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SEDAR 39

HMS Gulf of Mexico Smoothhound Complex

Assessment Process Report

SEDAR 39 Review Workshop

February 10-12, 2015, Panama City, FL



Outline

- Rationale
- Data inputs
- Model description
- Base model and results
- Retrospective analysis
- Uncertainty analysis (sensitivities)
- Projections
- Conclusions

Why assess a complex vs. individual species?

- Inability to differentiate among species due to difficulty of correct identification. This made it necessary to conduct the analyses on the complex of three species of GOM *Mustelus*

Why use surplus production models?

- Inability to differentiate among species precluded use of an age-structured model
- Use of a production model still allowed us to carry out quantitative projections

Why use Bayesian methods?

- Bayesian methods combine the *likelihood* with the *prior* distributions of each parameter to calculate a *posterior* distribution including both sources of information
- Demographic information allows us to develop an informative prior for r for smoothhound sharks

Why use state-space Bayesian surplus production model (SS-SPM) (Meyer and Millar 1999)?

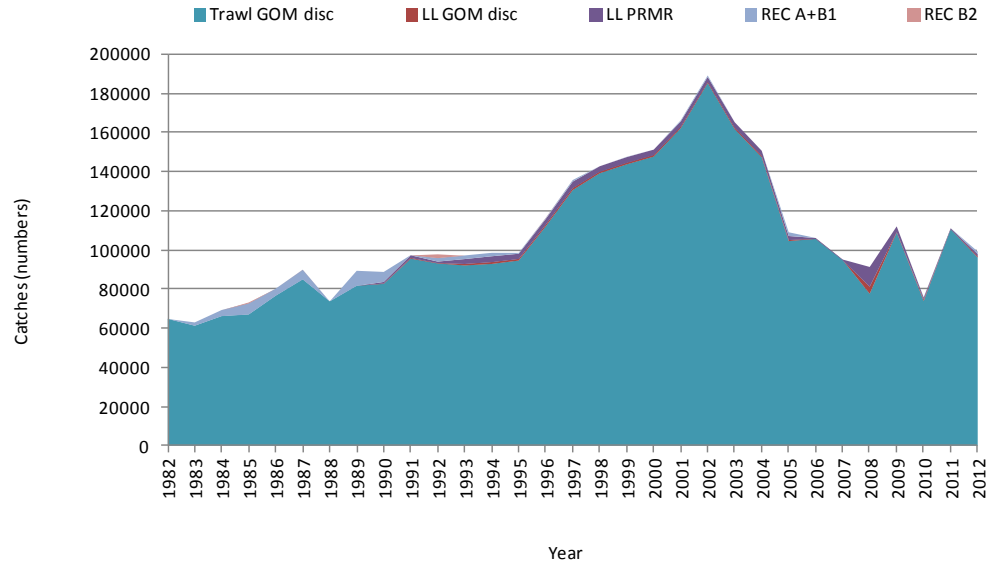
We initially attempted to use the Bayesian Surplus Production (BSP) model (McAllister and Babcock 2006), but the model was not able to fit the indices of abundance adequately (it showed flat trends) and the Assessment Panel (AP) recommended using an alternative approach. We thus decided to use a state-space Bayesian surplus production model (Meyer and Millar 1999), which in addition to considering observation error (like the BSP), also considers process error.

Data inputs

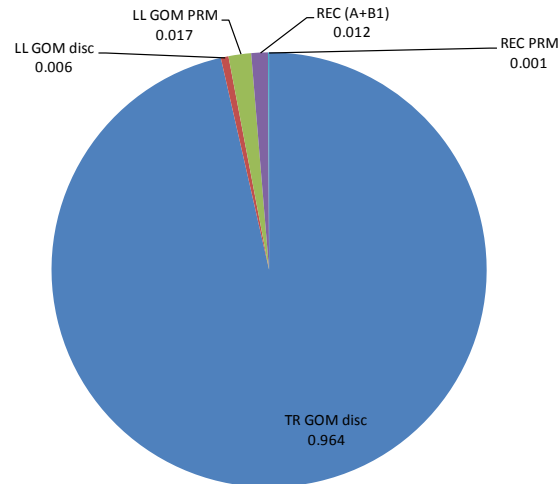
- Catch (one single series)
- Indices of abundance:
 1. NMFS SE Bottom Longline (NMFSSSEBLL)
 2. Groundfish Trawl_Fall (GROUNDTRF)
 3. Groundfish Trawl_Summer (GROUNDTRS)
 4. Small Pelagics Trawl (SMALLPELTR)
- Priors for r , K , $P_{82}=N_{82}/K$ (initial depletion), observation error process error variances, proportions of carrying capacity ($P_t=N_t/K$, $t \geq 2$)

Catches of smoothhounds in the Gulf of Mexico, 1982-2012 (top) and as a proportion for all years combined (bottom)

Mustelus spp. catches (Gulf of Mexico)

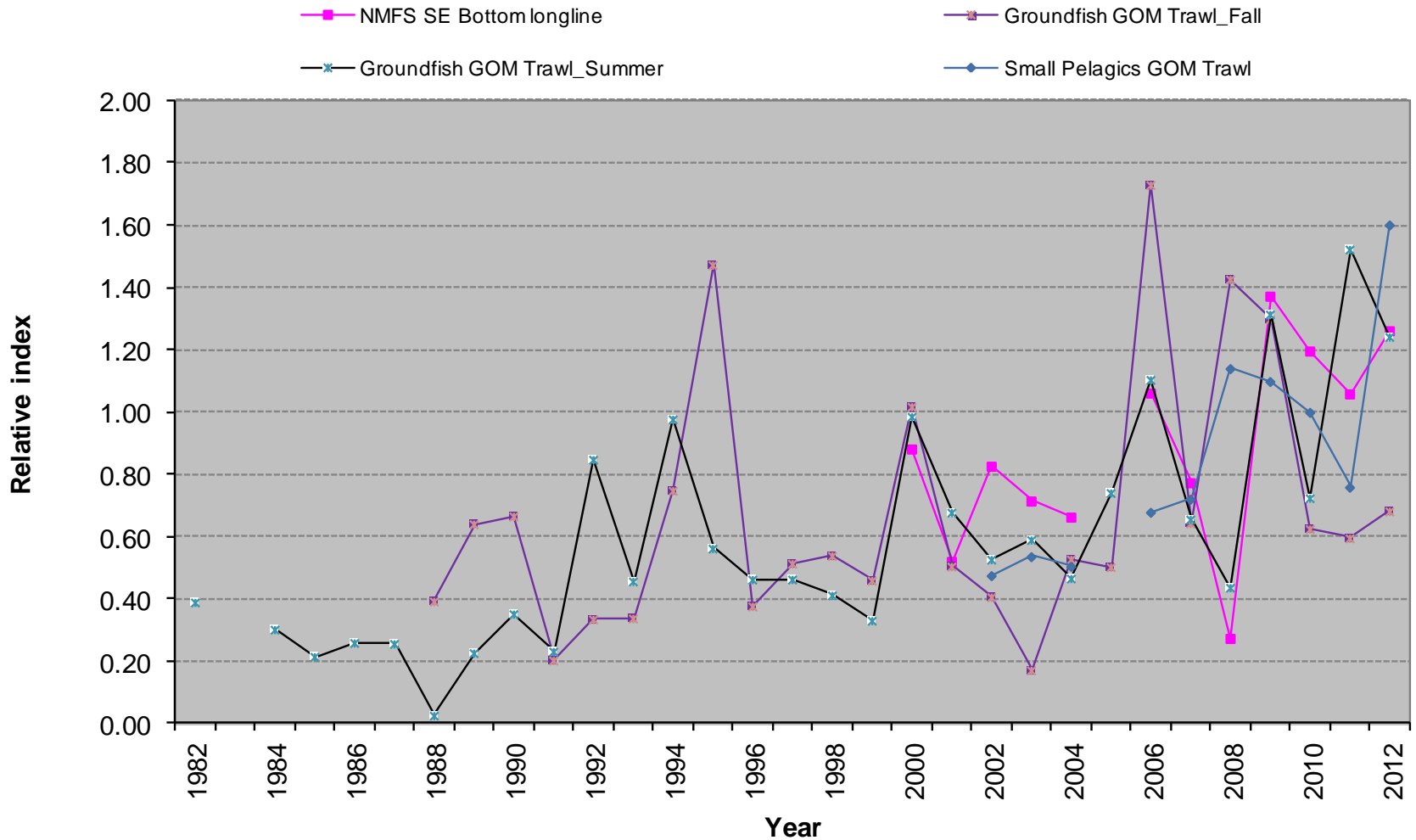


Smoothhound catches, 1982-2012 combined (Gulf of Mexico)

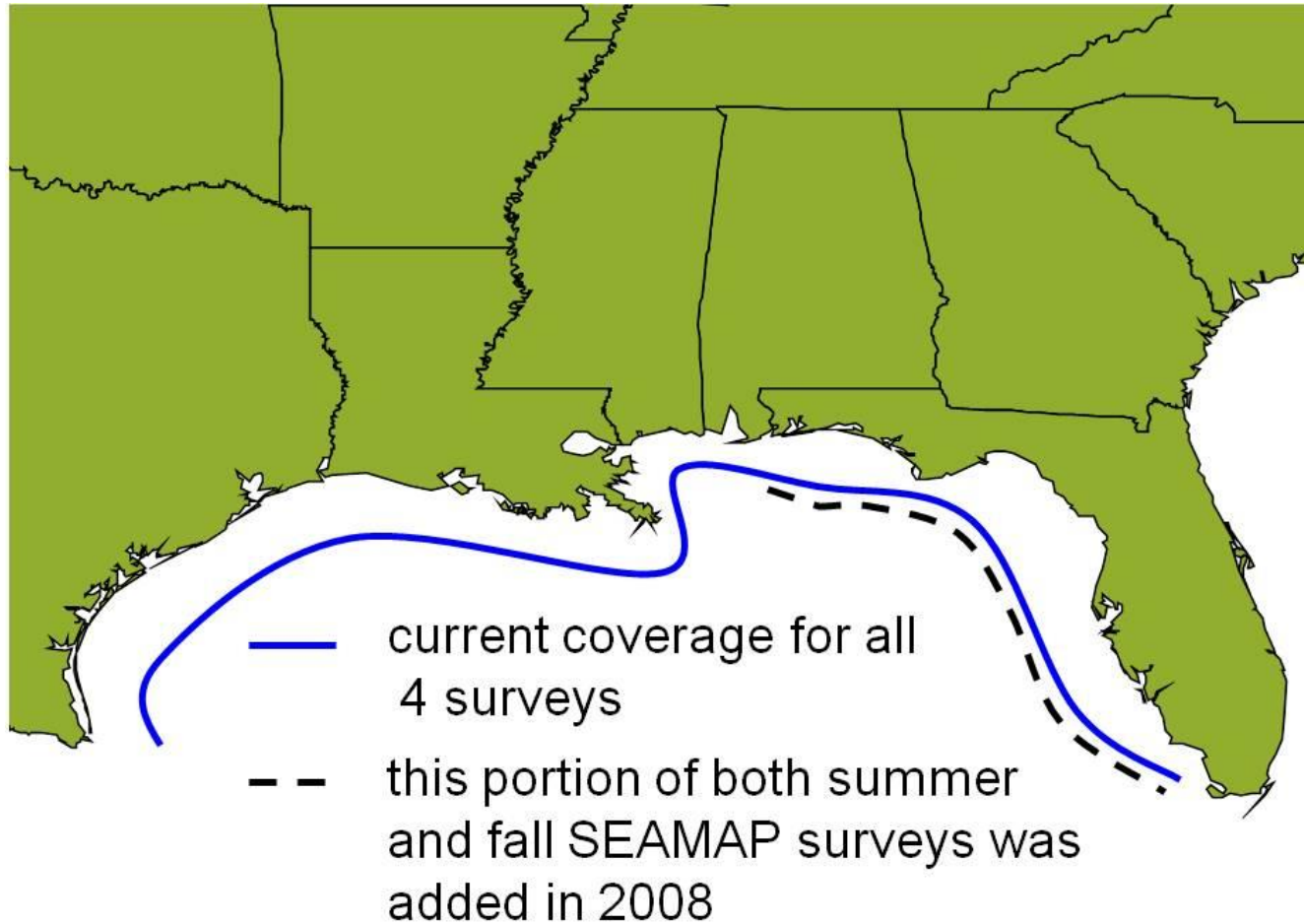


Indices of abundance

Indices of abundance: Gulf of Mexico



Approximate linear coverage of specific abundance indices for *Mustelus* spp. in the Gulf of Mexico



Model configuration

- Model started in 1982 and ended in 2012
- The first year in which both CPUE and catch data were available was 1982
- In the base run, each individual index of abundance value was weighted equally
- Model is fitted to the CPUEs and catch is treated as a known constant

Estimated parameters

Parameters to be estimated: K , r , P_{82} (initial depletion at the start of the model, $t=1$), P_t ($t \geq 2$), σ^2 for P_t (process error variance) and τ^2 for each CPUE index (observation error variance)

State-space Bayesian surplus production model (SS-SPM) (Meyer and Millar 1999)

Surplus production model is reparameterized by expressing the annual abundance as a proportion of carrying capacity:

$$P_{initial} = (P_{mean_initial})e^{\sigma_{initial}^2} \quad P_1 = (P_{initial})e^{\sigma^2} \quad \text{Hierarchical for the initial year}$$

$$P_t = (P_{t-1} + rP_{t-1}(1 - P_{t-1}) - \frac{C_{t-1}}{K})e^{\sigma^2}$$

$$P_t = \left(\frac{N_t}{K} \right)$$

Observed catch rates ($I_{j,t}$) relate to unobserved states (P_t) through a stochastic observation model for $I_{j,t}$ given P_t

$$I_{j,t} = q_j K P_t e^{\tau^2}$$

State-space Bayesian surplus production model (SS-SPM)

The catchability coefficient for each index of abundance (q_j) is taken as the MLE (closed form):

$$q_j = e^{\left(\frac{\sum_{t=1}^{t=y} (\ln(I_{j,t}) - \ln(N_t))}{n_j} \right)}$$

r (intrinsic rate of growth)

- *r* obtained from life tables
- Life History WG recommended using values for *Mustelus canis* + *Mustelus sinusmexicanus* and *M. norrisi* to bound the range of biologically plausible values
- Life tables were used to calculate r_{\max} for these 2 groupings based on values listed in the DW report

Biological Inputs: *M. canis-M. sinusmexicanus*

- Von Bertalanffy growth curve:
 $L_{\infty} = 113.8 \text{ cm FL}$, $K = 0.130 \text{ yr}^{-1}$, $t_0 = -3.87 \text{ yr}$
- Lifespan = 14 yr; $a_{50} = 3.6 \text{ yr}$
- Length-weight relationship: $W = 2 \times 10^{-6} L^{3.258}$
- Pup-production: pups = 10 (midpoint of 15 and 5)
- Parturition frequency: annual (1 yr)
- Natural Mortality = 0.30 (age-0) \rightarrow 0.17 (a_{max})
- $r = 0.28 \text{ yr}^{-1}$

