude_yrs))/(nyears_rec-BiasCor_exclude_yrs-1.0);
var_rec_dev=norm2(log_rec_dev(styr_rec_dev,endyr_rec_dev)- //sum(log_rec_dev(styr_rec_dev,endyr_rec_dev))
// (nyears_rec-(endyr_rec_dev-styr_rec_dev)))/(nyears_rec-(endyr_rec_dev-styr_rec_dev)-1.0);

//if (set_BiasCor <= 0.0) {BiasCor=exp(var_rec_dev/2.0);} //bias correction
rec_sigma_sq=square(rec_sigma);
if (set_BiasCor < 0.0) {BiasCor=exp(rec_sigma_sq/2.0);} //bias correction
else {BiasCor=set_BiasCor; }

FUNCTION get_numbers_at_age
//Initialization
SO=spr_F0*R0;
R_virgin=(R0/((5.0*steep-1.0)*spr_F0)* //BiasCor*4.0*steep*spr_F0*(1.0-steep));

```

```

B0=bpr_F0*R_virgin;
B0_q_DD=R_virgin*sum(elem_prod(N_bpr_F0(set_q_DD_stage,nages),wgt_mt(set_q_DD_stage,nages)));

F_initial=sel_initial*F_init;
// F_initial=F_init ratio*set F_init;

Z_initial=M*F_initial;

//Initial equilibrium age structure
N_spr_initial(i)=1.0*mfexp(-1.0*Z_initial(i)*spawn_time_frac); //at peak spawning time;
for (iage=2; iage<=nages; iage++)
{
  N_spr_initial(iage)=N_spr_initial(iage-1)*
    mfexp(-1.0*(Z_initial(iage-1)*(1.0-spawn_time_frac) + Z_initial(iage)*spawn_time_frac));
}
N_spr_initial(nages)=N_spr_initial(nages)/(1.0-mfexp(-1.0*Z_initial(nages))); //plus group
//  N_spr_F_init_mdry(i,(nages-1))=elem_prod(N_spr_initial(i,(nages-1)),
//                                         mfexp((-1.*N(nages-1)* F_initial))/2.0);

spr_initial=sum(elem_prod(N_spr_initial,reprod));

if (styr==styr_rec_dev) {R1=(R0/((5.0*steep-1.0)*spr_initial))* //without bias correction (deviation added later)
  (4.0*steep*spr_initial-spr_F0*(1.0-steep));} //with bias correction
else {R1=(R0/((5.0*steep-1.0)*spr_initial))* //BiasCorr4,0*steep*spr_initial-spr_F0*(1.0-steep);} //with bias correction

if(R1<0.0) {R1=1.0;} //Avoid negative popn sizes during search algorithm

//Compute equilibrium age structure for first year
N_initial_eq(i)=R1;
for (iage=2; iage<=nages; iage++)
{
  N_initial_eq(iage)=N_initial_eq(iage-1)*
    mfexp(-1.0*(Z_initial(iage-1)));
}
//plus group calculation
N_initial_eq(nages)=M_initial_eq(nages)/(1.0-mfexp(-1.0*Z_initial(nages))); //plus group

//Add deviations to initial equilibrium N
N(styr)(2,nages)=elem_prod(N_initial_eq(2,nages),mfexp(log_Nage_dev));

if (styr==styr_rec_dev) {N(styr,1)=N_initial_eq(1)*mfexp(log_rec_dev(styr_rec_dev));}
else {N(styr,1)=N_initial_eq(1);}

N_mdry(styr)(1,nages)=elem_prod(N(styr)(1,nages),(mfexp(-1.*Z_initial(1,nages))*0.5)); //mid year
N_spawn(styr)(1,nages)=elem_prod(N(styr)(1,nages),(mfexp(-1.*Z_initial(1,nages))*spawn_time_frac)); //peak spawning time
SSB(styr)=sum(elem_prod(N_spawn(styr),reprod));
MatFemB(styr)=sum(elem_prod(N_spawn(styr),reprod2));
B_q_DD(styr)=sum(elem_prod(N(styr)(set_q_DD_stage,nages),wgt_mt(set_q_DD_stage,nages)));

//Rest of years
for (iyear=styr; iyyear<endyr; iyyear++)
{
  if(iyyear<(styr_rec_dev-1)||iyyear>endyr_rec_dev) //recruitment follows S-R curve exactly
  {
    //add dzero to avoid log(zero)
    N(iyyear+1,1)=BiasCorr4*mfexp(log(((0.8*R0*steep*SSB(iyyear))/(0.2*R0*spr_F0*
      (1.0-steep)*(steep-0.2)+SSB(iyyear)))+dzero)+log_rec_historic_dev(iyyear+1));
    //N(iyyear+1,1)=SR_func(R0, steep, spr_F0, SSB(iyyear))*mfexp(log_rec_historic_dev(iyyear+1));
    //mfexp(log(((0.8*R0*steep*SSB(iyyear))/(0.2*R0*spr_F0*
    //  ((1.0-steep)*(steep-0.2)+SSB(iyyear)))+dzero)+log_rec_historic_dev(iyyear+1));
    N(iyyear+1)(2,nages)+=elem_prod(N(iyyear)(1,nages-1),(mfexp(-1.*Z(iyyear)(1,nages-1))));
    N(iyyear+1,nages)+=N(iyyear,nages)*mfexp(-1.*Z(iyyear,nages)); //plus group
    N_mdry(iyyear+1)(1,nages)=elem_prod(N(iyyear+1)(1,nages),(mfexp(-1.*Z(iyyear+1)(1,nages))*0.5)); //mid year
    N_spawn(iyyear+1)(1,nages)=elem_prod(N(iyyear+1)(1,nages),(mfexp(-1.*Z(iyyear+1)(1,nages))*spawn_time_frac)); //peak spawning time
    SSB(iyyear+1)=sum(elem_prod(N_spawn(iyyear+1),reprod));
    MatFemB(iyyear+1)=sum(elem_prod(N_spawn(iyyear+1),reprod2));
    B_q_DD(iyyear+1)=sum(elem_prod(N(iyyear+1)(set_q_DD_stage,nages),wgt_mt(set_q_DD_stage,nages)));
  }
  else //recruitment follows S-R curve with lognormal deviation
  {
    //add dzero to avoid log(zero)
    N(iyyear+1,1)=SR_func(R0, steep, spr_F0, SSB(iyyear))*mfexp(log_rec_dev(iyyear+1));
    //mfexp(log(((0.8*R0*steep*SSB(iyyear))/(0.2*R0*spr_F0*
    //  ((1.0-steep)*(steep-0.2)+SSB(iyyear)))+dzero)+log_rec_dev(iyyear+1));
    N(iyyear+1)(2,nages)+=elem_prod(N(iyyear)(1,nages-1),(mfexp(-1.*Z(iyyear)(1,nages-1))));
    N(iyyear+1,nages)+=N(iyyear,nages)*mfexp(-1.*Z(iyyear,nages)); //plus group
    N_mdry(iyyear+1)(1,nages)=elem_prod(N(iyyear+1)(1,nages),(mfexp(-1.*Z(iyyear+1)(1,nages))*0.5)); //mid year
    N_spawn(iyyear+1)(1,nages)=elem_prod(N(iyyear+1)(1,nages),(mfexp(-1.*Z(iyyear+1)(1,nages))*spawn_time_frac)); //peak spawning time
    SSB(iyyear+1)=sum(elem_prod(N_spawn(iyyear+1),reprod));
    MatFemB(iyyear+1)=sum(elem_prod(N_spawn(iyyear+1),reprod2));
    B_q_DD(iyyear+1)=sum(elem_prod(N(iyyear+1)(set_q_DD_stage,nages),wgt_mt(set_q_DD_stage,nages)));
  }
}

//last year (projection) has no recruitment variability
N(endyr+1,1)=SR_func(R0, steep, spr_F0, SSB(endyr));

//mfexp(log(((0.8*R0*steep*SSB(endyr))/(0.2*R0*spr_F0*
//  ((1.0-steep)+(steep-0.2)*SSB(endyr)))+dzero));
N(endyr+1)(2,nages)+=elem_prod(N(endyr)(1,nages-1),(mfexp(-1.*Z(endyr)(1,nages-1))));
N(endyr+1,nages)+=N(endyr,nages)*mfexp(-1.*Z(endyr,nages)); //plus group
//SSB(endyr+1)=sum(elem_prod(N(endyr+1),reprod));
}

```

```

//Time series of interest
rec=column(N,1);
SdSO=SSB/SO;

FUNCTION get_landings_numbers //Baranov catch eqn
for (iyear=sty; iyear<=endyr; iyear++)
{
  for (iage=1; iage<=nages; iage++)
  {
    L_cl_num(iyear,iage)=N(iyear,iage)*F_CL(iyear,iage)*
      (1.-mfexp(-1.*Z(iyear,iage)))/Z(iyear,iage);
    L_ch_num(iyear,iage)=N(iyear,iage)*F_CH(iyear,iage)*
      (1.-mfexp(-1.*Z(iyear,iage)))/Z(iyear,iage);
    L_ra_num(iyear,iage)=N(iyear,iage)*F_RA(iyear,iage)*
      (1.-mfexp(-1.*Z(iyear,iage)))/Z(iyear,iage);
  }

  pred_CL_L_knum(iyear)=sum(L_cl_num(iyear))/1000.0;
  pred_CH_L_knum(iyear)=sum(L_ch_num(iyear))/1000.0;
  pred_RA_L_knum(iyear)=sum(L_ra_num(iyear))/1000.0;
}

FUNCTION get_landings_wgt

//----Predicted landings-----
for (iyear=sty; iyear<=endyr; iyear++)
{
  L_cl_klb(iyear)=elem_prod(L_cl_num(iyear),gutwgt_CL_klb(iyear)); //in 1000 lb
  L_ch_klb(iyear)=elem_prod(L_ch_num(iyear),gutwgt_CH_klb(iyear)); //in 1000 lb
  L_ra_klb(iyear)=elem_prod(L_ra_num(iyear),gutwgt_RA_klb(iyear)); //in 1000 lb

  pred_CL_L_klb(iyear)=sum(L_cl_klb(iyear));
  pred_CH_L_klb(iyear)=sum(L_ch_klb(iyear));
  pred_RA_L_klb(iyear)=sum(L_ra_klb(iyear));
}

FUNCTION get_catchability_fcn
//Get rate increase if estimated, otherwise fixed above
if (set_q_rate_phase>0.0)
{
  for (iyear=sty,cl_cpue; iyear<=endyr,cl_cpue; iyear++)
  {
    if (iyear>2003)
      {q_rate_fcn(CL(iyear))=(1.0+q_rate)*q_rate_fcn(CL(iyear-1)); //compound
       q_rate_fcn(CL(iyear))=(1.0+(iyear-sty,cl_cpue)*q_rate)*q_rate_fcn(CL(sty,cl_cpue)); //linear}
    if (iyear>2003) {q_rate_fcn(CL(iyear))=q_rate_fcn(CL(iyear-1));}
  }
} //end q_rate conditional

//Get density dependence scalar (=1.0 if density independent model is used)
if (q_DD_beta>0.0)
{
  B_q_DD+=dzero;
  for (iyear=sty;iyear<=endyr;iyear++)
  {
    q_DD_fcn(iyear)=pow(B0_q_DD,q_DD_beta)*pow(B_q_DD(iyear),-q_DD_beta);
    //q_DD_fcn(iyear)=1.0+4.0/(1.0+mfexp(0.75*(B_q_DD(iyear)-0.1*B0_q_DD)));
  }
}

FUNCTION get_indices
//---Predicted CPUEs-----

//Commercial longline cpue
q_CL(sty,cl_cpue)=mfexp(log_q_CL);
for (iyear=sty,cl_cpue; iyear<=endyr,cl_cpue; iyear++)
{
  //index in weight units. original index in lb and re-scaled. predicted in klb, but difference is absorbed by q
  N_CL(iyear)=elem_prod(elem_prod(N_mdry(iyear),sel_CL(iyear)),gutwgt_CL_klb(iyear));
  pred_CL_cpue(iyear)=q_CL(iyear)*q_rate_fcn(CL(iyear))*q_DD_fcn(iyear)*sum(N_CL(iyear));
  if (iyear>endyr,cl_cpue){q_CL(iyear+1)=q_CL(iyear)*mfexp(q_RW_log_dev_CL(iyear));}
}

q_MM=mfexp(log_q_MM);
for (iyear=1; iyear<=nyr_MM_cpue; iyear++)
{
  if(iyear<nyr_MM_cpue)
  {
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)-2),sel_MM(yrs_MM_cpue(iyear)-2)),wgt_MM_klb(yrs_MM_cpue(iyear)-2));
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)-1),sel_MM(yrs_MM_cpue(iyear)-1)),wgt_MM_klb(yrs_MM_cpue(iyear)-1));
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)),sel_MM(yrs_MM_cpue(iyear))),wgt_MM_klb(yrs_MM_cpue(iyear)));
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)+1),sel_MM(yrs_MM_cpue(iyear)+1)),wgt_MM_klb(yrs_MM_cpue(iyear)+1));
    pred_MM_cpue(iyear)=q_MM*sum(N_MM(iyear))/4;
  }
  if(iyear==nyr_MM_cpue)
  {
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)-1),sel_MM(yrs_MM_cpue(iyear)-1)),wgt_MM_klb(yrs_MM_cpue(iyear)-1));
    N_MM(iyear)=elem_prod(elem_prod(N_mdry(yrs_MM_cpue(iyear)),sel_MM(yrs_MM_cpue(iyear))),wgt_MM_klb(yrs_MM_cpue(iyear)));
    pred_MM_cpue(iyear)=q_MM*sum(N_MM(iyear))/2;
  }
}

for (iyear=1; iyear<=nyr_MM_cpue; iyear++)
{
  pred_MM_cpue_allyr(yrs_MM_cpue(iyear))=pred_MM_cpue(iyear); // for graphing purposes only
}

FUNCTION get_length_comps
//Commercial longline
for (iyear=1;iyear<=nyr_CL_lenc;iyear++)
{
  pred_CL_lenc(iyear)=(L_cl_num(yrs_CL_lenc(iyear))*lenprob_CL)
}

```

```

    /sum(L_cL_num(yrs_cL_lenc(iyear)));
}

//Commercial handleline
for (iyear=1;iyear<=nyr_ch_lenc;iyear++)
{
    pred_ch_lenc(iyear)=(L_ch_num(yrs_ch_lenc(iyear))*lenprob_ch)
        /sum(L_ch_num(yrs_ch_lenc(iyear)));
}

//All recreational
for (iyear=1;iyear<=nyr_rA_lenc;iyear++)
{
    pred_rA_lenc(iyear)=(L_rA_num(yrs_rA_lenc(iyear))*lenprob_rA)
        /sum(L_rA_num(yrs_rA_lenc(iyear)));
}

//MARMAP
// for (iyear=1;iyear<=nyr_mm_lenc;iyear++)
//{
// if(iyear<nyr_mm_lenc)
//{
//     pred_mm_lenc(iyear)=elem_prod(N(yrs_mm_lenc(iyear)-2),sel_mm(yrs_mm_lenc(iyear)-2))*lenprob_mm;
//     pred_mm_lenc(iyear)*=elem_prod(N(yrs_mm_lenc(iyear)-1),sel_mm(yrs_mm_lenc(iyear)-1))*lenprob_mm;
//     pred_mm_lenc(iyear)+=elem_prod(N(yrs_mm_lenc(iyear)),sel_mm(yrs_mm_lenc(iyear)))*lenprob_mm;
//     pred_mm_lenc(iyear)+=elem_prod(N(yrs_mm_lenc(iyear)+1),sel_mm(yrs_mm_lenc(iyear)+1))*lenprob_mm;
//     pred_mm_lenc(iyear)=pred_mm_lenc(iyear)/sum(pred_mm_lenc(iyear));
//}
// if(iyear==nyr_mm_lenc)
//{
//     pred_mm_lenc(iyear)+=elem_prod(N(yrs_mm_lenc(iyear)-1),sel_mm(yrs_mm_lenc(iyear)-1))*lenprob_mm;
//     pred_mm_lenc(iyear)+=elem_prod(N(yrs_mm_lenc(iyear)),sel_mm(yrs_mm_lenc(iyear)))*lenprob_mm;
//     pred_mm_lenc(iyear)=pred_mm_lenc(iyear)/sum(pred_mm_lenc(iyear));
//}
//}