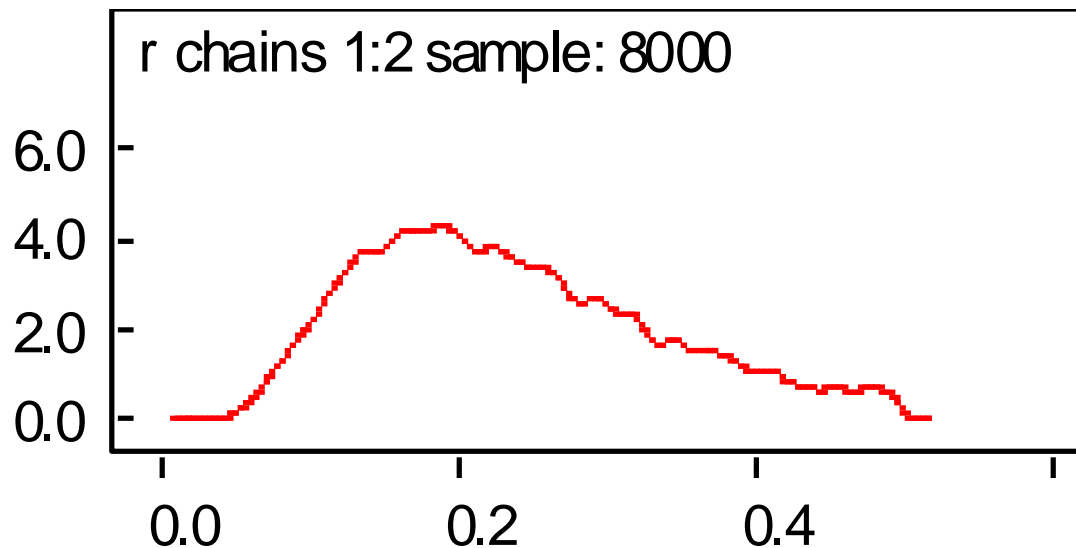
Biological Inputs: *M. norrisi*

- Von Bertalanffy growth curve:
 $L_{\infty} = 95.05$ cm FL, $K = 0.250$ yr⁻¹, $t_0 = -2.03$ yr
- Lifespan = 9 yr; $a_{50} = 3.6$ yr
- Length-weight relationship: $W = 2 \times 10^{-6} L^{3.2486}$
- Pup-production: pups = 11.3
- Parturition frequency: annual (1 yr)
- Natural Mortality = 0.47 (age-0) \rightarrow 0.24 (a_{\max})
- $r = 0.18$ yr⁻¹

Prior for r

An informative prior for $r=0.23 \text{ yr}^{-1}$, equivalent to a $\log(r)=-1.470$, was used as the mean of a lognormal distribution with a precision=4, which corresponds to a CV of 0.5 on the arithmetic scale

$$r \sim \text{dlnorm}(-1.470, 4.0) | (0.01, 0.5)$$

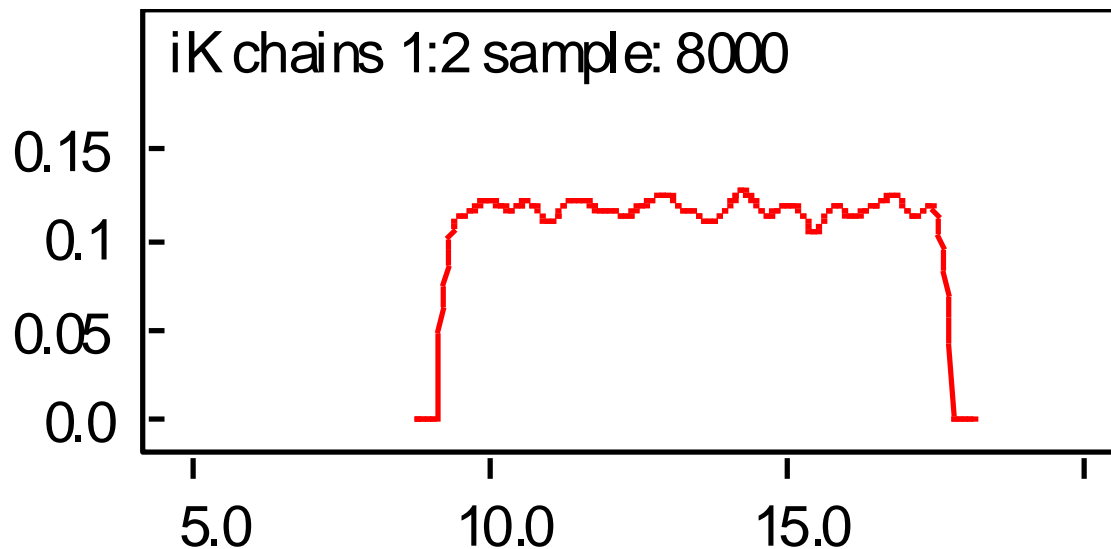


| node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|------|-------|---------|----------|---------|--------|--------|-------|--------|
| r | 0.236 | 0.09876 | 0.001084 | 0.08492 | 0.2215 | 0.4596 | 50001 | 8000 |

Prior for K (*carrying capacity*)

Uniform on $\log(K)$, with a range of 10^4 to 50×10^6 (ca. 250 times the maximum observed catch) individuals on the arithmetic scale

$$iK \sim \text{dunif}(9.21, 17.73); \quad K = \exp(iK)$$

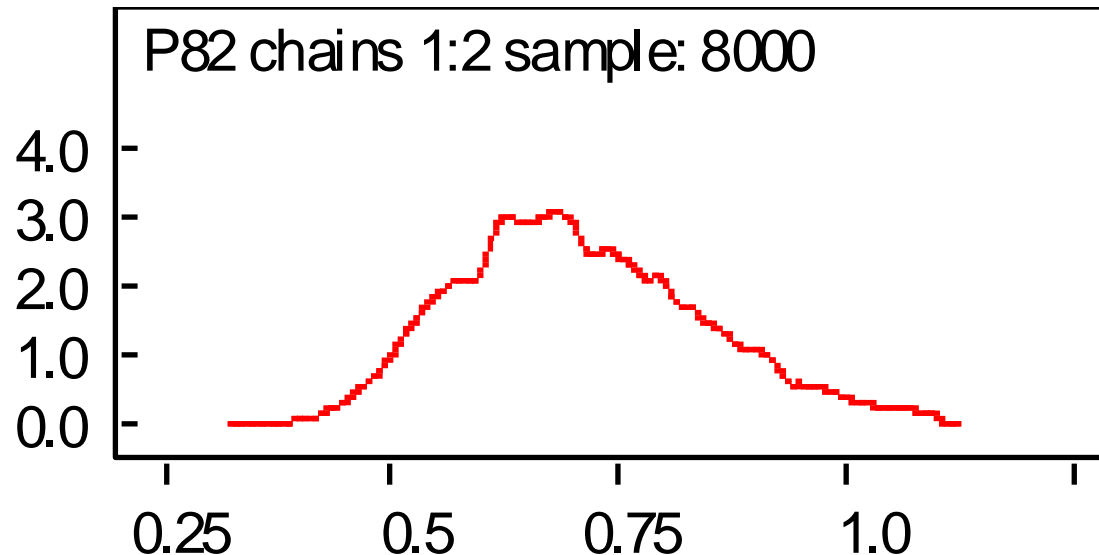


| node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|------|-------|-------|----------|-------|--------|-------|-------|--------|
| iK | 13.47 | 2.462 | 0.02572 | 9.406 | 13.45 | 17.53 | 50001 | 8000 |

Prior for $P_{82} = N_{82}/K$ (*initial depletion*)

An informative prior for $P_{82}=0.7$, equivalent to a $\log(P_{82})=-0.357$, was used as the mean of a lognormal distribution with the precision=25, which corresponds to a CV of 0.2 on the arithmetic scale

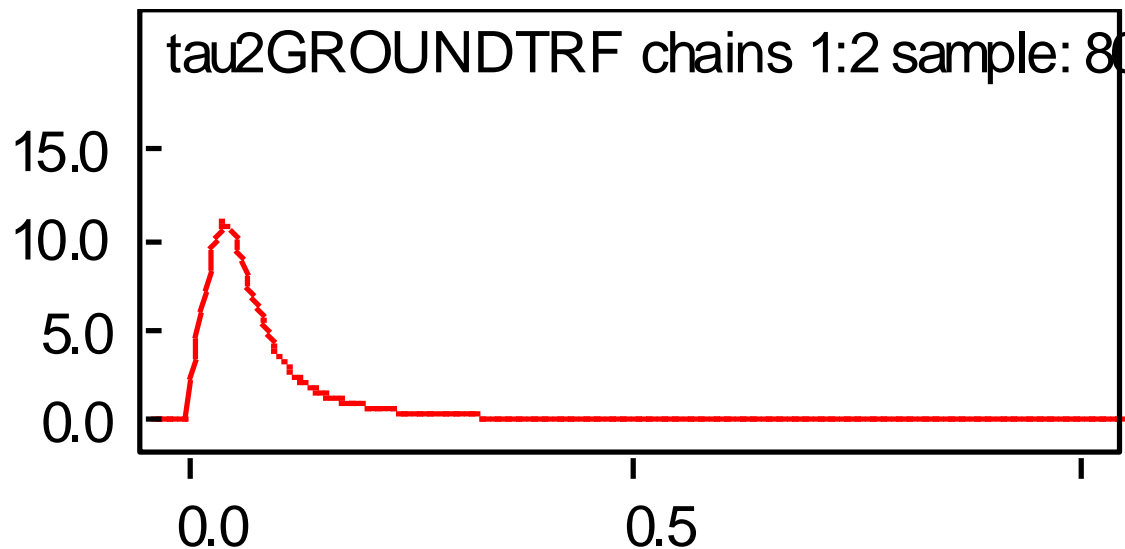
$$P_{82} \sim \text{dlnorm}(-0.357, 25.0) | (0.2, 1.1)$$



| node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|------|-------|--------|----------|--------|--------|-------|-------|--------|
| P82 | 0.708 | 0.1359 | 0.001381 | 0.4762 | 0.6945 | 1.005 | 50001 | 8000 |

Prior for observation error variance (inverse gamma)

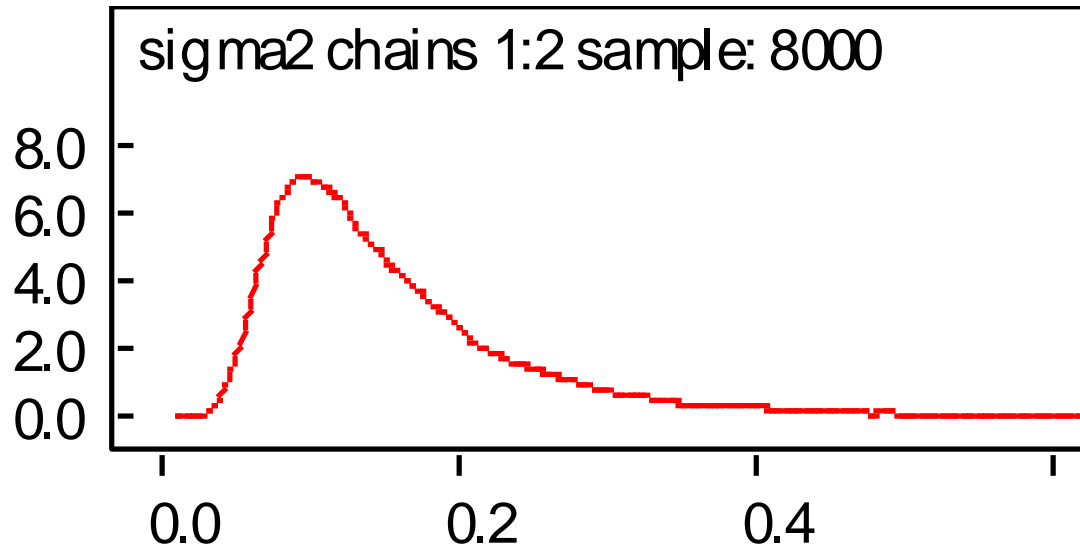
- Same for each CPUE index
- $\text{itau2GROUNDTRF} \sim \text{dgamma}(2.0, 0.1)$ Precision
- $\text{tau2GROUNDTRF} \leftarrow 1/\text{itau2GROUNDTRF}$ Variance
- $\text{IGROUNDTRF}_{[i]} \sim \text{dlnorm}(\text{lmeanGROUNDTRF}_{[i]}, \text{itau2GROUNDTRF})$



| node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|---------------|---------|--------|----------|---------|---------|--------|-------|--------|
| tau2GROUNDTRF | 0.09917 | 0.2513 | 0.002924 | 0.01795 | 0.05974 | 0.3957 | 50001 | 8000 |

Prior for process error variance (inverse gamma)

- $P_{[i]} = N_{[i]}/K$
- $\text{isigma2} \sim \text{dgamma}(4.0, 0.5)$
- $\text{sigma2} \leftarrow 1/\text{isigma2}$
- $\text{Pmean}_{[i]} \leftarrow \log(\max(P_{[i-1]} + r * P_{[i-1]} * (1 - P_{[i-1]}) - C_{[i-1]}/K, 0.0001))$
- $P_{[i]} \sim \text{dlnorm}(\text{Pmean}_{[i]}, \text{isigma2})|(0.0001, 1.1)$



| node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|--------|-------|--------|----------|--------|--------|--------|-------|--------|
| sigma2 | 0.167 | 0.1221 | 0.001461 | 0.0572 | 0.1357 | 0.4626 | 50001 | 8000 |

MCMC simulation

- Two chains
- A thinning interval of 5 was used to minimize parameter autocorrelation
- Initial 50,000 iterations were discarded
- Another 20,000 iterations with a thinning interval of 5 were run to generate the posterior distributions and DIC (sample size: $2 \times 20,000 / 5 = 8,000$)

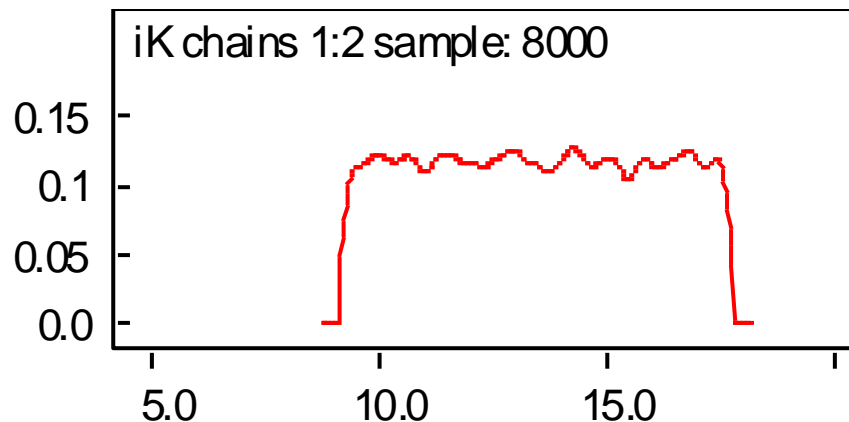
Posterior distribution

Joint posterior distribution of the unobservable states given the data, which is equal to the product of the joint prior distribution and the sampling distribution (likelihood of the CPUE data) by Bayes' theorem

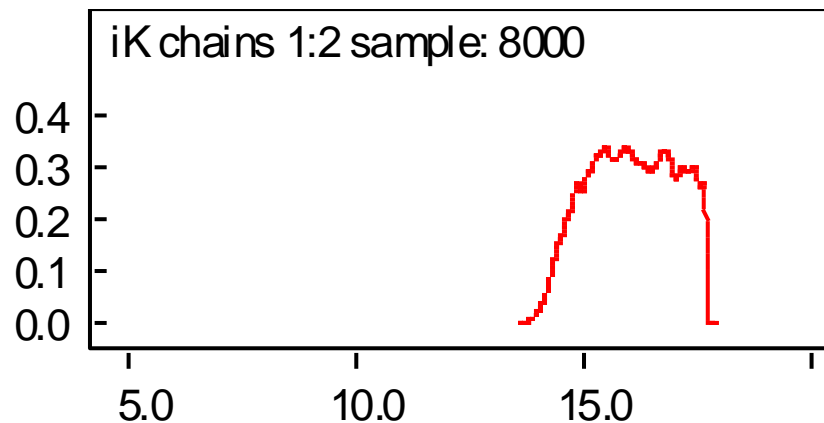
$$\begin{aligned} p(K, r, P_{82}, \sigma^2, \tau^2, P_2, \dots, P_n | I_1, \dots, I_n) = \\ p(K) p(r) p(P_{82}) p(\sigma^2) p(\tau^2) p(P_1 | P_{82}, \sigma^2) \\ \times \prod_{i=2}^{i=n} p(P_i | P_{i-1}, K, r, \sigma^2) \prod_{t=1}^{t=n} p(I_t | P_t, \tau^2) \end{aligned}$$

Prior and posterior distribution for carrying capacity ($K = \exp(iK)$) in the base run

Prior



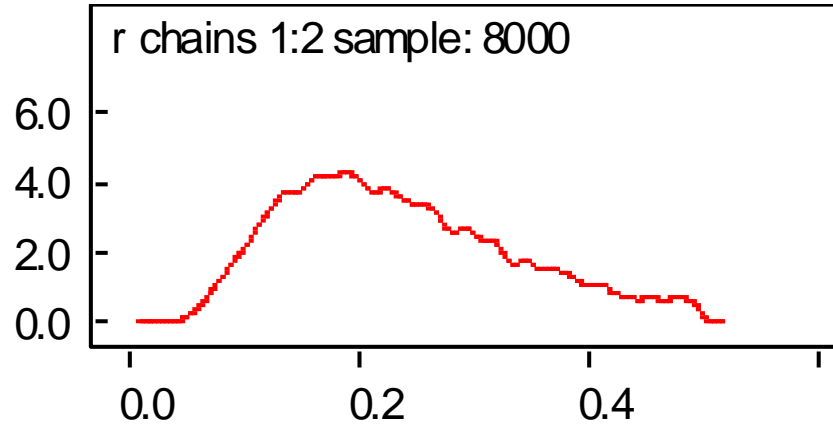
Posterior



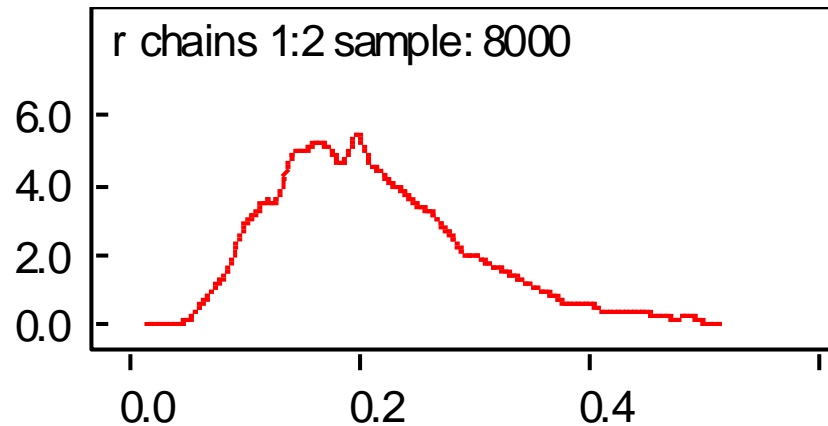
| | node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|-----------|------|-------|--------|----------|-------|--------|-------|-------|--------|
| Prior | iK | 13.47 | 2.462 | 0.02572 | 9.406 | 13.45 | 17.53 | 50001 | 8000 |
| Posterior | iK | 16.07 | 0.9529 | 0.01097 | 14.36 | 16.07 | 17.64 | 50001 | 8000 |

Prior and posterior distribution for the intrinsic rate of increase (r) in the base run

Prior



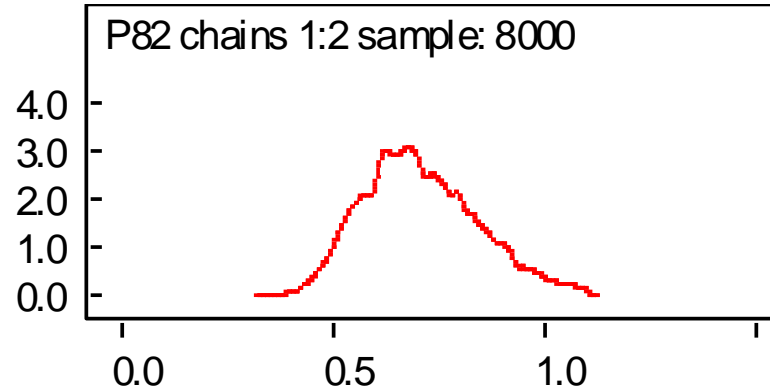
Posterior



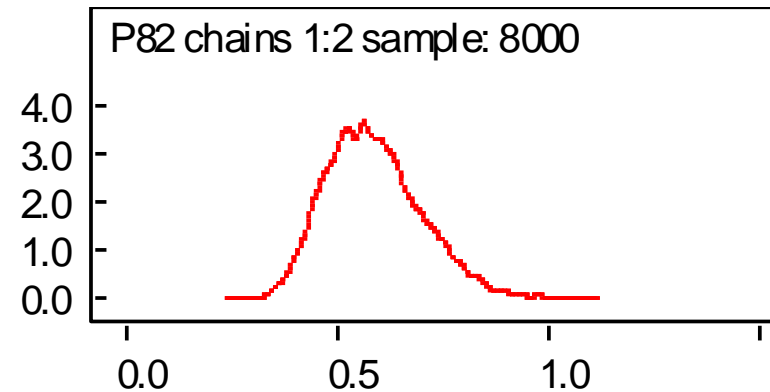
| | node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|-----------|------|--------|---------|----------|---------|--------|--------|-------|--------|
| Prior | r | 0.236 | 0.09876 | 0.001084 | 0.08492 | 0.2215 | 0.4596 | 50001 | 8000 |
| Posterior | r | 0.2115 | 0.08397 | 9.921E-4 | 0.08319 | 0.1993 | 0.4118 | 50001 | 8000 |

Prior and posterior distribution for initial depletion (P_{82}) in the base run

Prior



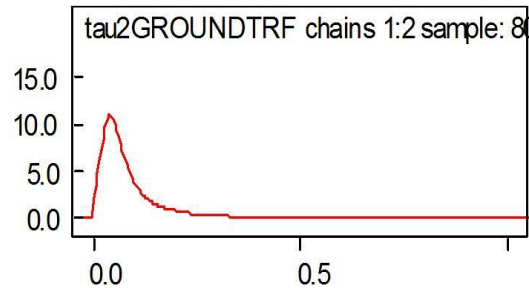
Posterior



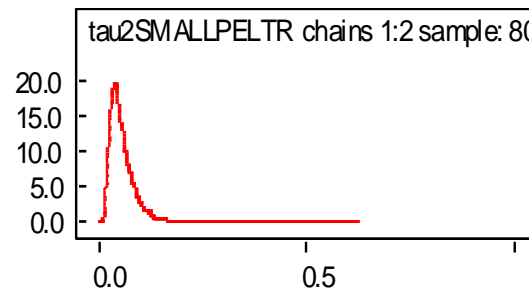
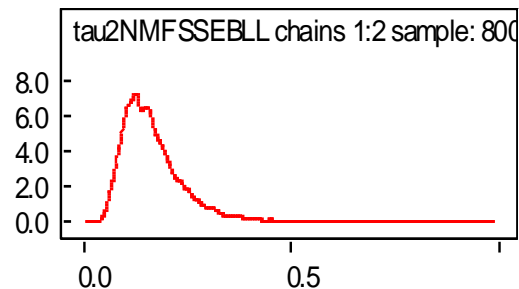
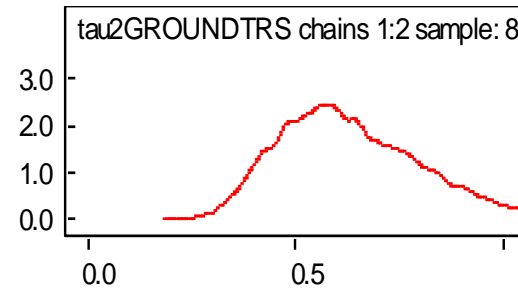
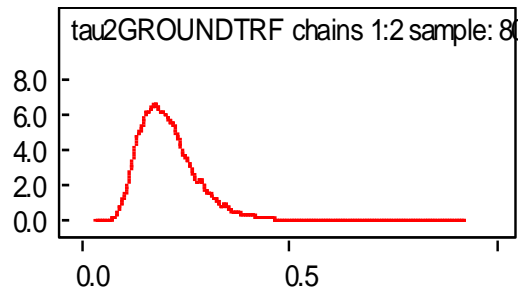
| | node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|-----------|------|--------|--------|----------|--------|--------|--------|-------|--------|
| Prior | P82 | 0.708 | 0.1359 | 0.001381 | 0.4762 | 0.6945 | 1.005 | 50001 | 8000 |
| Posterior | P82 | 0.5886 | 0.115 | 0.001462 | 0.3957 | 0.5777 | 0.8397 | 50001 | 8000 |

Prior and posterior distribution for the observation error variance (τ^2) in the base run

Prior



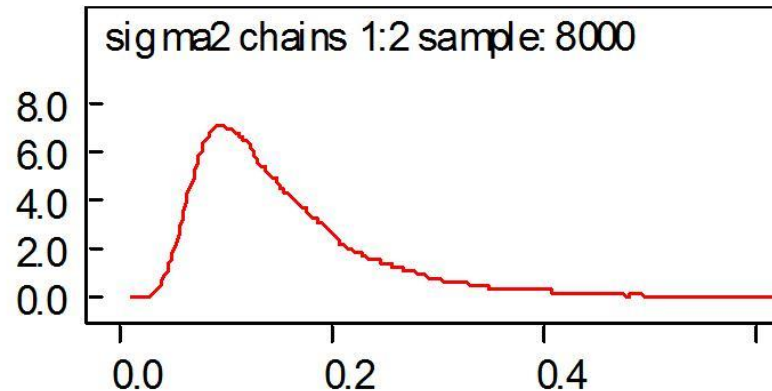
Posterior



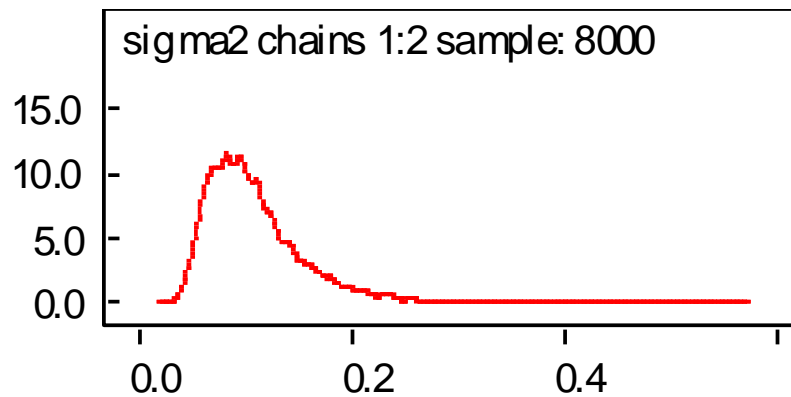
The prior (top panel) was the same for the four indices, but posteriors (four lower panels) differed.

Prior and posterior distribution for the process error variance (σ^2) in the base run

Prior



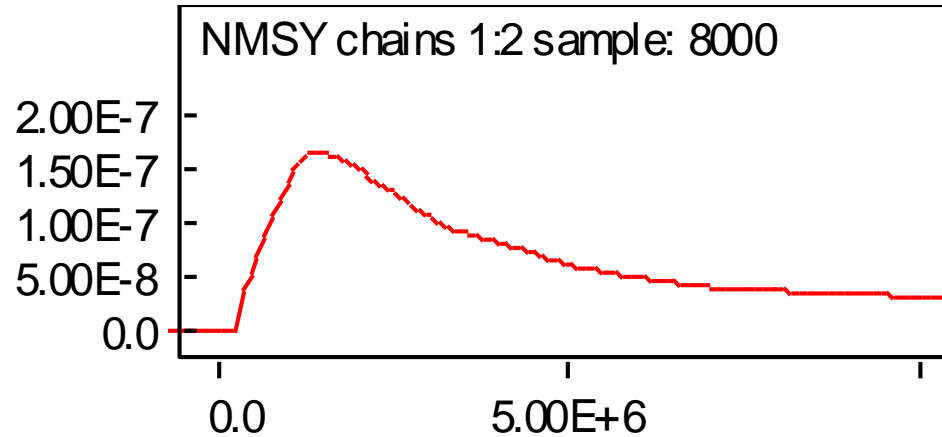
Posterior



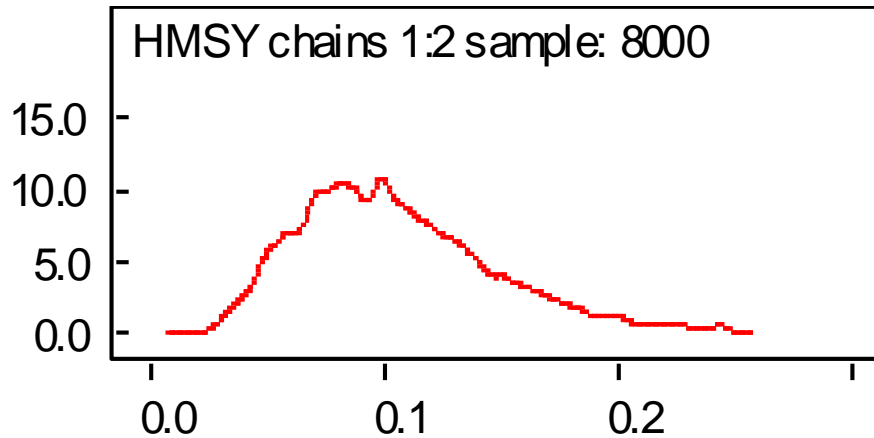
| | node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|-----------|--------|--------|---------|----------|---------|---------|--------|-------|--------|
| Prior | sigma2 | 0.167 | 0.1221 | 0.001461 | 0.0572 | 0.1357 | 0.4626 | 50001 | 8000 |
| Posterior | sigma2 | 0.1092 | 0.04772 | 7.778E-4 | 0.04947 | 0.09912 | 0.2293 | 50001 | 8000 |

Posterior distribution for the predicted exploitable number at MSY (N_{msy}) and exploitation rate at MSY (H_{msy}) in the base run