FUNCTION get_age_comps

//Commercial longline
for (iyear=1;iyear<=nyr_cl_agec;iyear++)
{
    ErrorFree_cl_agec(iyear)=L_cL_num(yrs_cL_agec(iyear))/sum(L_cL_num(yrs_cL_agec(iyear)));
    pred_cl_agec(iyear)=age_error*ErrorFree_cl_agec(iyear);
}

//Commercial handleline
for (iyear=1;iyear<=nyr_ch_agec;iyear++)
{
    ErrorFree_ch_agec(iyear)=L_ch_num(yrs_ch_agec(iyear))/sum(L_ch_num(yrs_ch_agec(iyear)));
    pred_ch_agec(iyear)=age_error*ErrorFree_ch_agec(iyear);
}

//MARMAP longline
for (iyear=1;iyear<=nyr_mm_agec;iyear++)
{
    if(iyear<nyr_mm_agec)
    {
        ErrorFree_mm_agec(iyear)=elem_prod(N(yrs_mm_agec(iyear)-2),sel_mm(yrs_mm_agec(iyear)-2));
        ErrorFree_mm_agec(iyear)*=elem_prod(N(yrs_mm_agec(iyear)-1),sel_mm(yrs_mm_agec(iyear)-1));
        ErrorFree_mm_agec(iyear)=elem_prod(N(yrs_mm_agec(iyear)),sel_mm(yrs_mm_agec(iyear)));
        ErrorFree_mm_agec(iyear)+=elem_prod(N(yrs_mm_agec(iyear)+1),sel_mm(yrs_mm_agec(iyear)+1));
        pred_mm_agec(iyear)=age_error*(ErrorFree_mm_agec(iyear)/sum(ErrorFree_mm_agec(iyear)));
    }
    if(iyear==nyr_mm_agec)
    {
        ErrorFree_mm_agec(iyear)=elem_prod(N(yrs_mm_agec(iyear)-1),sel_mm(yrs_mm_agec(iyear)-1));
        ErrorFree_mm_agec(iyear)=elem_prod(N(yrs_mm_agec(iyear)),sel_mm(yrs_mm_agec(iyear)));
        pred_mm_agec(iyear)=age_error*(ErrorFree_mm_agec(iyear)/sum(ErrorFree_mm_agec(iyear)));
    }
}

//-----
FUNCTION get_weighted_current
F_temp_sum=0.0;
F_temp_sum+=mfexp((selpar_n_yrs_wgted*log_avg_F_cL+
    sum(log_F_dev_cl((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted);
F_temp_sum+=mfexp((selpar_n_yrs_wgted*log_avg_F_ch+
    sum(log_F_dev_ch((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted);
F_temp_sum+=mfexp((selpar_n_yrs_wgted*log_avg_F_rA+
    sum(log_F_dev_rA((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted);

F_cL_prop=mfexp((selpar_n_yrs_wgted*log_avg_F_cL+
    sum(log_F_dev_cl((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted)/F_temp_sum;
F_ch_prop=mfexp((selpar_n_yrs_wgted*log_avg_F_ch+
    sum(log_F_dev_ch((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted)/F_temp_sum;
F_rA_prop=mfexp((selpar_n_yrs_wgted*log_avg_F_rA+
    sum(log_F_dev_rA((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted)/F_temp_sum;

log_F_dev_end_cL=sum(log_F_dev_cl((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted;
log_F_dev_end_ch=sum(log_F_dev_ch((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted;
log_F_dev_end_rA=sum(log_F_dev_rA((endyr-selpar_n_yrs_wgted+1),endyr))/selpar_n_yrs_wgted;

F_end_L*sel_cL(endyr)*mfexp(log_avg_F_cL+log_F_dev_end_cL)+
    sel_ch(endyr)*mfexp(log_avg_F_ch+log_F_dev_end_ch)+
    sel_rA(endyr)*mfexp(log_avg_F_rA+log_F_dev_end_rA);

F_end=F_end_L;
F_end_apex=max(F_end);

sel_wgted_tot=F_end/F_end_apex;
sel_wgted_L=elem_prod(sel_wgted_tot, elem_div(F_end_L,F_end));

```

```

wgt_wgted_L_denom=F_cl_prop+F_ch_prop+F_rA_prop;
wgt_wgted_L_klb=F_cl_prop/wgt_wgted_L_denom*gutwgt_cl_klb(endyr) +
F_ch_prop/wgt_wgted_L_denom*gutwgt_ch_klb(endyr) +
F_rA_prop/wgt_wgted_L_denom*wgt_rA_klb(endyr);

FUNCTION get_msy
//compute values as functions of F
for(ff=1; ff<=n_iter_msy; ff++)
{
  //uses fishery-weighted F's
  Z_age_msy=0.0;
  F_L_age_msy=0.0;

  F_L_age_msy=F_msy(ff)*sel_wgted_L;
  Z_age_msy+=F_L_age_msy;

  N_age_msy(1)=1.0;
  for (iage=2; iage<=nages; iage++)
  {
    N_age_msy(iage)=N_age_msy(iage-1)*mfexp(-1.*Z_age_msy(iage-1));
  }
  N_age_msy(nages)=N_age_msy(nages)/(1.0-mfexp(-1.*Z_age_msy(nages)));
  N_age_msy_mdyr(1,(nages-1))=elem_prod(N_age_msy(1,(nages-1)),
  mfexp((-1.*Z_age_msy(1,(nages-1)))*spawn_time_frac));
  N_age_msy_mdyr(nages)=(N_age_msy_mdyr(nages-1)*
  (mfexp(-1.*Z_age_msy(nages-1)*(1.0-spawn_time_frac) +
  Z_age_msy(nages)*spawn_time_frac))) /
  (1.0-mfexp(-1.*Z_age_msy(nages)));
  spr_msy(ff)=sum(elem_prod(N_age_msy_mdyr,reprod));

  //Compute equilibrium values of R (including bias correction), SSB and Yield at each F
  R_eq(ff)=(R0/((5.0*steep-1.0)*spr_msy(ff)))*
  (BiasCorv4_0*steep*spr_msy(ff)-spr_F0*(1.0-steep));
  if (R_eq(ff)<dzero) {R_eq(ff)=dzero;}
  N_age_msy=R_eq(ff);
  N_age_msy_mdyr=R_eq(ff);

  for (iage=1; iage<=nages; iage++)
  {
    L_age_msy(iage)=N_age_msy(iage)*(F_L_age_msy(iage)/Z_age_msy(iage))*(
    1.-mfexp(-1.*Z_age_msy(iage)));
  }

  SSB_eq(ff)=sum(elem_prod(N_age_msy_mdyr,reprod));
  B_eq(ff)=sum(elem_prod(N_age_msy,wgt_mt));
  L_eq_klb(ff)=sum(elem_prod(L_age_msy,wgt_wgted_L_klb));
  L_eq_knum(ff)=sum(L_age_msy)/1000.0;
}

msy_klb_out=max(L_eq_klb);

for(ff=1; ff<=n_iter_msy; ff++)
{
  if(L_eq_klb(ff) == msy_klb_out)
  {
    SSB_msy_out=SSB_eq(ff);
    B_msy_out=B_eq(ff);
    R_msy_out=R_eq(ff);
    msy_knum_out=L_eq_knum(ff);
    F_msy_out=F_msy(ff);
    spr_msy_out=spr_msy(ff);
  }
}

//-----
FUNCTION get_miscellaneous_stuff

sigma_rec_dev=sqrt(var_rec_dev); //pow(var_rec_dev,0.5); //sample SD of predicted residuals (may not equal rec_sigma)
len_cv=elem_div(len_sd,meanlen_TL);

//compute total landings- and discards-at-age in 1000 fish and klb
L_total_num_initialize();
L_total_klb_initialize();
L_total_knum_yr_initialize();
L_total_klb_yr_initialize();

for(iyearsty; iyear<=endyr; iyear++)
{
  L_total_klb_yr(iyear)= pred_cl_L_klb(iyear)+pred_ch_L_klb(iyear) +
  pred_ra_L_klb(iyear);
  L_total_knum_yr(iyear)=pred_cl_L_knum(iyear)+pred_ch_L_knum(iyear) +
  pred_ra_L_knum(iyear);

  B(iyear)=elem_prod(N(iyear),wgt_mt);
  totH(iyear)=sum(N(iyear));
  totB(iyear)=sum(B(iyear));
}