Posterior

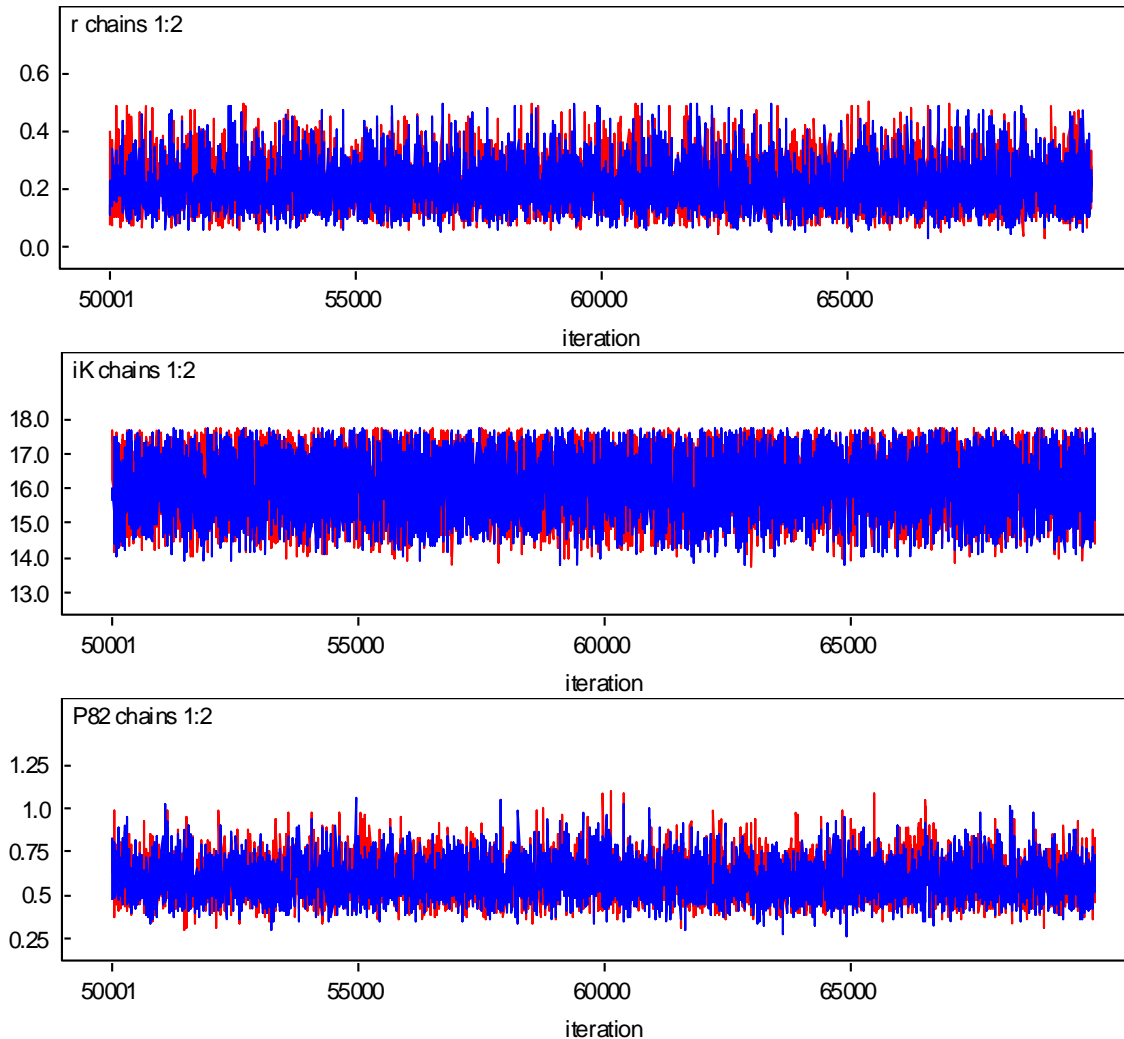


Posterior

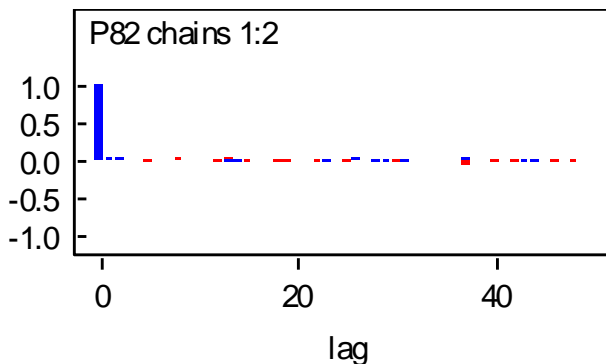
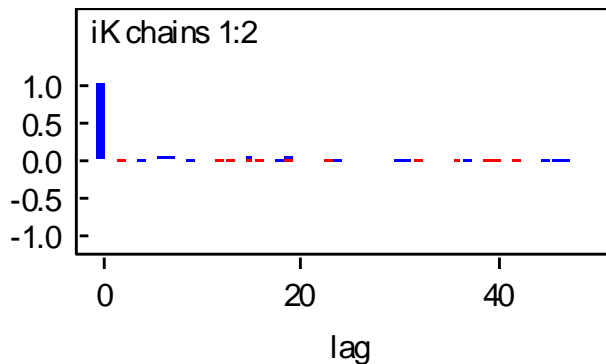
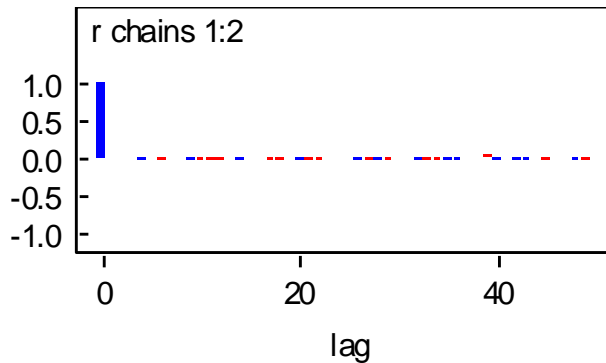


| | node | mean | sd | MC error | 2.5% | median | 97.5% | start | sample |
|-----------|-----------|----------|---------|----------|----------|----------|----------|-------|--------|
| Prior | N_{MSY} | 7.188E+6 | 6.3E+6 | 69280.0 | 859400.0 | 4.746E+6 | 2.297E+7 | 50001 | 8000 |
| Posterior | H_{MSY} | 0.1057 | 0.04198 | 4.961E-4 | 0.0416 | 0.09967 | 0.2059 | 50001 | 8000 |

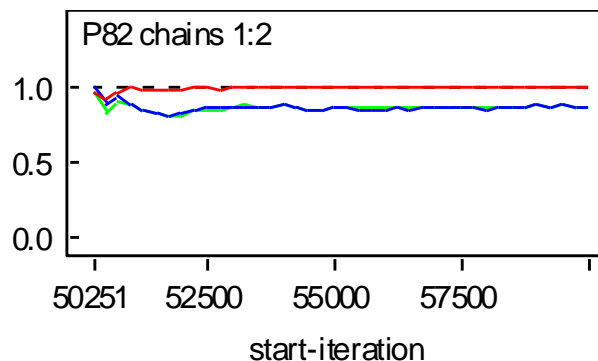
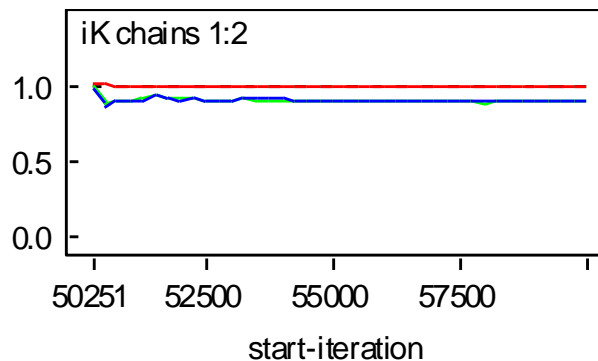
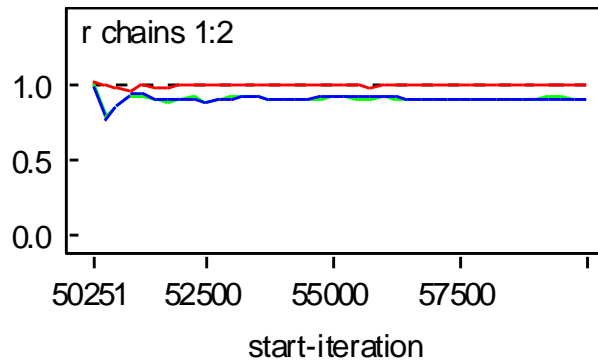
Convergence diagnostic for the base run showing the time series history of mixing for the two chains for the key model parameters



Convergence diagnostic for the base run showing the autocorrelation for the two chains for the key model parameters

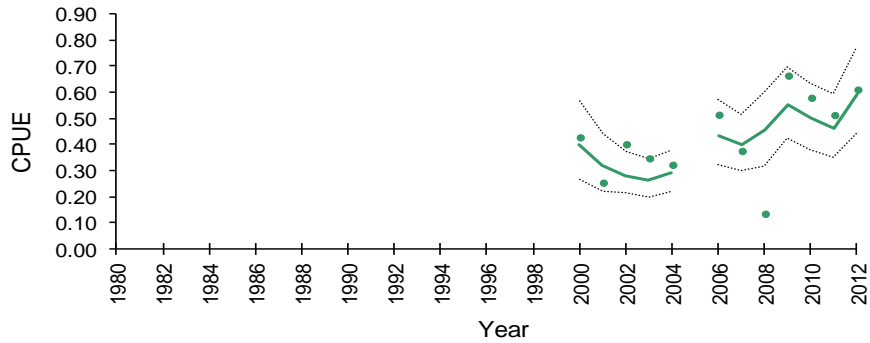


Convergence diagnostic for the base run showing the Gelman-Rubin statistic for the two chains for the key model parameters

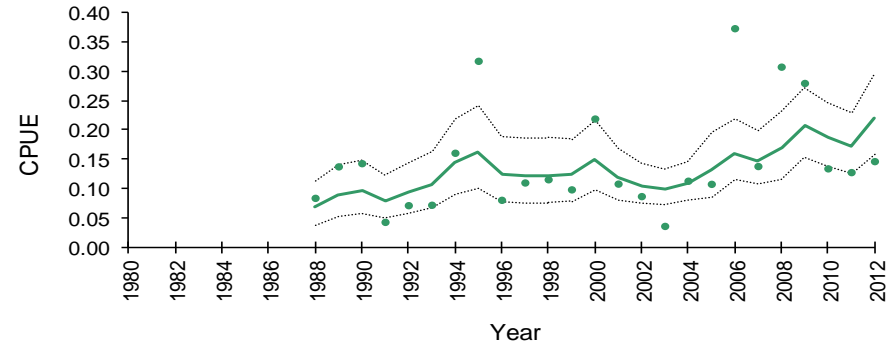


Predicted fits to the four indices of abundance in the base run

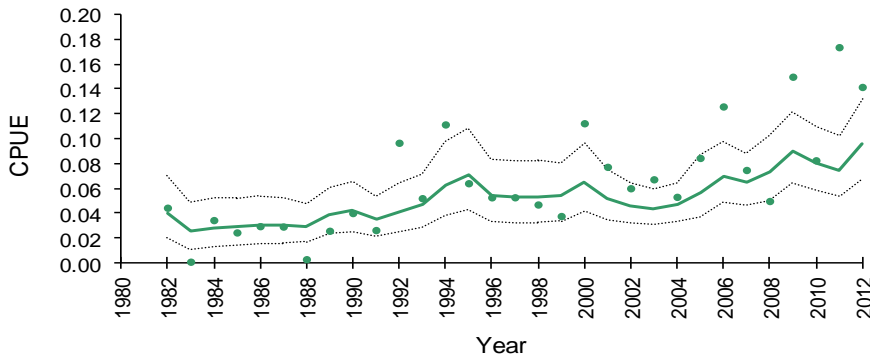
Model fit to NMFSSSEBL series



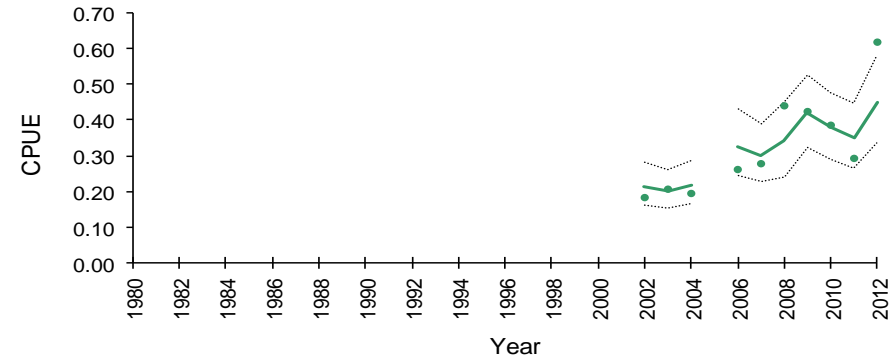
Model fit to GROUNDTRF series



Model fit to GROUNDTRS series



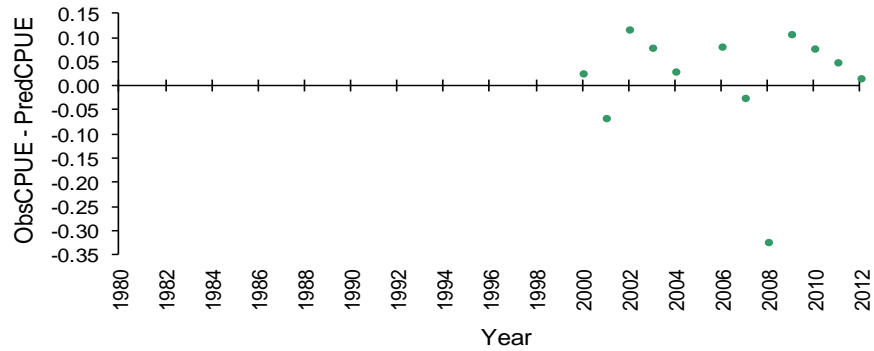
Model fit to SMALLPELTR series



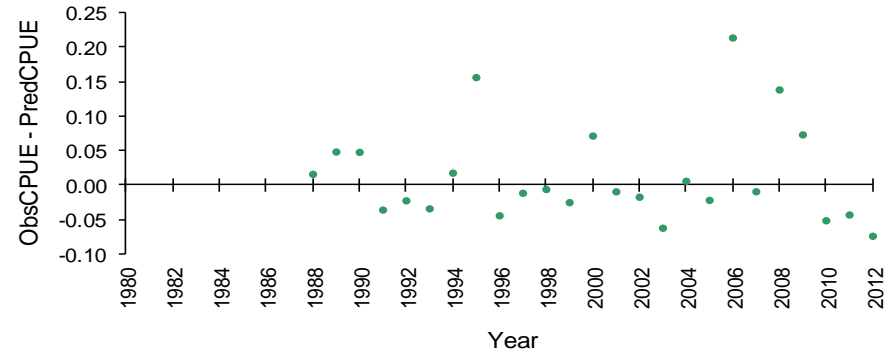
Solid circles are observed CPUEs, solid lines are mean predicted CPUEs, and dotted lines are 95% credible intervals.

Residual plots (normal scale) of the CPUE fits for the base run

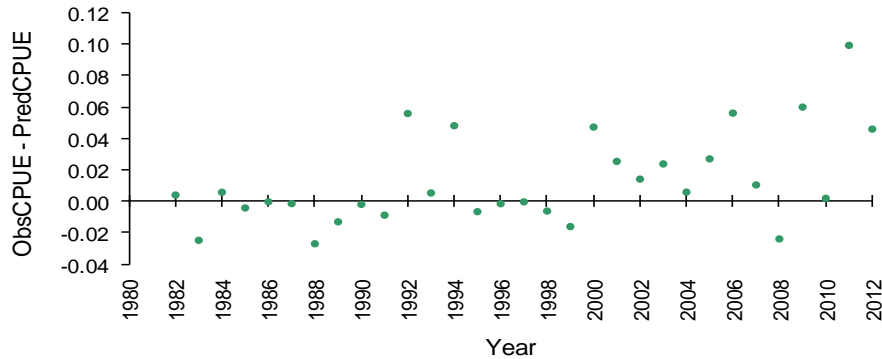
Model fit to NMFSSSEBLL series



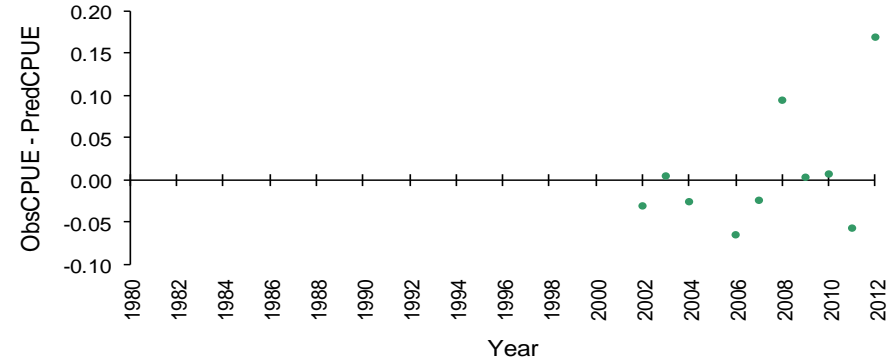
Model fit to GROUNDTRF series



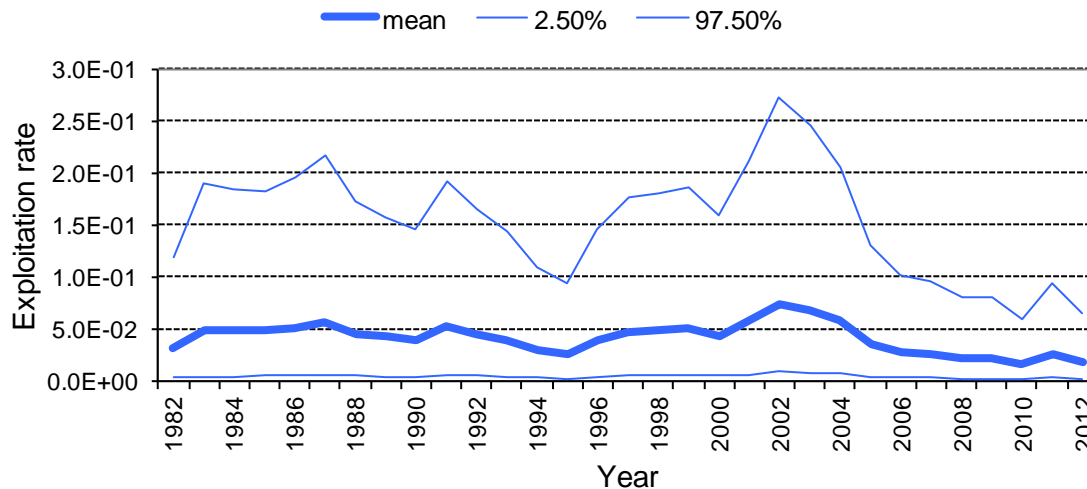
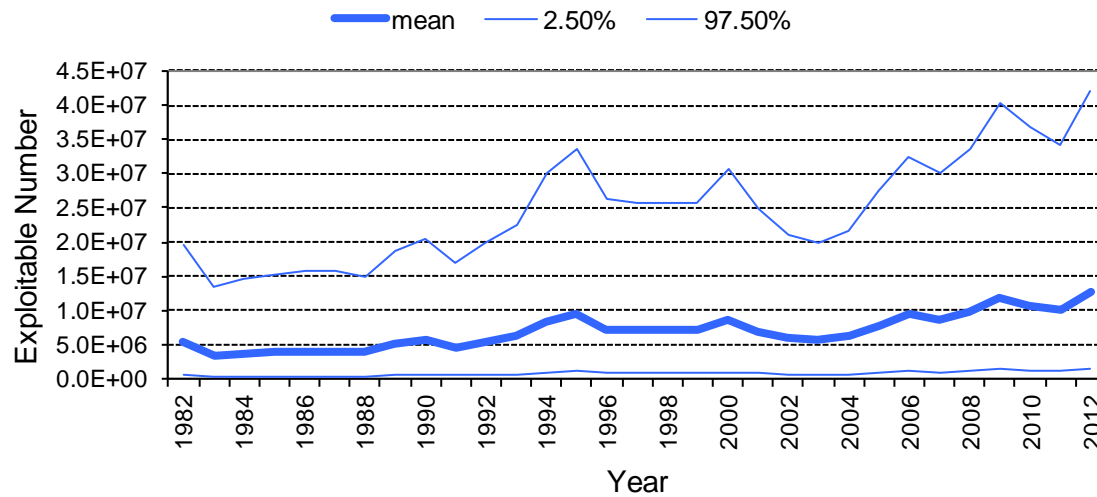
Model fit to GROUNDTRS series



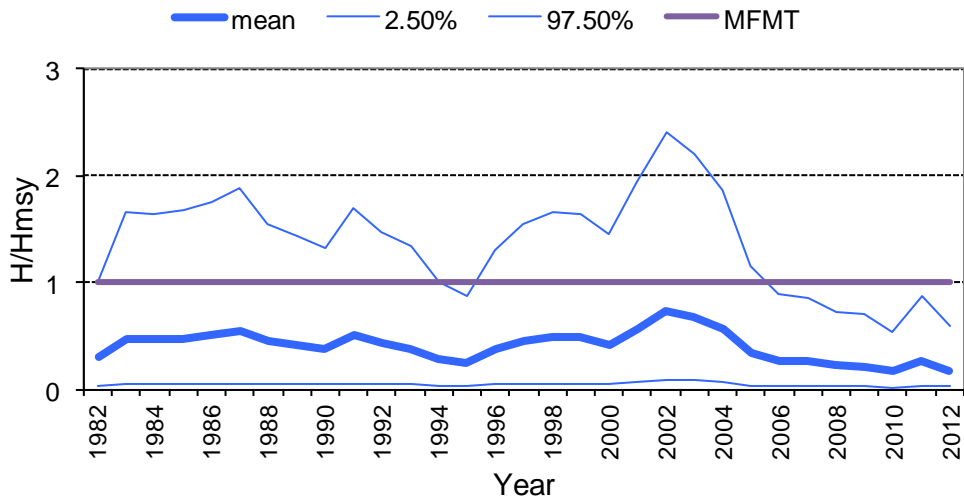
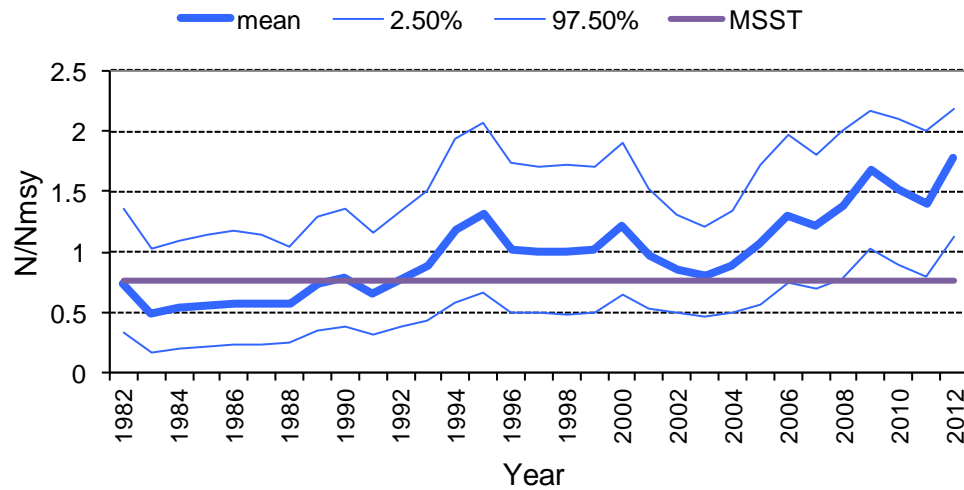
Model fit to SMALLPELTR series



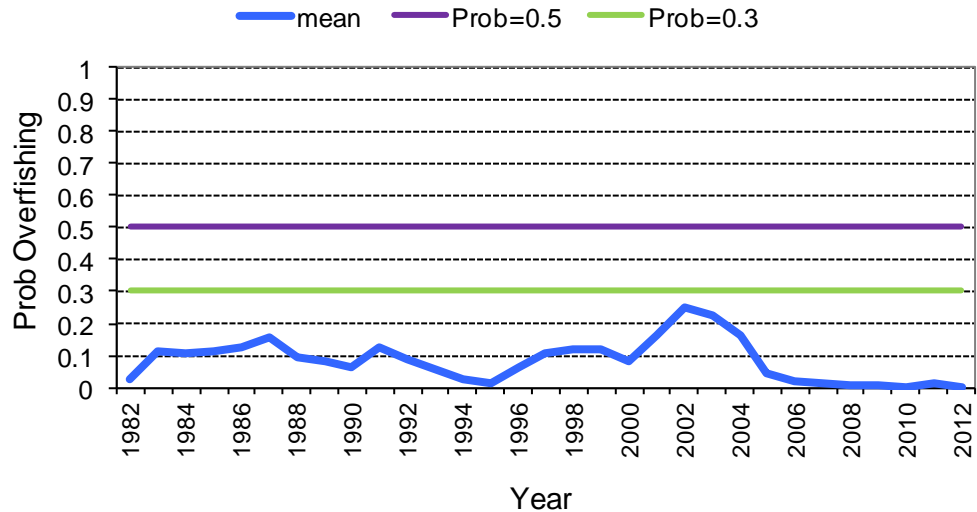
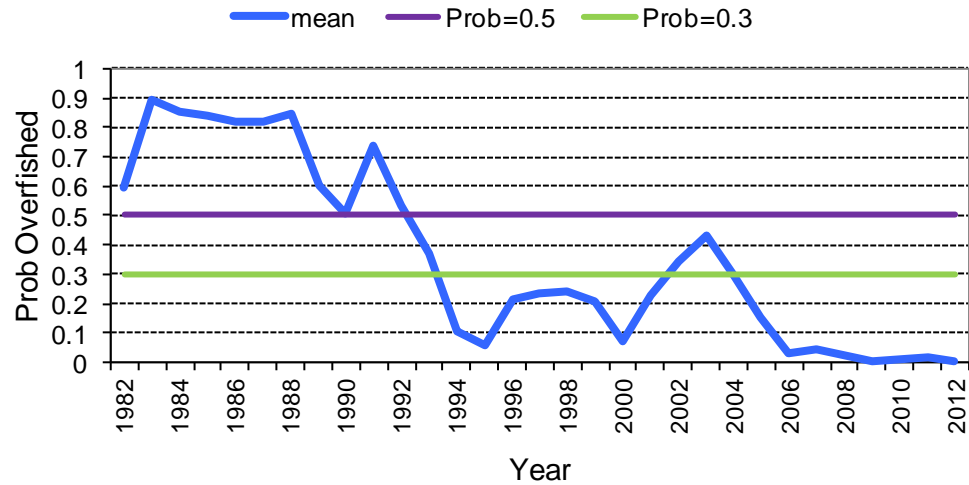
Predicted exploitable number (top) and exploitation rate (bottom) trajectories (with 95% credible intervals) for the base run



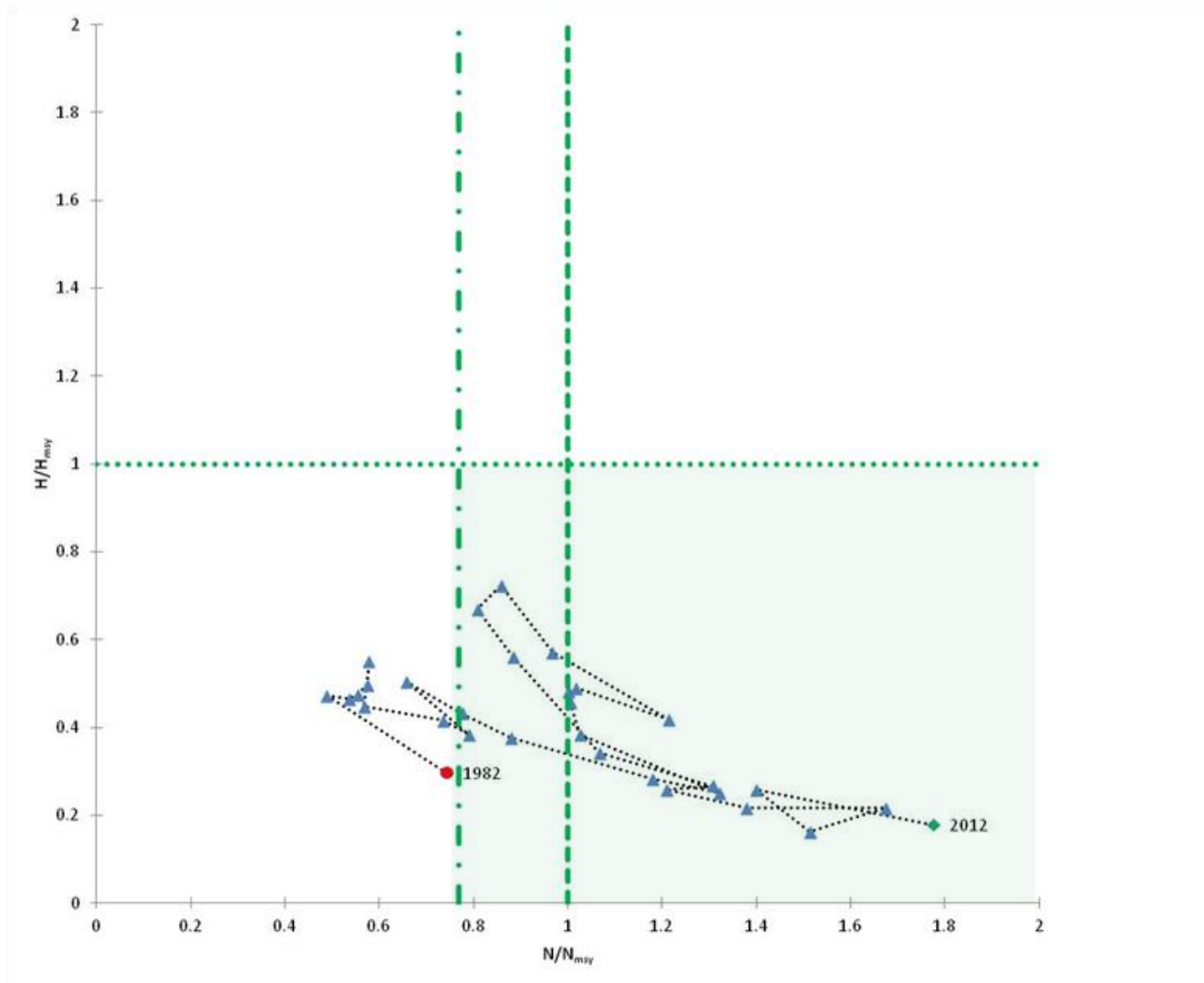
Predicted relative exploitable number (top) and relative exploitation rate (bottom) trajectories (with 95% credible intervals) for the base



Probability of exploitable number being smaller than MSST (overfished condition; top) and probability of exploitation rate being larger than H_{MSY} (overfishing condition; bottom) for the base run