L_total_num=(L_rA_num+L_cl_num+L_ch_num); //landings at age in number fish
L_total_klb=L_rA_klb+L_cl_klb+L_ch_klb; //landings at age in klb whole weight

B(endyr+1)=elem_prod(N(endyr+1),wgt_mt);
totH(endyr+1)=sum(N(endyr+1));
totB(endyr+1)=sum(B(endyr+1));

// steep_sd=steep;
// fullF_sd=fsum;

if(F_msy_out>0)
{
  FdF_msy=Fapex/F_msy_out;
}

```

```

FdF_msy_end=FdF_msy(endyr);
FdF_msy_end_mean=pow((FdF_msy(endyr)*FdF_msy(endyr-1)*FdF_msy(endyr-2)),(1.0/3.0));
}
if(SSB_msy_out>0)
{
    SdSSB_msy=SSB/SSB_msy_out;
    SdSSB_msy_end=SdSSB_msy(endyr);
}

//fill in log recruitment deviations for yrs they are nonzero
for(iyear=styr_rec_dev; iyear<=endyr_rec_dev; iyear++)
    {log_rec_dev_output(iyear)=log_rec_dev(iyear);}
//for(iyear=(styr+1); iyear<=(styr_rec_dev+1); iyear++)
//    {log_rec_historic_dev_output(iyear)=log_rec_historic_dev(iyear);}

//fill in log Nage deviations for ages they are nonzero (ages2+)
for(iage=2; iage<=nages; iage++)
{
    log_Nage_dev_output(iage)=log_Nage_dev(iage);
}

//-----
FUNCTION get_per_recruit_stuff

//static per-recruit stuff

for(iyear=styr; iyear<=endyr; iyear++)
{
    N_age_spr(1)=1.0;
    for(iage=2; iage<=nages; iage++)
    {
        N_age_spr(iage)=N_age_spr(iage-1)*mfexp(-1.*Z(iyear, iage-1));
    }
    N_age_spr(nages)=N_age_spr(nages)/(1.0-mfexp(-1.*Z(iyear, nages)));
    N_age_spr_mdyr(1, (nages-1))=elem_prod(N_age_spr(1, (nages-1)),
                                             mfexp(-1.*Z(iyear)(1, (nages-1))*spawn_time_frac));
    N_age_spr_mdyr(nages)=(N_age_spr_mdyr(nages-1)*
                           (mfexp(-1.*Z(iyear)(nages-1)*(1.0-spawn_time_frac) + Z(iyear)(nages)*spawn_time_frac) ))
                           /(1.0-mfexp(-1.*Z(iyear)(nages)));
    spr_static(iyear)=sum(elem_prod(N_age_spr_mdyr, reprod))/spr_F0;
}

//compute SSB/R and YPR as functions of F
for(ff=1; ff<=n_iter_spr; ff++)
{
    //uses fishery-weighted F's, same as in MSY calculations
    Z_age_spr=0.0;
    F_L_Age_spr=0.0;

    F_L_Age_spr=F_spr(ff)*sel_wgted_L;

    Z_age_spr=M+F_L_Age_spr;

    N_age_spr(1)=1.0;
    for (iage=2; iage<=nages; iage++)
    {
        N_age_spr(iage)=N_age_spr(iage-1)*mfexp(-1.*Z_age_spr(iage-1));
    }
    N_age_spr(nages)=N_age_spr(nages)/(1-mfexp(-1.*Z_age_spr(nages)));
    N_age_spr_mdyr(1, (nages-1))=elem_prod(N_age_spr(1, (nages-1)),
                                             mfexp((-1.*Z_age_spr(1, (nages-1)))*spawn_time_frac));
    N_age_spr_mdyr(nages)=(N_age_spr_mdyr(nages-1)*
                           (mfexp(-1.*Z_age_spr(nages-1)*(1.0-spawn_time_frac) + Z_age_spr(nages)*spawn_time_frac) ))
                           /(1.0-mfexp(-1.*Z_age_spr(nages)));

    spr_spr(ff)=sum(elem_prod(N_age_spr_mdyr, reprod));
    L_spr(ff)=0.0;
    for (iage=1; iage<=nages; iage++)
    {
        L_age_spr(iage)=N_age_spr(iage)*(F_L_Age_spr(iage)/Z_age_spr(iage))*(
            (1.-mfexp(-1.*Z_age_spr(iage))));
        L_spr(ff)+=L_age_spr(iage)*wgtr_wgted_L_klb(iage)*1000.0; //in lb
    }
}

FUNCTION get_effective_sample_sizes

neff_CL_lenc_allyr_out=missing;//"missing" defined in admdb2r.cpp
neff_CH_lenc_allyr_out=missing;
neff_RA_lenc_allyr_out=missing;
//neff_MM_lenc_allyr_out=missing;
neff_CL_agec_allyr_out=missing;
neff_CH_agec_allyr_out=missing;
neff_MM_agec_allyr_out=missing;

for (iyear=1; iyear<=nyr_CL_lenc; iyear++)
    {if (nsamp_CL_lenc(iyear)>minSS_CL_lenc)
     {neff_CL_lenc_allyr_out(yrs_CL_lenc(iyear))=multinom_eff_N(pred_CL_lenc(iyear), obs_CL_lenc(iyear));}
     else {neff_CL_lenc_allyr_out(yrs_CL_lenc(iyear))=-99;}}
```

```

//for (iyear=1; iyear<=nyr_mm_lenc; iyear++)
//  {if (nsamp_mm_lenc(iyear)>minSS_mm_lenc)
//    {neff_mm_lenc_allyr_out(yrs_mm_lenc(iyear))=multinom_eff_N(pred_mm_lenc(iyear),obs_mm_lenc(iyear));}
//  else {neff_mm_lenc_allyr_out(yrs_mm_lenc(iyear))=-99;}
//  }

for (iyear=1; iyear<=nyr_cl_agec; iyear++)
{if (nsamp_cl_agec(iyear)>minSS_cl_agec)
  {neff_cl_agec_allyr_out(yrs_cl_agec(iyear))=multinom_eff_N(pred_cl_agec(iyear),obs_cl_agec(iyear));}
  else {neff_cl_agec_allyr_out(yrs_cl_agec(iyear))=-99;}
}

for (iyear=1; iyear<=nyr_ch_agec; iyear++)
{if (nsamp_ch_agec(iyear)>minSS_ch_agec)
  {neff_ch_agec_allyr_out(yrs_ch_agec(iyear))=multinom_eff_N(pred_ch_agec(iyear),obs_ch_agec(iyear));}
  else {neff_ch_agec_allyr_out(yrs_ch_agec(iyear))=-99;}
}

for (iyear=1; iyear<=nyr_mm_agec; iyear++)
{if (nsamp_mm_agec(iyear)>minSS_mm_agec)
  {neff_mm_agec_allyr_out(yrs_mm_agec(iyear))=multinom_eff_N(pred_mm_agec(iyear),obs_mm_agec(iyear));}
  else {neff_mm_agec_allyr_out(yrs_mm_agec(iyear))=-99;}
}

//-----

FUNCTION evaluate_objective_function
fval=0.0;
fval_data=0.0;
//fval=square(xdum-9.0); //used in model development
//---Likelihoods-----
//---Indices-----
f_cl_cpue=0.0;
f_cl_cpue=lk_lognormal(pred_cl_cpue, obs_cl_cpue, cl_cpue_cv, w_I_cl);
fval+=f_cl_cpue;
fval_data+=f_cl_cpue;

f_mm_cpue=0.0;
f_mm_cpue=lk_lognormal(pred_mm_cpue, obs_mm_cpue, mm_cpue_cv, w_I_mm);
fval+=f_mm_cpue;
fval_data+=f_mm_cpue;

//---Lands-----
//f_cl_L in 1000 lb ww
f_cl_L=lk_lognormal(pred_cl_L_klb(styr_cl_L, endyr_cl_L), obs_cl_L(styr_cl_L, endyr_cl_L),
                     cl_L_cv(styr_cl_L, endyr_cl_L), w_L);
fval+=f_cl_L;
fval_data+=f_cl_L;

//f_ch_L in 1000 lb ww
f_ch_L=lk_lognormal(pred_ch_L_klb(styr_ch_L, endyr_ch_L), obs_ch_L(styr_ch_L, endyr_ch_L),
                     ch_L_cv(styr_ch_L, endyr_ch_L), w_L);
fval+=f_ch_L;
fval_data+=f_ch_L;