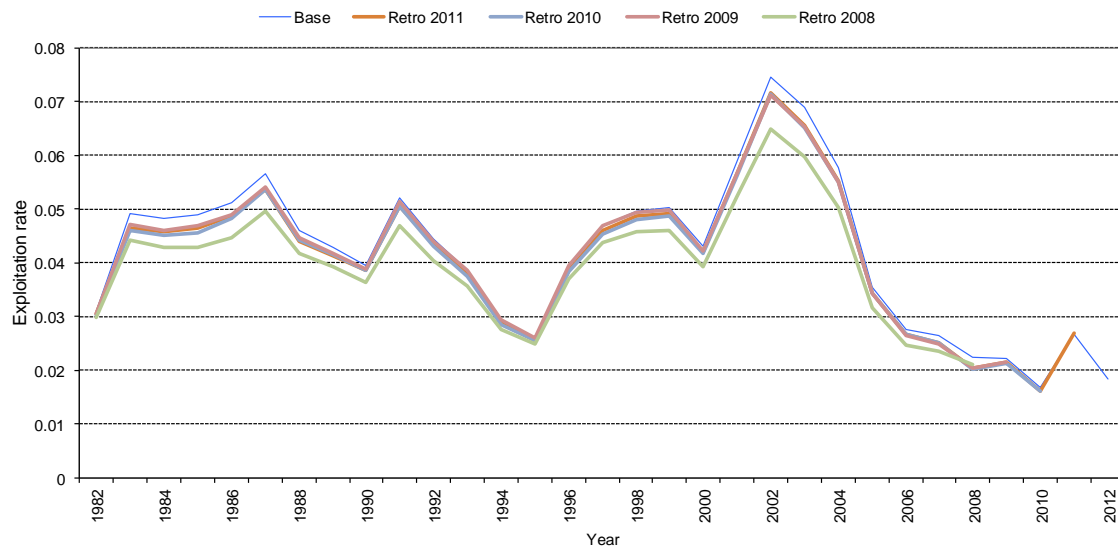
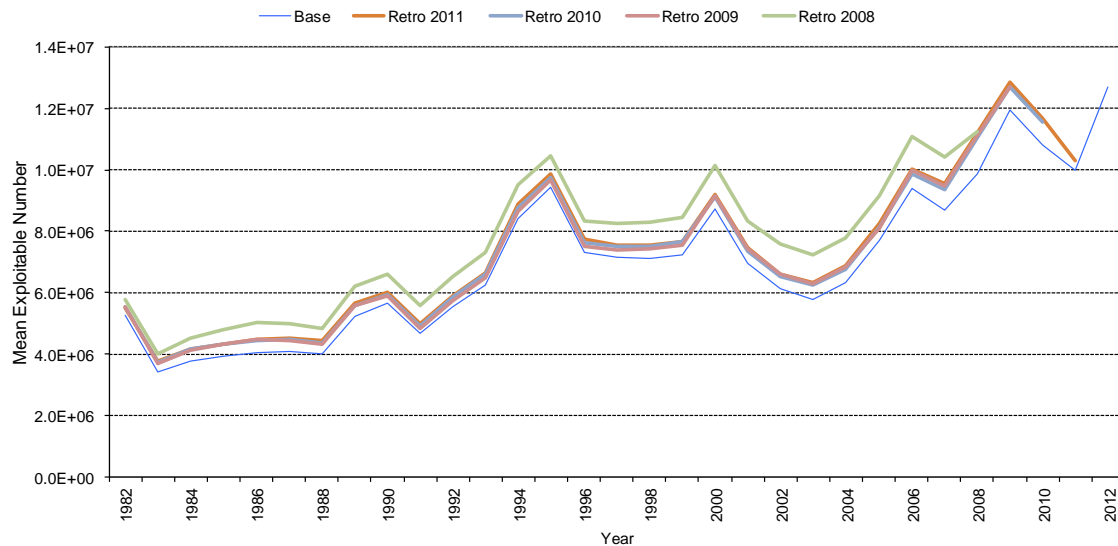
Combined relative exploitable number and relative exploitation rate trajectory for the base run



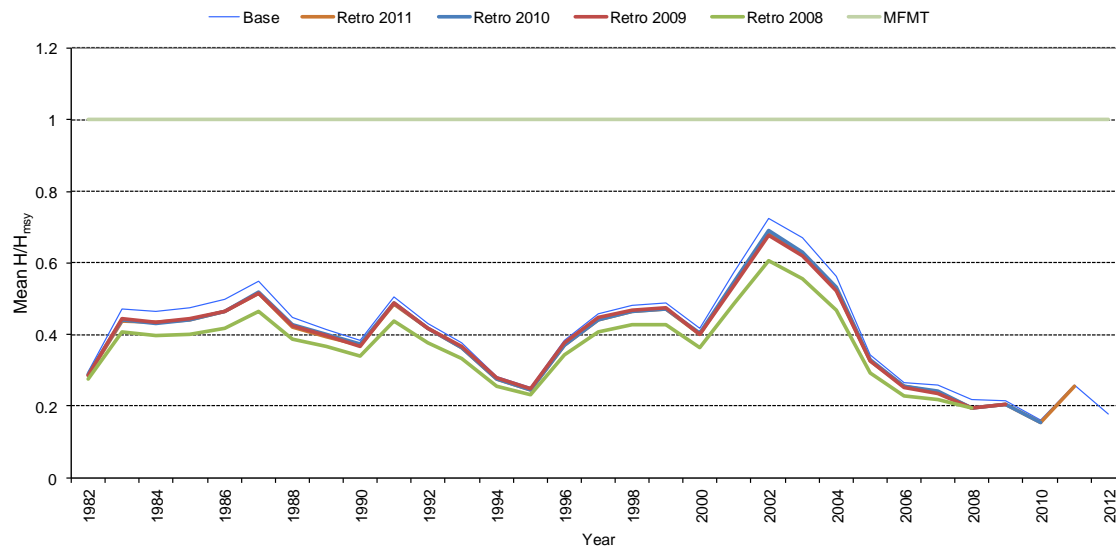
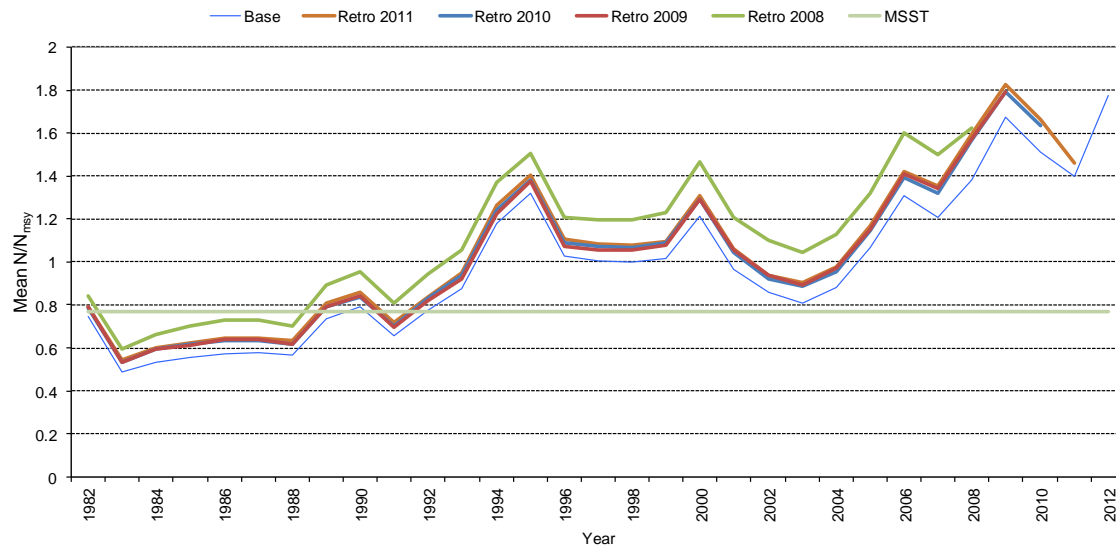
Summary of results (mean and CV) for base model

| Run | Base | |
|--|--------------|-------------|
| | Mean | CV |
| K | 1.44E+07 | 0.88 |
| r | 0.212 | 0.40 |
| MSY | 6.89E+05 | 0.95 |
| N ₂₀₁₂ | 1.27E+07 | 0.90 |
| H ₂₀₁₂ | 0.018 | 0.96 |
| N ₂₀₁₃ ratio | 0.787 | 0.24 |
| N ₁₉₈₂ | 5.28E+06 | 0.98 |
| H₂₀₁₂/H_{MSY} | 0.179 | 0.89 |
| N₂₀₁₂/N_{MSY} | 1.776 | 0.16 |
| N _{MSY} | 7.19E+06 | 0.88 |
| H _{MSY} | 0.106 | 0.40 |
| P ₁₉₈₂ | 0.589 | 0.20 |
| MSST ((1-M)*N _{msy}) | 5.53E+06 | |
| Convergence diagnostics | | |
| Chain mixing | Good | |
| Autocorrelations | Low | |
| Gelman-Rubin | Good | |
| (MC error)/(posterior sd) | <5% | |
| Abundance index RMSE/(Index Mean) | | |
| NMFS SE Bottom LL | 0.269 | |
| NMFS SEAMAP Gr Tr (F) | 0.487 | |
| NMFS SEAMAP Gr Tr (S) | 0.487 | |
| NMFS Small Pel Tr | 0.210 | |

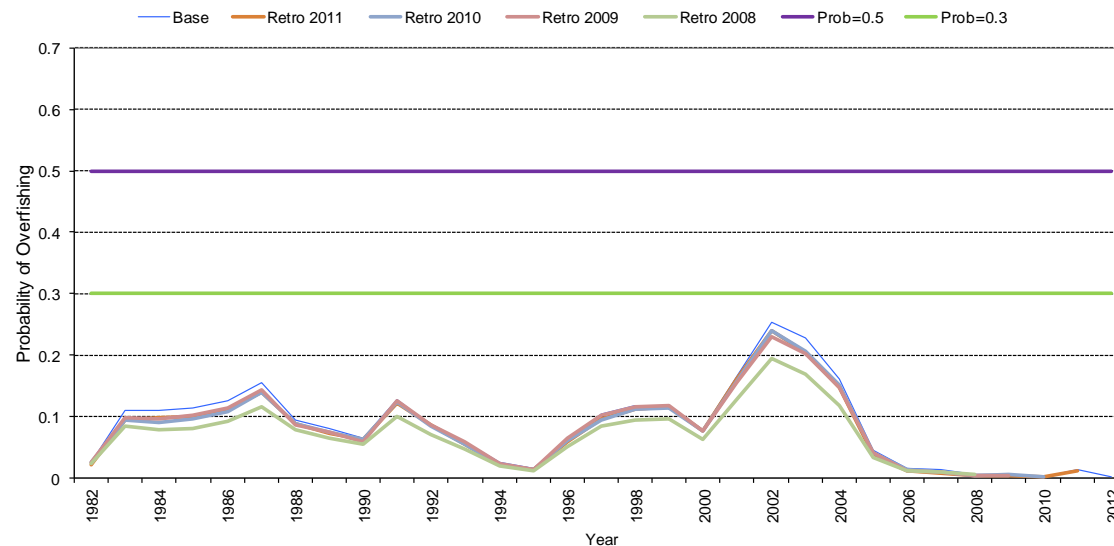
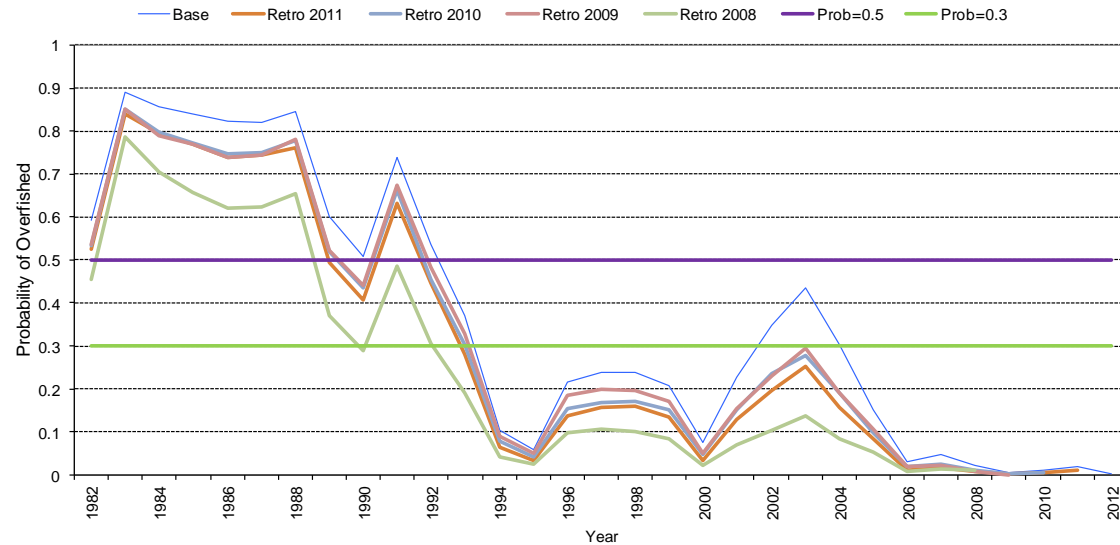
Predicted exploitable number (top) and exploitation rate (bottom) trajectories for the base model retrospective analysis



Predicted relative exploitable number (top) and relative exploitation rate (bottom) trajectories for the base model retrospective analysis



Probability of exploitable number being smaller than MSST (overfished condition) (top) and probability of exploitation rate being larger than H_{MSY} (bottom) for the base model retrospective analysis



Summary of results (mean and CV) for the base model retrospective runs

| Run | Base | | Retro2011 | | Retro2010 | | Retro2009 | | Retro2008 | |
|---|--------------------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|--------------|-------------|
| | Mean | CV | Mean | CV | Mean | CV | Mean | CV | Mean | CV |
| K | 1.44E+07 | 0.88 | 1.41E+07 | 0.90 | 1.42E+07 | 0.89 | 1.42E+07 | 0.90 | 1.39E+07 | 0.91 |
| r | 0.212 | 0.40 | 0.214 | 0.39 | 0.213 | 0.40 | 0.216 | 0.39 | 0.224 | 0.40 |
| MSY | 6.89E+05 | 0.95 | 6.84E+05 | 0.98 | 6.88E+05 | 0.97 | 7.00E+05 | 0.98 | 7.16E+05 | 1.00 |
| N _{cur} | 1.27E+07 | 0.90 | 1.03E+07 | 0.93 | 1.16E+07 | 0.92 | 1.27E+07 | 0.92 | 1.12E+07 | 0.95 |
| H _{2012cur} | 0.018 | 0.96 | 0.027 | 0.99 | 0.016 | 1.00 | 0.022 | 0.98 | 0.021 | 1.04 |
| N _{cur+1} ratio | 0.787 | 0.24 | 0.715 | 0.27 | 0.762 | 0.25 | 0.787 | 0.24 | 0.753 | 0.26 |
| N ₁₉₈₂ | 5.28E+06 | 0.98 | 5.52E+06 | 0.99 | 5.55E+06 | 1.00 | 5.53E+06 | 1.02 | 5.76E+06 | 1.01 |
| H _{cur} /H _{MSY} | 0.179 | 0.89 | 0.257 | 0.91 | 0.155 | 0.89 | 0.204 | 0.89 | 0.196 | 0.99 |
| N _{cur} /N _{MSY} | 1.776 | 0.16 | 1.462 | 0.20 | 1.635 | 0.19 | 1.794 | 0.16 | 1.622 | 0.21 |
| N _{MSY} | 7.19E+06 | 0.88 | 7.06E+06 | 0.90 | 7.10E+06 | 0.89 | 7.09E+06 | 0.90 | 6.95E+06 | 0.91 |
| H _{MSY} | 0.106 | 0.40 | 0.107 | 0.39 | 0.106 | 0.40 | 0.108 | 0.39 | 0.112 | 0.40 |
| P ₁₉₈₂ | 0.589 | 0.20 | 0.594 | 0.19 | 0.594 | 0.19 | 0.599 | 0.20 | 0.607 | 0.19 |
| MSST ((1-M)*N _{msy}) | 5.53E+06 | | 5.43E+06 | | 5.46E+06 | | 5.45E+06 | | 5.35E+06 | |
| Convergence diagnostics | | | | | | | | | | |
| Chain mixing | Good | | Good | | Good | | Good | | Good | |
| Autocorrelations | Low | | Low | | Low | | Low | | Low | |
| Gelman-Rubin | Good | | Good | | Good | | Good | | Good | |
| (MC error)/(posterior sd) | <5% | | <5% | | <5% | | <5% | | <5% | |
| Abundance index | | | | | | | | | | |
| | RMSE/(Index Mean) | | | | | | | | | |
| NMFS SE Bottom LL | 0.269 | | 0.311 | | 0.330 | | 0.358 | | 0.355 | |
| NMFS SEAMAP Gr Tr (F) | 0.487 | | 0.479 | | 0.481 | | 0.474 | | 0.518 | |
| NMFS SEAMAP Gr Tr (S) | 0.487 | | 0.513 | | 0.463 | | 0.477 | | 0.467 | |
| NMFS Small Pel Tr | 0.210 | | 0.131 | | 0.132 | | 0.150 | | 0.217 | |
| cur = 2012 for base, 2011 for Retro2011, 2010 for Retro2010, 2009 for Retro2009, and 2008 for Retro2008 | | | | | | | | | | |

Evaluation of uncertainty

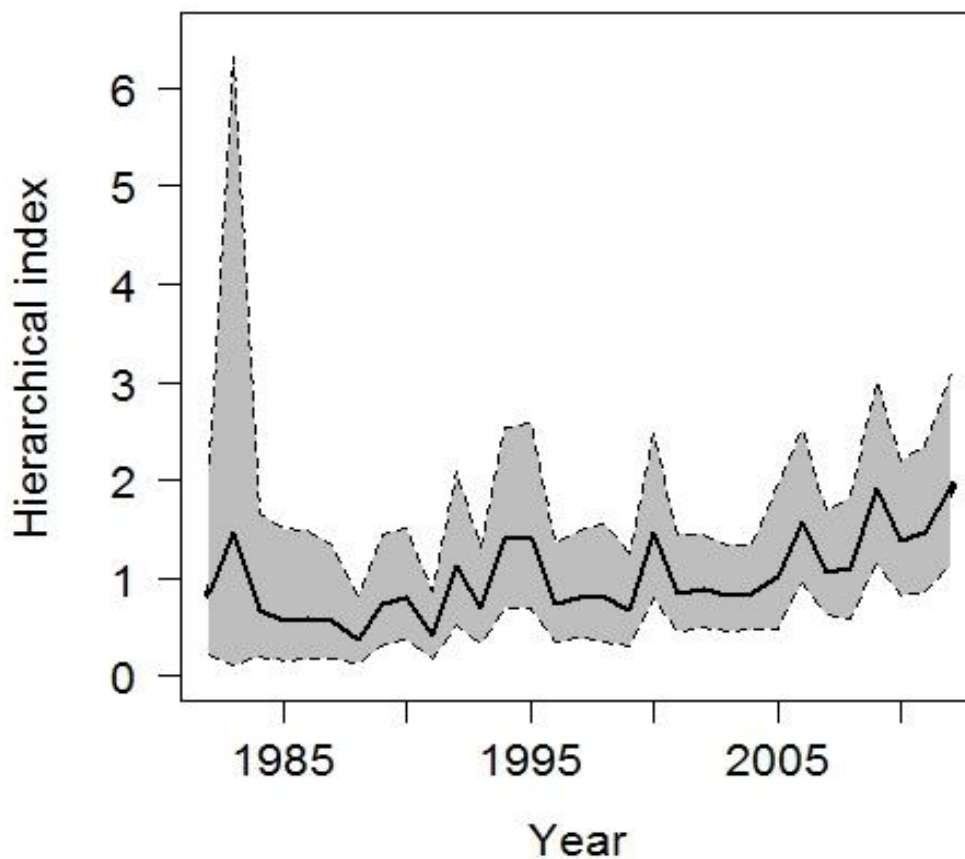
Different data inputs

- *Sensitivity run 1 (Hierarchical index)*
- *Sensitivity run 2 (Inverse CV weighting)*
- *Sensitivity runs 3 and 4 (Low and high catch)*

Same data inputs

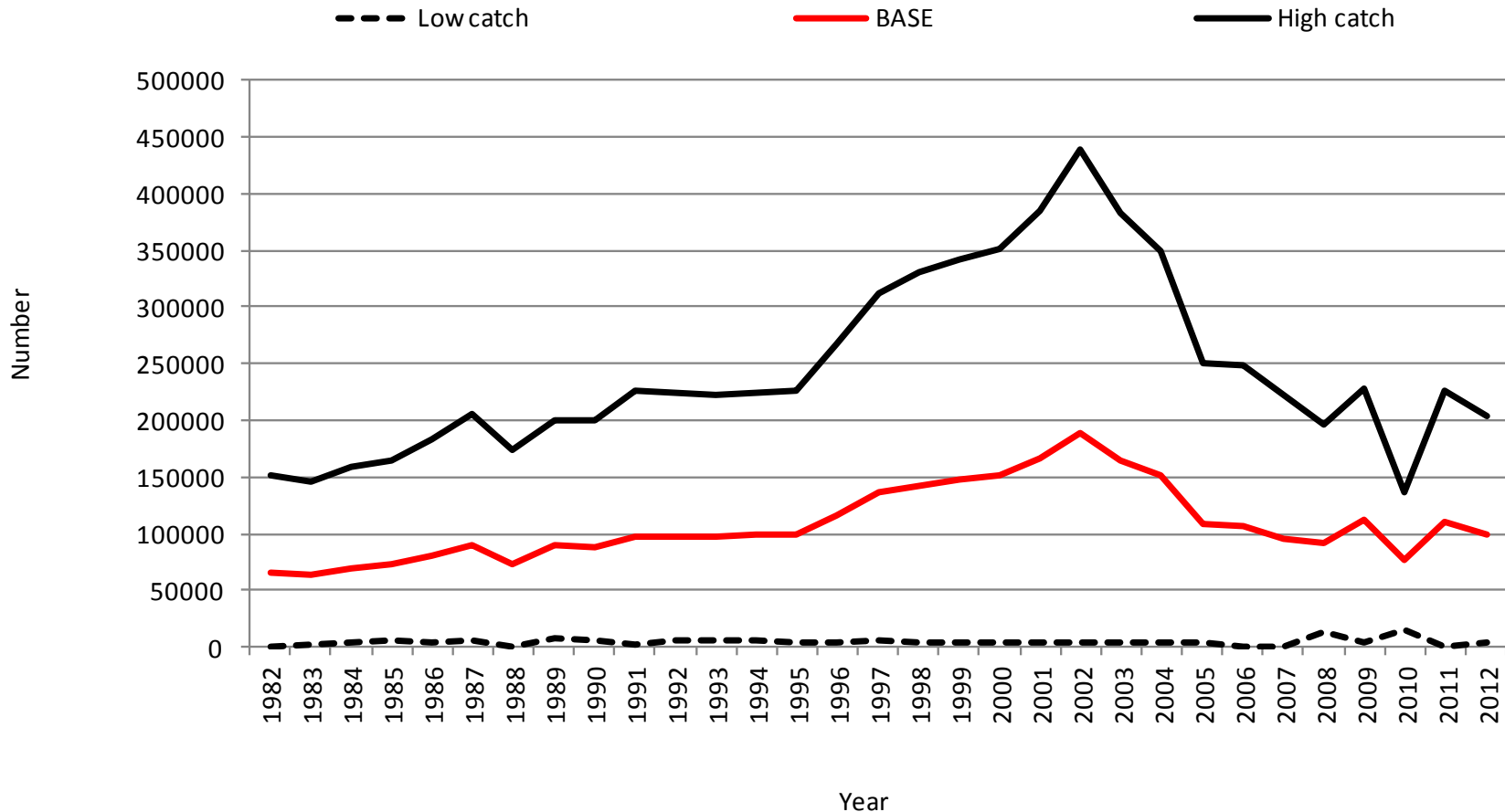
- *Sensitivity runs 5 and 6 (Low and high productivity)*
- *Sensitivity runs 7, 8, and 9 (Large process error variance, large observation error variance, and both simultaneously)*
- *Sensitivity runs 10 and 11 (High and low initial depletion)*
- *Sensitivity runs 12 and 13 (High and low carrying capacity)*

Hierarchical index of abundance used in sensitivity run 1

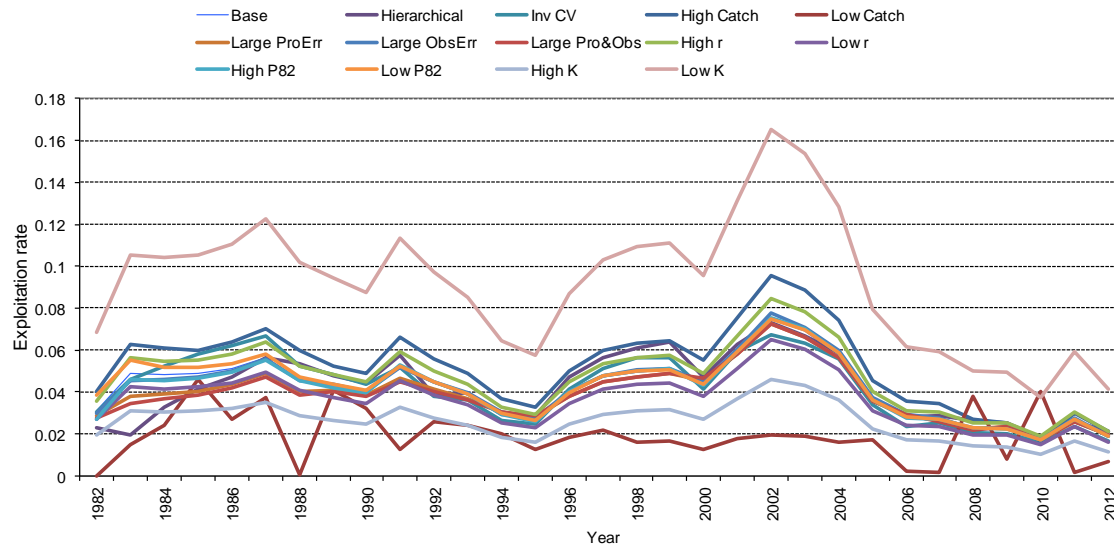
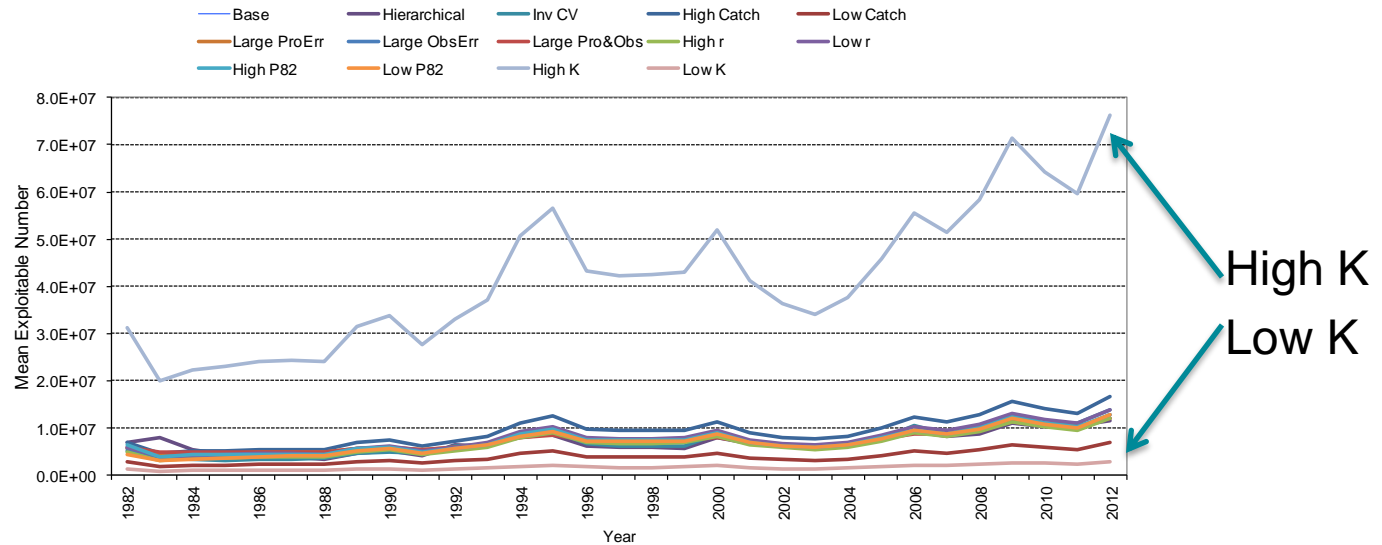


Low and high catches used in the low and high catch sensitivity runs (3 and 4)

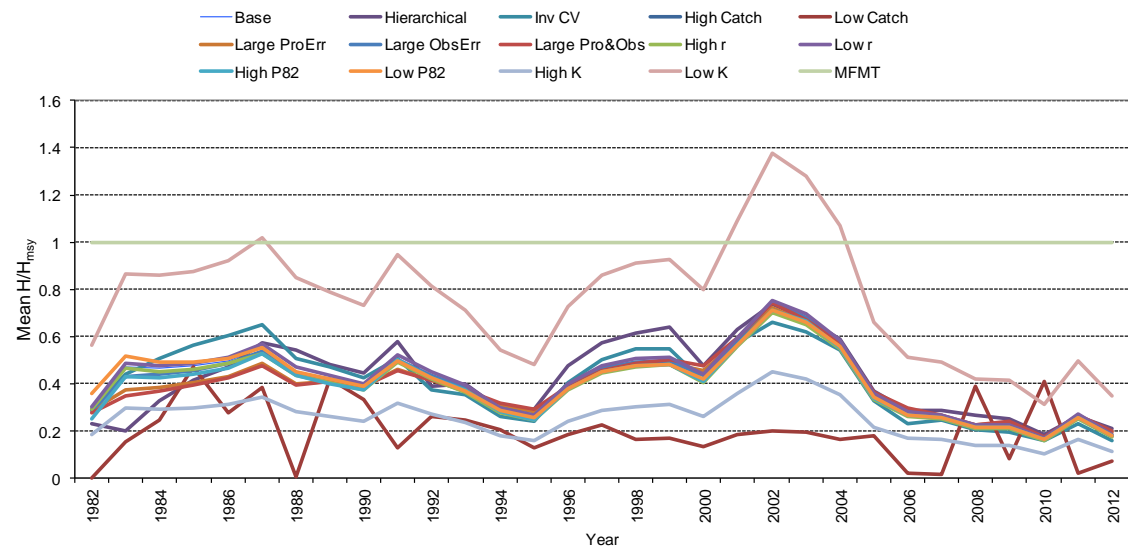
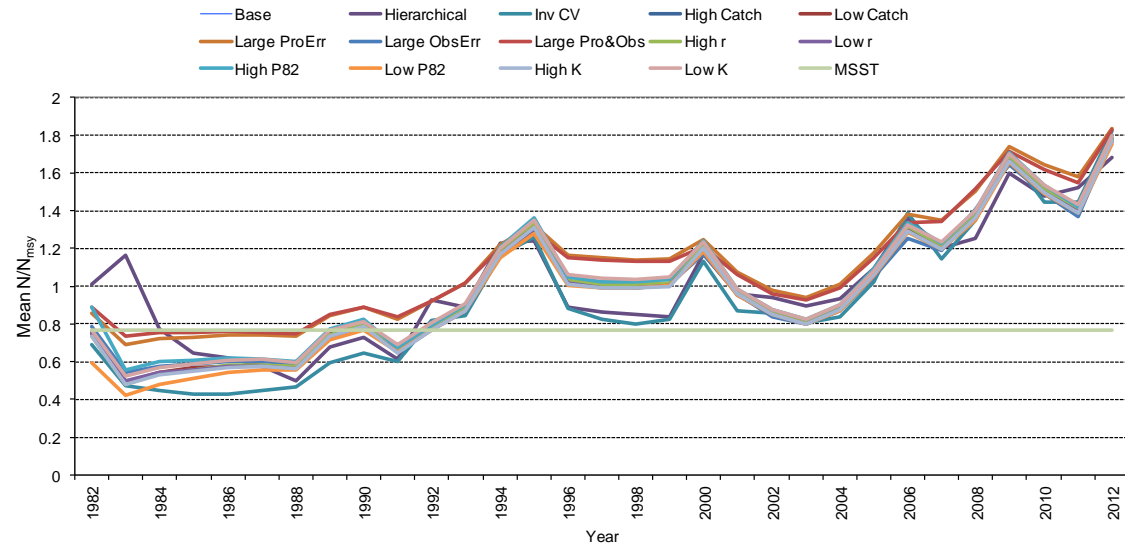
Mustelus complex catches (Gulf of Mexico): Low, Base, High catch scenarios