//f_ra_L in 1000 fish
f_ra_L=lk_lognormal(pred_ra_L_knum(styr_ra_L, endyr_ra_L), obs_ra_L(styr_ra_L, endyr_ra_L),
                     ra_L_cv(styr_ra_L, endyr_ra_L), w_L);
fval+=f_ra_L;
fval_data+=f_ra_L;

//---Length comps-----
//f_cl_lenc
f_cl_lenc=lk_multinomial(nsamp_cl_lenc, pred_cl_lenc, obs_cl_lenc, nyr_cl_lenc, minSS_cl_lenc, w_lc_cl);
fval+=f_cl_lenc;
fval_data+=f_cl_lenc;

//f_ch_lenc
f_ch_lenc=lk_multinomial(nsamp_ch_lenc, pred_ch_lenc, obs_ch_lenc, nyr_ch_lenc, minSS_ch_lenc, w_lc_ch);
fval+=f_ch_lenc;
fval_data+=f_ch_lenc;

//f_ra_lenc
f_ra_lenc=lk_multinomial(nsamp_ra_lenc, pred_ra_lenc, obs_ra_lenc, nyr_ra_lenc, minSS_ra_lenc, w_lc_ra);
fval+=f_ra_lenc;
fval_data+=f_ra_lenc;

//f_mm_lenc
//f_mm_lenc=lk_multinomial(nsamp_mm_lenc, pred_mm_lenc, obs_mm_lenc, nyr_mm_lenc, minSS_mm_lenc, w_lc_mm);
//fval+=f_mm_lenc;
//fval_data+=f_mm_lenc;

//-----Age comps-----
//f_cl_agec
f_cl_agec=lk_multinomial(nsamp_cl_agec, pred_cl_agec, obs_cl_agec, nyr_cl_agec, minSS_cl_agec, w_ac_cl);
fval+=f_cl_agec;
fval_data+=f_cl_agec;

//f_ch_agec
f_ch_agec=lk_multinomial(nsamp_ch_agec, pred_ch_agec, obs_ch_agec, nyr_ch_agec, minSS_ch_agec, w_ac_ch);
fval+=f_ch_agec;
fval_data+=f_ch_agec;

//f_mm_agec
f_mm_agec=lk_multinomial(nsamp_mm_agec, pred_mm_agec, obs_mm_agec, nyr_mm_agec, minSS_mm_agec, w_ac_mm);
fval+=f_mm_agec;
fval_data+=f_mm_agec;

```

```

//----Constraints and penalties-----
f_rec_devo=0.0;
//rec_sigma_sq=square(rec_sigma);
rec_logL_add=nyrs_rec*log(rec_sigma);
f_rec_devs=(square(log_rec_dev(styr_rec_dev) + rec_sigma_sq/2.0)/(2.0*rec_sigma_sq));
for(iyear=(styr_rec_dev+1); iyear<endyr; iyear++)
{f_rec_dev+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
(2.0*rec_sigma_sq));
f_rec_dev+=rec_logL_add;
fval+=w_rec*f_rec_dev;

f_rec_dev_early=0.0; //possible extra constraint on early rec deviations
if (w_rec_early>0.0)
{ if (styr_rec_dev<endyr_rec_phase1)
{
    for(iyear=styr_rec_dev; iyear<endyr_rec_phase1; iyear++)
    //f_rec_dev_early+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
    // (2.0*rec_sigma_sq)) + rec_logL_add;
    {f_rec_dev_early+=square(log_rec_dev(iyear));}
}
fval+=w_rec_early*f_rec_dev_early;
}

f_rec_dev_end=0.0; //possible extra constraint on ending rec deviations
if (w_rec_end>0.0)
{ if (endyr_rec_phase2<endyr)
{
    for(iyear=(endyr_rec_phase2+1); iyear<endyr; iyear++)
    //f_rec_dev_end+=(square(log_rec_dev(iyear)-R_autocorr*log_rec_dev(iyear-1) + rec_sigma_sq/2.0)/
    // (2.0*rec_sigma_sq)) + rec_logL_add;
    {f_rec_dev_end+=square(log_rec_dev(iyear));}
}
fval+=w_rec_end*f_rec_dev_end;
}

//fval+=norm2(log_Nage_dev); //applies if initial age structure is estimated

//Random walk components of fishery dependent indices
f_cl_RW_cpue=0.0;
for (iyear=styr_cl_cpue; iyear<endyr_cl_cpue; iyear++)
{f_cl_RW_cpue+=square(q_RW_log_dev_CL(iyear))/(2.0*set_q_RW_CL_var);}
fval+=f_cl_RW_cpue;

//--Priors-----
//neg_log_prior arguments: estimate, prior, variance, pdf type
//Variance input as a negative value is considered to be CV in arithmetic space (CV=-1 implies loose prior)
//pdf type 1=none, 2=normal, 3=normal, 4=beta
f_priors=0.0;
f_priors+=neg_log_prior(len_cv_val, set_len_cv, square(set_len_cv_se), 2);
//f_priors+=neg_log_prior(stEEP, set_stEEP, square(set_stEEP_se), 4);
f_priors+=neg_log_prior(rec_sigma, set_rec_sigma, square(set_rec_sigma_se), 3);
//f_priors+=neg_log_prior(R_autocorr, set_R_autocorr, 1.0, 1);
//f_priors+=neg_log_prior(q_DD_beta, set_q_DD_beta, square(set_q_DD_beta_se), 2);
//f_priors+=neg_log_prior(q_rate, set_q_rate, dzero*square(set_q_rate), 2);
//f_priors+=neg_log_prior(F_init, set_F_init, -1.0, 2);
//f_priors+=neg_log_prior(M_constant, set_M_constant, square(set_M_constant_se), 2);

//f_priors+=neg_log_prior(selpar_L50_CL, set_selpar_L50_CL, 1.0, 3);
f_priors+=neg_log_prior(selpar_slope_CL, set_selpar_slope_CL, -0.5, 3);
//f_priors+=neg_log_prior(selpar_L50_CH, set_selpar_L50_CH, 1.0, 3);
f_priors+=neg_log_prior(selpar_slope_CH, set_selpar_slope_CH, -0.5, 3);
//f_priors+=neg_log_prior(selpar_L50_MM, set_selpar_L50_MM, 1.0, 3);
f_priors+=neg_log_prior(selpar_slope_MM, set_selpar_slope_MM, -0.5, 3);

//f_priors+=neg_log_prior(selpar_L50_rA, set_selpar_L50_rA, 0.5, 2);
//f_priors+=neg_log_prior(selpar_slope_rA, set_selpar_slope_rA, 0.5, 2);
//f_priors+=neg_log_prior(selpar_L502_CL, set_selpar_L502_CL, -1.0, 1);
//f_priors+=neg_log_prior(selpar_slope2_CL, set_selpar_slope2_CL, -1.0, 1);
//f_priors+=neg_log_prior(selpar_min_CL, set_selpar_min_CL, -1.0, 1);
//f_priors+=neg_log_prior(selpar_afull_CL, set_selpar_afull_CL, -1.0, 1);

//f_priors+=neg_log_prior(selpar_peak_CB, set_selpar_peak_CB, -1.0, 2);
//f_priors+=neg_log_prior(selpar_top_CB, set_selpar_top_CB, -1.0, 2);
//f_priors+=neg_log_prior(selpar_ascwid_CD, set_selpar_ascwid_CD, -1.0, 2);
//f_priors+=neg_log_prior(selpar_deswid_CD, set_selpar_deswid_CD, -1.0, 2);
//f_priors+=neg_log_prior(selpar_init_CD, set_selpar_init_CD, -1.0, 2);
//f_priors+=neg_log_prior(selpar_final_CD, set_selpar_final_CD, -1.0, 2);

fval+=f_priors;

//if(!last_phase())
//{
//for (iyear=styr; iyear<endyr; iyear++)
//{
//    if(FapeX(iyear)>1.0)
//    {
//        fval+=10*(mfexp(FapeX(iyear)-1.0)-1.0);
//    }
//}
//cout << "fval = " << fval << " fval_data = " << fval_data << endl;
//cout << endl;
//cout << "f_CL_U = " << f_CL_cpue << " f_MM_U = " << f_MM_cpue << " f_cL_L = " << f_cL_L << " f_cH_L = " << f_cH_L
//<< " f_rA_L = " << f_rA_L << endl;
//cout << "f_CL_lenc = " << f_CL_lenc << " f_cH_lenc = " << f_cH_lenc << " f_rA_lenc = " << f_rA_lenc << " f_MM_lenc = " << f_MM_lenc << endl;
//cout << "f_CL_agec = " << f_CL_agec << " f_cH_agec = " << f_cH_agec << " f_MM_agec = " << f_MM_agec << endl;
//cout << "f_rec_dev = " << f_rec_dev << " f_rec_dev_early = " << f_rec_dev_early << " f_rec_dev_end = " << f_rec_dev_end << " f_rec_histDev = " << f_rec_histDev << " f_CL_RW = " << f_CL_RW_cpue << endl;
//cout << endl;

//-----Logistic function: 2 parameters
FUNCTION dvar_vector logistic(const dvar_vector& ages, const dvariable& L50, const dvariable& slope)

```

```

//ages=vector of ages, L50=age at 50% selectivity, slope=rate of increase
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
Sel_Tmp=1./(1.+mfexp(-1.*slope*(ages-L50))); //logistic;
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Logistic function: 4 parameters
FUNCTION dvar_vector logistic_double(const dvar_vector& ages, const dvariable& L501, const dvariable& slope1, const dvariable& L502, const dvariable& slope2)
//ages=vector of ages, L50=age at 50% selectivity, slope=rate of increase, L502=age at 50% decrease additive to L501, slope2=slope of decrease
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
Sel_Tmp=elem_prod( (1./1.+mfexp(-1.*slope1*(ages-L501))), (1.- (1. / (1.+mfexp(-1.*slope2*(ages-(L501+L502)))))) );
Sel_Tmp=Sel_Tmp/max(Sel_Tmp);
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Jointed logistic function: 6 parameters (increasing and decreasing logistics joined at peak selectivity)
FUNCTION dvar_vector logistic_joint(const dvar_vector& ages, const dvariable& L501, const dvariable& slope1, const dvariable& L502, const dvariable& slope2, const dvariable& satval, const dvariable& joint)
//ages=vector of ages, L501=age at 50% sel (ascending limb), slope1=rate of increase,L502=age at 50% sel (descending), slope2=rate of increase (ascending),
//satval=saturation value of descending limb, joint=location in age vector to join curves (may equal age or age + 1 if age=0 is included)
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
Sel_Tmp=1.0;
for (iage=1; iage<=nages; iage++)
{
  if (double(iage)<joint) {Sel_Tmp(iage)=1. / (1.+mfexp(-1.*slope1*(ages(iage)-L501)))};
  if (double(iage)>joint) {Sel_Tmp(iage)=1.0 - (1.0-satval) / (1.+mfexp(-1.*slope2*(ages(iage)-L502)))};
}
Sel_Tmp=Sel_Tmp/max(Sel_Tmp);
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Double Gaussian function: 6 parameters (as in SS3)
FUNCTION dvar_vector gaussian_double(const dvar_vector& ages, const dvariable& peak, const dvariable& top, const dvariable& ascwid, const dvariable& deswid, const dvariable& init, const dvariable& final)
//ages=vector of ages, peak=ascending inflection location (as logistic), top=width of plateau, ascwid=ascent width (as log(width))
//deswid=descent width (as log(width))
RETURN_ARRAYS_INCREMENT();
dvar_vector Sel_Tmp(ages.indexmin(),ages.indexmax());
dvar_vector sel_step1(ages.indexmin(),ages.indexmax());
dvar_vector sel_step2(ages.indexmin(),ages.indexmax());
dvar_vector sel_step3(ages.indexmin(),ages.indexmax());
dvar_vector sel_step4(ages.indexmin(),ages.indexmax());
dvar_vector sel_step5(ages.indexmin(),ages.indexmax());
dvar_vector sel_step6(ages.indexmin(),ages.indexmax());
dvar_vector pars_tmp(1,6); dvar_vector sel_tmp_iq(1,2);

pars_tmp(1)=peak;
pars_tmp(2)=peak+1.0+(0.99*ages(nages)-peak-1.0)/(1.0+mfexp(-top));
pars_tmp(3)=mfexp(ascwid);
pars_tmp(4)=mfexp(deswid);
pars_tmp(5)=1.0/(1.0+mfexp(-init));
pars_tmp(6)=1.0/(1.0+mfexp(-final));

sel_tmp_iq(1)=mfexp(-(square(ages(1)-pars_tmp(1))/pars_tmp(3)));
sel_tmp_iq(2)=mfexp(-(square(ages(nages)-pars_tmp(2))/pars_tmp(4)));

sel_step1=mfexp(-(square(ages-pars_tmp(1))/pars_tmp(3));
sel_step2=pars_tmp(5)+(1.0-par_tmp(5))*(sel_step1-sel_tmp_iq(1))/(1.0-sel_tmp_iq(1));
sel_step3=mfexp(-(square(ages-pars_tmp(2))/pars_tmp(4));
sel_step4=1.0*(pars_tmp(6)-1.0)*(sel_step3-1.0)/(sel_tmp_iq(2)-1.0);
sel_step5=1.0/(1.0+mfexp(-(20.* elem_div((ages-pars_tmp(1)), (1.0+sfabs(ages-pars_tmp(1)))) )) );
sel_step6=1.0/(1.0+mfexp(-(20.0*elem_div((ages-pars_tmp(2)), (1.+sfabs(ages-pars_tmp(2)))) )) );

Sel_Tmp=elem_prod(sel_step2,(1.0-sel_step5)+ elem_prod(sel_step4,sel_step6));
elem_prod(sel_step5,((1.0-sel_step6)+ elem_prod(sel_step4,sel_step6)) );

Sel_Tmp=Sel_Tmp/max(Sel_Tmp);
RETURN_ARRAYS_DECREMENT();
return Sel_Tmp;

//-----
//Spawner-recruit function (Beverton-Holt)
FUNCTION dvariable SR_func(const dvariable& R0, const dvariable& h, const dvariable& spr_F0, const dvariable& SSB)
//R0=virgin recruitment, h=steepness, spr_F0=spawners per recruit @ F=0, SSB=spawning biomass
RETURN_ARRAYS_INCREMENT();
dvariable Recruits_Tmp;
Recruits_Tmp=((0.8*R0*h*SSB)/(0.2*R0*spr_F0*(1.0-h)+(h-0.2)*SSB));
RETURN_ARRAYS_DECREMENT();
return Recruits_Tmp;

//-----
//compute multinomial effective sample size for a single yr
FUNCTION double multinom_eff_N(const dvar_vector& pred_comp, const dvar_vector& obs_comp)
//pred_comp=vector of predicted comps, obscomp=vector of observed comps
dvariable EffN_Tmp; dvariable numer; dvariable denom;
RETURN_ARRAYS_INCREMENT();
numer=sum( elem_prod(pred_comp,(1.0-pred_comp)) );
denom=sum( square(obs_comp-pred_comp) );
if (denom>0.0) (EffN_Tmp=numer/denom);
else (EffN_Tmp=missing);
RETURN_ARRAYS_DECREMENT();
return EffN_Tmp;

//-----
//Likelihood contribution: lognormal
FUNCTION dvariable lk_lognormal(const dvar_vector& pred, const dvar_vector& obs, const dvar_vector& cv, const dvariable& wgt_dat)
//pred=vector of predicted vals, obs=vector of observed vals, cv=vector of CVs in arithmetic space, wgt_dat=constant scaling of CVs
//dzero is small value to avoid log(0) during search
RETURN_ARRAYS_INCREMENT();
dvariable LkvalTmp;

```

```

dvar_vector var(cv.indexmin(),cv.indexmax()); //variance in log space
var=log(1.0+square(cv/wgt_dat)); // convert cv in arithmetic space to variance in log space
LkvalTmp+=sum(0.5*elem_div(square(log(elem_div((pred+dzero),(obs+dzero)))),var));
RETURN_ARRAYS_DECREMENT();
return LkvalTmp;

//-----
//Likelihood contribution: multinomial
FUNCTION dvariable lk_multinomial(const dvar_vector& nsamp, const dvar_matrix& pred_comp, const dvar_matrix& obs_comp, const double& ncomp, const double& minSS, const dvariable& wgt_dat)
//nsamp=vector of N's, pred_comp=matrix of predicted comps, obs_comp=matrix of observed comps, ncomp = number of yrs in matrix, minSS=min N threshold, wgt_dat=scaling of N's
RETURN_ARRAYS_INCREMENT();
dvariable LkvalTmp;
LkvalTmp=0.0;
for (int ii=1; ii<=ncomp; ii++)
{if (nsamp(ii)>minSS)
 {LkvalTmp+=wgt_dat*nsamp(ii)*sum(elem_prod((obs_comp(ii)+dzero),
 log(elem_div((pred_comp(ii)+dzero), (obs_comp(ii)+dzero))))));
 }
}
RETURN_ARRAYS_DECREMENT();
return LkvalTmp;

//-----
//Likelihood contribution: priors
FUNCTION dvariable neg_log_prior(dvariable pred, const double& prior, dvariable var, int pdf)
//prior=prior point estimate, var=variance (if negative, treated as CV in arithmetic space), pred=predicted value, pdf=prior type (1=none, 2=lognormal, 3=normal, 4=beta)
dvariable LkvalTmp;
dvariable alpha, beta, ab_iq;
LkvalTmp=0.0;
// compute generic pdf's
switch(pdf) {
  case 1: //option to turn off prior
  LkvalTmp=0.0;
  break;
  case 2: // lognormal
  if(prior<=0.0) cout << "YIKES: Don't use a lognormal distn for a negative prior" << endl;
  else if(pred<0) LkvalTmp=huge_number;
  else {
    if(var<0.0) var=log(1.0+var*var); // convert cv to variance on log scale
    LkvalTmp= 0.5*( square(log(pred/prior))/var + log(var) );
  }
  break;
  case 3: // normal
  if(var<0.0 && prior!=0.0) var=square(var*prior); // convert cv to variance on observation scale
  else if(var<0.0 && prior==0.0) var=-var; // cv not really appropriate if prior value equals zero
  LkvalTmp= 0.5* ( square(pred-prior)/var + log(var) );
  break;
  case 4: // beta
  if(var<0.0) var=square(var*prior); // convert cv to variance on observation scale
  if(prior<0.0 || prior>1.0) cout << "YIKES: Don't use a beta distn for a prior outside (0,1)" << endl;
  ab_iq=prior*(1.0-prior)/var - 1.0; alpha=prior*ab_iq; beta=(1.0-prior)*ab_iq;
  if(pred<0 && pred<1) LkvalTmp= (1.0-alpha)*log(pred)+(1.0-beta)*log(1.0-pred)-gammln(alpha+beta)+gammln(alpha)+gammln(beta);
  else LkvalTmp=huge_number;
  break;
  default: // no such prior pdf currently available
  cout << "The prior must be either 1(lognormal), 2(normal), or 3(beta)." << endl;
  cout << "Presently it is " << pdf << endl;
  exit(0);
}
return LkvalTmp;

//-----
REPORT_SECTION

if (last_phase())
{
  // cout<<"start report"<<endl;
  get_weighted_current();
  //cout<<"got weighted"<<endl;
  get_msy();
  //cout<<"got msy"<<endl;
  get_miscellaneous_stuff();
  //cout<<"got misc stuff"<<endl;
  get_per_recruit_stuff();
  //cout<<"got per recruit"<<endl;
  get_effective_sample_sizes();

  cout <<endl;
  cout << "><-><-><-><-><-><-><-><-><-><-><-><->" <<endl;
  cout << "BC Fmsy" << F_msy_out<< " BC SSBmsy" << SSB_msy_out <<endl;
  cout << "F status" << FdF_msy_end<<endl;
  cout << "Pop status" << SdSSB_msy_end<<endl;
  cout << "h" << steep<< " R0" << R0<<endl;
  cout << "><-><-><-><-><-><-><-><-><-><->" <<endl;

  // report << "TotalLikelihood " << fval << endl;
  // report << "N" << endl;
  // report << N<<endl;
  // report << "F" << endl;
  // report << F <<endl;

  #include "spp_make_Robject.cxx" // write the S-compatible report
} //endl last phase loop

```



## Appendix B Data inputs for the Beaufort Assessment Model





```

6.0 # age at 50% selectivity
3.0 # slope of ascending limb
#20.0 # descending age at 50% selection
#0.0 # slope of descending limb
#1.0 # minimum selectivity
#6.0 # first age at full selection
#7.0 #peak=ascending inflection location (as logistic),
#-1.0 #top=width of plateau,
#2.5 #ascwid=ascent width (as log(width))
#4.3 #decwid=descent width (as log(width))
#-7.9 #init
#5.0 #final
#8.0 # age at 50% selection (2nd period)
#1.5 # slope of ascending limb (2nd period)

#commercial handline selectivity starting values
6.0 # age at 50% selectivity
3.0 # slope of ascending limb
#20.0 # descending age at 50% selection
#0.0 # slope of descending limb
#1.0 # minimum selectivity
#6.0 # first age at full selection
#7.0 #peak=ascending inflection location (as logistic),
#-1.0 #top=width of plateau,
#2.5 #ascwid=ascent width (as log(width))
#4.3 #decwid=descent width (as log(width))
#-7.9 #init
#5.0 #final

#recreational selectivity starting values
6.0 # age at 50% selectivity
2.0 # slope of ascending limb
#20.0 # descending age at 50% selection
#0.0 # slope of descending limb
#1.0 # minimum selectivity
#6.0 # first age at full selection
#7.0 #peak=ascending inflection location (as logistic),
#-1.0 #top=width of plateau,
#2.5 #ascwid=ascent width (as log(width))
#4.3 #decwid=descent width (as log(width))
#-7.9 #init
#5.0 #final

#MARMAP selectivity starting values
6.0 # age at 50% selectivity
3.0 # slope of ascending limb
#20.0 # descending age at 50% selection
#0.0 # slope of descending limb
#1.0 # minimum selectivity
#6.0 # first age at full selection
#7.0 #peak=ascending inflection location (as logistic),
#-1.0 #top=width of plateau,
#2.5 #ascwid=ascent width (as log(width))
#4.3 #decwid=descent width (as log(width))
#-7.9 #init
#5.0 #final

##### Likelihood Component Weighting#####
##Weights in objective fcn
1.0 #landings
0.114 #cL length comps
1.591 #cH length comps
0.0 #rA length comps
#1.0 #mm length comps
0.039 #cL age comps
1.46 #cH age comps
0.073 #mm age comps
8.71 #mm index
3.0 #cL index
1.0 #S-R residuals
0.0 #constraint on early recruitment deviations
0.0 #constraint on ending recruitment deviations
0.0 #penalty if F exceeds 3.0 (reduced by factor of 10 each phase, not applied in final phase of optimization)
0.0 #weight on tuning F (penalty not applied in final phase of optimization)
#0.0 #penalty on deviation in CV at age
#0.0 #penalty on first difference in CV at age

#log catchabilities (initial guesses)
-8.0 #MARMAP longline CPUE
-8.0 #commercial logbook CPUE
#rate increase switch: Integer value (choose estimation phase, negative value turns it off)
-1
##annual positive rate of increase on all fishery dependent q's due to technology creep
0.0
# DD q switch: Integer value (choose estimation phase, negative value turns it off)
-1
##density dependent catchability exponent, value of zero is density independent, est range is (0.1,0.9)
0.0
##SE of density dependent catchability exponent (0.128 provides 95% CI in range 0.5)
0.128
#Age to begin counting D-D q (should be age near full exploitation)
4
#Random walk switch: Integer value (choose estimation phase, negative value turns it off)
-3
#Variance (sd^2) of fishery dependent random walk catchabilities (0.03 is near the sd=0.17 of Wilberg and Bence
0.03

##log mean F's (initial guesses)
-5.0 #commercial longline
-5.5 #comm handline
-6.5 #recreational

#Initial F (Input here, could also use mean of first few years)
0.01

```

```

#Tuning F (not applied in last phase of optimization)
0.2
#Year for tuning F
2006

##threshold sample sizes for length comps (set to 99999.0 if sel is fixed)
1.0 #CL
1.0 #cH
1.0 #RA
#1.0 #mm

##threshold sample sizes (greater than or equal to) for age comps
1.0 #CL
1.0 #cH
1.0 #mm

#Ageing error matrix (columns are true age 1-25, rows are ages as read for age comps: columns should sum to one)
1.21674E-12 0.000138245 3.98227E-05 3.80014E-06 3.04762E-07 1.65774E-08 6.97239E-10 2.91631E-11 7.67427E-13 2.19448E-14 4.20047E-16 8.38542E-18 1.32313E-19 1.57241E-21 1.87743E-23 2.2826E-25
1.94823E-27 1.65772E-29 9.22312E-32 4.98883E-34 2.67307E-36 1.47043E-38 5.14917E-41 1.98284E-43
0 1.092915419 0.008203951 0.0006502195 4.96291E-05 2.95815E-06 1.42989E-07 6.66902E-09 2.11376E-10 6.91767E-12 1.58937E-13 3.67438E-15 6.80654E-17 9.66359E-19 1.34641E-20 1.87078E-22 1.87201E-24
1.83586E-26 1.21286E-28 7.68159E-31 4.75828E-33 2.99047E-35 1.23858E-37 5.58598E-40
0 1.21674E-12 0.813892668 0.200612753 0.025603013 0.002606191 0.000205664 1.29284E-05 7.39139E-07 3.00616E-08 1.19008E-09 3.4169E-11 9.4871E-13 2.12493E-14 3.69106E-16 6.13551E-18 9.94585E-20
1.18634E-21 1.36244E-23 1.08181E-25 8.11791E-28 5.87939E-30 4.26736E-32 2.10782E-34 1.1223E-36
0 2.19178E-48 0.092915419 0.044133735 0.231960431 0.044133735 0.00557101 0.000515354 3.97033E-05 2.20754E-06 1.11732E-07 4.17373E-09 1.44336E-10 4.02584E-12 8.76196E-14 1.77659E-15 3.42995E-17
4.95839E-19 6.77368E-21 6.54489E-23 5.88815E-25 5.04262E-27 4.27274E-29 2.53786E-31 1.60812E-33
0 5.8451E-108 0.000138245 0.200612753 0.483564988 0.24100681 0.058795547 0.0090557048 0.001033624 8.37034E-05 5.72485E-06 2.89667E-07 1.29391E-08 4.62875E-10 1.29268E-11 3.26876E-13 7.67288E-15
1.3668E-16 2.25614E-18 2.68573E-20 2.93126E-22 3.00208E-24 3.00178E-26 2.16187E-28 1.64335E-30
0 2.3078E-191 2.68073E-09 0.008203951 0.231960431 0.424406659 0.2410763503 0.070175785 0.013041743 0.01638768 0.00016008 1.14224E-05 6.83479E-07 3.22971E-08 1.18528E-09 3.82156E-11 1.11341E-12
2.48486E-14 5.03428E-16 7.47534E-18 1.00154E-19 1.2406E-21 1.47971E-23 1.30291E-25 1.19767E-27
0 1.3489E-298 6.77482E-16 3.98227E-05 0.025603013 0.24100681 0.387322602 0.239721872 0.079752598 0.0165665 0.002442862 0.000255917 2.12734E-05 1.3676E-06 6.75446E-08 2.83897E-09 1.04805E-10 2.97941E-12
7.5256E-14 1.41126E-15 2.3487E-23 5.55861E-19 5.118E-21 5.55553E-23 6.2251E-25
0 0 2.23143E-24 2.29446E-08 0.000650259 0.044133735 0.241763503 0.361033738 0.236368913 0.086473511 0.020344459 0.003257803 0.000390157 3.51436E-05 2.3922E-06 1.34011E-07 6.39928E-09 2.35609E-10
7.53662E-12 1.80715E-13 3.78029E-15 7.08553E-17 1.24208E-18 1.67595E-20 2.30757E-22
0 0 9.57798E-05 1.56919E-12 3.80014E-06 0.002606191 0.058795547 0.239721872 0.339525345 0.233063621 0.092465542 0.023563147 0.0042163 0.000548062 5.26556E-05 4.01959E-06 2.53459E-07 1.22881E-08
5.05643E-10 1.56961E-11 4.17603E-13 9.79278E-16 2.11508E-16 3.57703E-18 6.10045E-20
0 0 5.35884E-47 1.27383E-15 5.11012E-09 4.96291E-05 0.00557101 0.070175785 0.236368913 0.324343317 0.22935076 0.096833367 0.026848172 0.00518688 0.000720327 7.66098E-05 6.51194E-06 4.22679E-07
2.2727E-08 9.2469E-10 3.16623E-11 9.39467E-13 2.52713E-14 5.40143E-16 1.15019E-17
0 0 3.90741E-61 1.22741E-16 5.51811E-12 3.04762E-07 0.000205664 0.009057048 0.079752598 0.233063621 0.310460919 0.226099747 0.10073686 0.029790441 0.006124267 0.000927786 0.000108527 9.58891E-06
6.84342E-07 3.69496E-08 1.64764E-09 6.25604E-11 2.11863E-12 5.77059E-14 1.54659E-15
0 0 3.71313E-77 1.40383E-30 1.12577E-16 6.03502E-10 2.95815E-16 0.000515354 0.013041743 0.086473511 0.22935076 0.299956602 0.222716621 0.10383452 0.032360678 0.007139582 0.0001173262 0.000143469
1.3805E-05 1.00146E-06 5.8847E-08 2.89174E-09 1.24626E-10 4.36171E-12 1.48314E-13
0 0 4.59867E-95 1.90581E-18 1.84431E-21 3.85382E-23 1.65774E-08 1.29284E-05 0.001033624 0.0165665 0.092465542 0.226099747 0.29013984 0.21963455 0.106272301 0.034910717 0.008227667 0.001415735
0.000186565 1.84105E-05 1.44254E-06 2.7813E-08 5.14383E-09 2.33248E-10 1.01435E-11
0 0 7.4228E-115 3.07105E-47 6.95246E-27 9.38594E-17 3.61951E-11 1.42989E-08 3.97033E-05 0.001638768 0.020344459 0.096833367 0.222716621 0.281938007 0.216901007 0.108469067 0.037426976 0.009213755
0.0016891 0.000229565 2.42701E-05 2.06635E-06 1.48967E-07 8.82479E-09 4.94758E-10
0 0 1.5615E-136 5.87406E-57 6.0306E-33 5.26986E-21 3.07906E-14 6.97239E-10 7.39139E-07 8.37034E-05 0.002442862 0.023563147 0.10073686 0.21963455 0.275132607 0.21414808 0.110438129 0.03954793 0.01024502
0.001941585 0.000280256 3.1944E-05 3.02706E-06 2.3622E-07 1.72107E-08
0 0 4.2811E-05 160 1.33362E-67 1.20365E-39 1.12848E-17 2.01205E-17 1.49892E-12 6.66902E-09 2.20754E-06 0.00016008 0.003257803 0.026848172 0.10383452 0.216901007 0.268648 0.211387655 0.111954895 0.041629568
0.011138216 0.002222116 0.000342781 4.31597E-05 4.47356E-06 4.26975E-07
0 0 5.1297E-185 3.59394E-79 5.52789E-47 7.79263E-31 1.31784E-21 1.42068E-15 2.91631E-11 3.00616E-08 5.72485E-06 0.000255917 0.0042163 0.029790441 0.106272301 0.21414808 0.262462028 0.209023295
0.113324201 0.043339502 0.012082195 0.002553207 0.000431778 5.99397E-05 7.55451E-06
0 0 7.1238E-213 1.14961E-91 5.84165E-55 1.73527E-36 6.63038E-26 5.93656E-19 6.18078E-14 2.11376E-10 1.11732E-07 1.14224E-05 0.000390157 0.00518688 0.032360678 0.108469067 0.211387655 0.257382228
0.2066689 0.114382946 0.045107907 0.013200708 0.003030875 0.0005682 9.53256E-05
0 0 4.3237E-242 4.3649E-105 1.42046E-63 1.24608E-42 1.29972E-30 1.09369E-22 6.34875E-17 7.67427E-13 1.19008E-09 2.89667E-07 2.12734E-05 0.000548062 0.006124267 0.034910717 0.110438129 0.209023295
0.282498779 0.204761211 0.115584719 0.047375131 0.014928009 0.003810778 0.000857853
0 0 3.4201E-273 1.9672E-119 7.94773E-73 2.88548E-49 9.92654E-36 8.8832E-27 3.1606E-20 1.43866E-15 6.91767E-12 4.17373E-09 6.83479E-07 3.51436E-05 0.000720327 0.007139582 0.037426976 0.111954895
0.2066689 0.248624064 0.203277388 0.118017272 0.051589524 0.01802176 0.0050550733
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