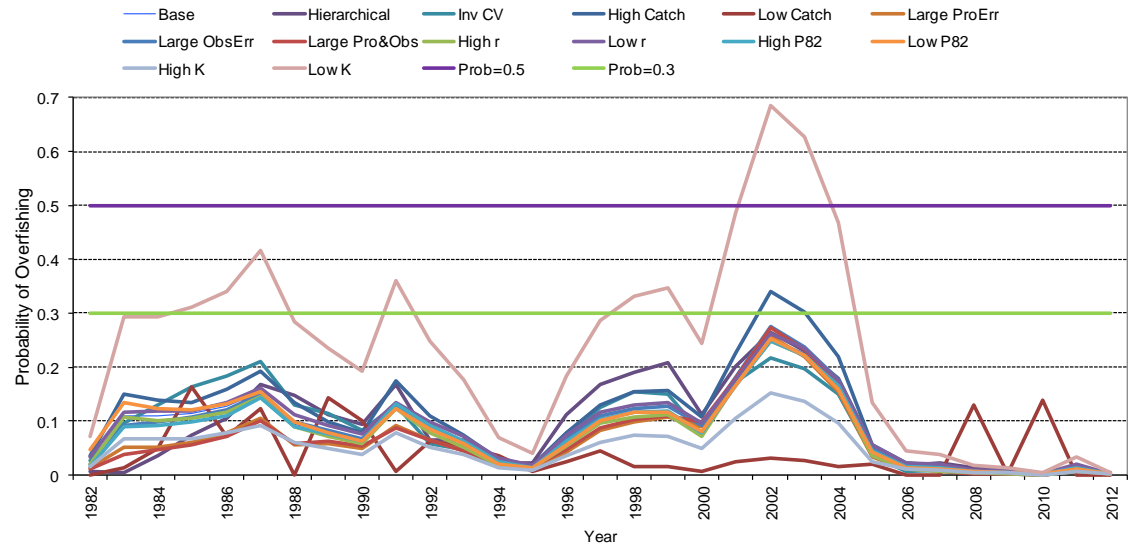
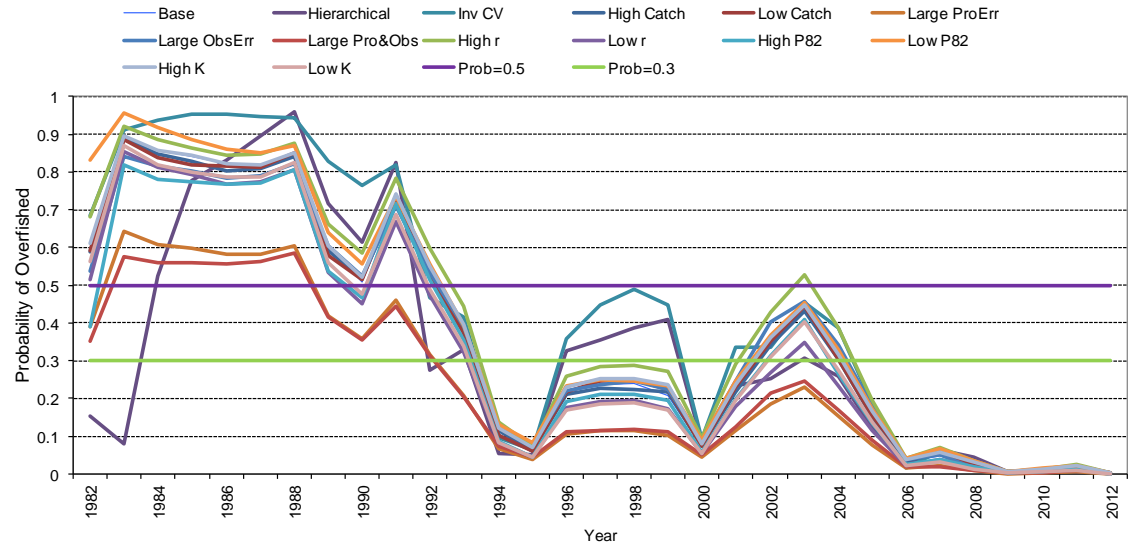
Predicted exploitable number (top) and exploitation rate (bottom) trajectories for each of the 13 sensitivity runs



Predicted relative exploitable number (top) and relative exploitation rate (bottom) trajectories for each of the 13 sensitivity runs



Probability of exploitable number being smaller than MSST (overfished condition; top) and probability of exploitation rate being larger than H_{MSY} (overfishing condition; bottom) for each of the 13 sensitivity runs



Summary of results (mean and CV) for sensitivity runs 1-4

| Run | Base | | Hierarchical | | Inv CV | | Low Catch | | High Catch | |
|-------------------------------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|
| | Mean | CV | Mean | CV | Mean | CV | Mean | CV | Mean | CV |
| K | 1.44E+07 | 0.88 | 1.37E+07 | 0.90 | 1.52E+07 | 0.84 | 7.65E+06 | 1.50 | 1.88E+07 | 0.67 |
| r | 0.212 | 0.40 | 0.204 | 0.40 | 0.210 | 0.39 | 0.195 | 0.39 | 0.223 | 0.39 |
| MSY | 6.89E+05 | 0.95 | 6.27E+05 | 0.98 | 7.21E+05 | 0.90 | 3.48E+05 | 1.64 | 9.61E+05 | 0.74 |
| N ₂₀₁₂ | 1.27E+07 | 0.90 | 1.15E+07 | 0.94 | 1.38E+07 | 0.86 | 6.77E+06 | 1.54 | 1.67E+07 | 0.70 |
| H ₂₀₁₂ | 0.018 | 0.96 | 0.021 | 0.97 | 0.016 | 0.97 | 0.007 | 1.60 | 0.021 | 0.81 |
| N ₂₀₁₃ ratio | 0.787 | 0.24 | 0.767 | 0.24 | 0.789 | 0.23 | 0.790 | 0.24 | 0.785 | 0.24 |
| N ₁₉₈₂ | 5.28E+06 | 0.98 | 6.84E+06 | 0.95 | 5.16E+06 | 0.95 | 2.77E+06 | 1.61 | 6.95E+06 | 0.79 |
| H ₂₀₁₂ /H _{MSY} | 0.179 | 0.89 | 0.211 | 0.89 | 0.159 | 0.87 | 0.071 | 1.51 | 0.196 | 0.73 |
| N ₂₀₁₂ /N _{MSY} | 1.776 | 0.16 | 1.680 | 0.19 | 1.826 | 0.15 | 1.776 | 0.17 | 1.778 | 0.16 |
| N _{MSY} | 7.19E+06 | 0.88 | 6.84E+06 | 0.90 | 7.60E+06 | 0.84 | 3.82E+06 | 1.50 | 9.42E+06 | 0.67 |
| H _{MSY} | 0.106 | 0.40 | 0.102 | 0.40 | 0.105 | 0.39 | 0.098 | 0.39 | 0.112 | 0.39 |
| P ₁₉₈₂ | 0.589 | 0.20 | 0.638 | 0.18 | 0.584 | 0.20 | 0.590 | 0.20 | 0.588 | 0.20 |
| MSST ((1-M)*N _{msy}) | 5.53E+06 | | 5.26E+06 | | 5.84E+06 | | 2.94E+06 | | 7.24E+06 | |
| Convergence diagnostics | | | | | | | | | | |
| Chain mixing | Good | | Good | | Good | | Good | | Good | |
| Autocorrelations | Low | | Low | | Low | | Low | | Low | |
| Gelman-Rubin | Good | | Good | | Good | | Good | | Good | |
| (MC error)/(posterior sd) | <5% | | <5% | | <5% | | <5% | | <5% | |
| Abundance Index | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | |
| NMFS SE Bottom LL | 0.269 | | | | 0.260 | | 0.272 | | 0.268 | |
| NMFS SEAMAP Gr Tr (F) | 0.487 | | | | 0.478 | | 0.485 | | 0.488 | |
| NMFS SEAMAP Gr Tr (S) | 0.487 | | | | 0.431 | | 0.488 | | 0.489 | |
| NMFS Small Pel Tr | 0.210 | | | | 0.212 | | 0.207 | | 0.210 | |
| Hierarchical | | | 0.099 | | | | | | | |

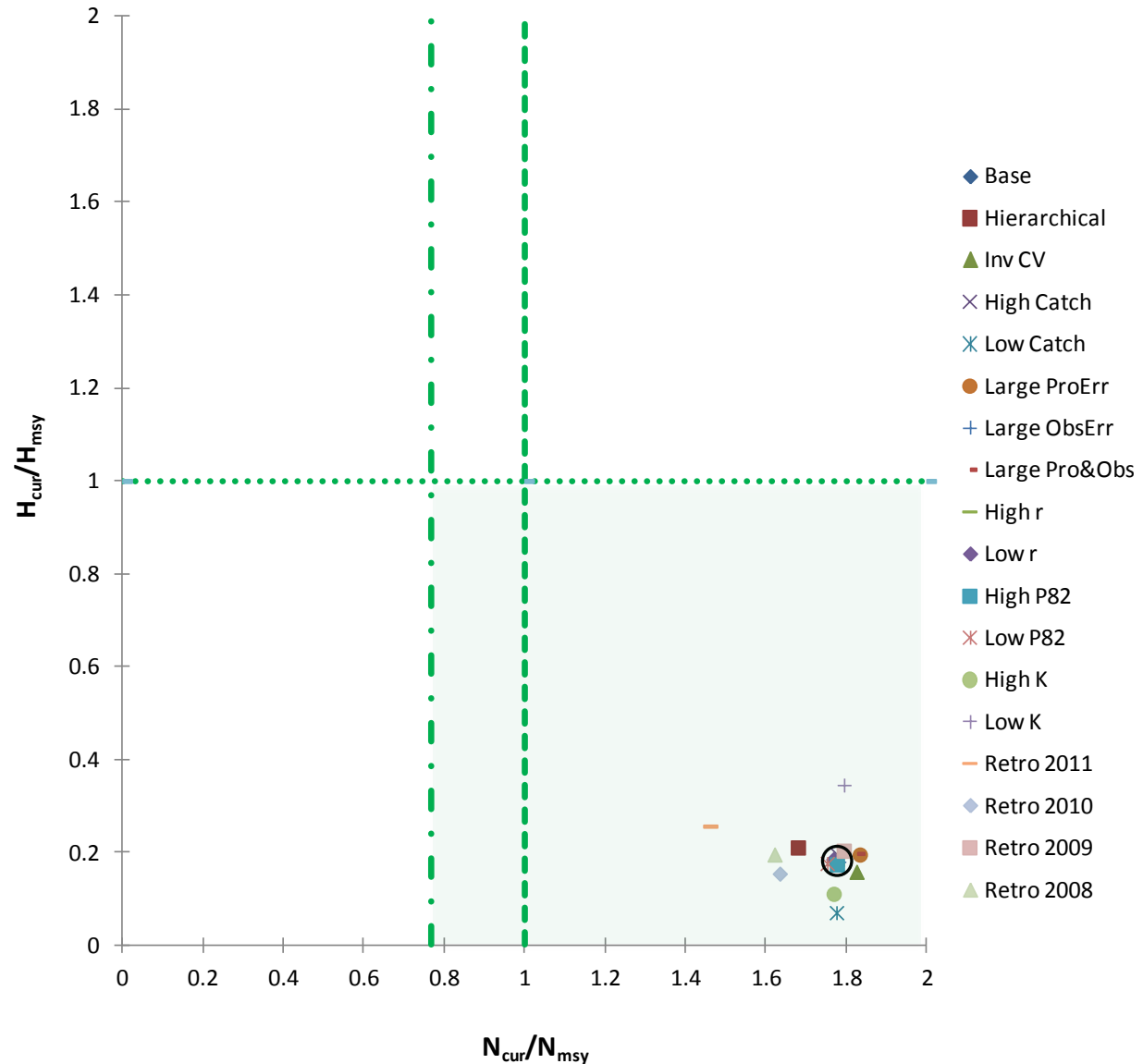
Summary of results (mean and CV) for sensitivity runs 5-13

| Run | Base | | Low r | | High r | | Large ProErr | | Large ObsErr | | Large Pro&Obs | |
|-------------------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| | Mean | CV | Mean | CV | Mean | CV | Mean | CV | Mean | CV | Mean | CV |
| K | 1.44E+07 | 0.88 | 1.58E+07 | 0.82 | 1.34E+07 | 0.93 | 1.30E+07 | 0.93 | 1.44E+07 | 0.89 | 1.31E+07 | 0.93 |
| r | 0.212 | 0.40 | 0.182 | 0.42 | 0.241 | 0.37 | 0.199 | 0.40 | 0.210 | 0.39 | 0.195 | 0.40 |
| MSY | 6.89E+05 | 0.95 | 6.59E+05 | 0.92 | 7.28E+05 | 1.00 | 5.70E+05 | 0.98 | 6.80E+05 | 0.96 | 5.61E+05 | 0.98 |
| N ₂₀₁₂ | 1.27E+07 | 0.90 | 1.39E+07 | 0.85 | 1.19E+07 | 0.96 | 1.20E+07 | 0.95 | 1.27E+07 | 0.91 | 1.20E+07 | 0.95 |
| H ₂₀₁₂ | 0.018 | 0.96 | 0.016 | 0.99 | 0.021 | 0.97 | 0.020 | 0.93 | 0.019 | 0.97 | 0.020 | 0.92 |
| N ₂₀₁₃ ratio | 0.787 | 0.24 | 0.785 | 0.24 | 0.736 | 0.35 | 0.848 | 0.19 | 0.793 | 0.23 | 0.847 | 0.19 |
| N ₁₉₈₂ | 5.28E+06 | 0.98 | 5.85E+06 | 0.93 | 4.85E+06 | 1.04 | 5.48E+06 | 1.00 | 5.56E+06 | 0.99 | 5.72E+06 | 1.00 |
| H ₂₀₁₂ /H _{MSY} | 0.179 | 0.89 | 0.186 | 0.92 | 0.175 | 0.86 | 0.196 | 0.79 | 0.180 | 0.87 | 0.198 | 0.77 |
| N ₂₀₁₂ /N _{MSY} | 1.776 | 0.16 | 1.768 | 0.17 | 1.777 | 0.16 | 1.834 | 0.14 | 1.782 | 0.16 | 1.828 | 0.14 |
| N _{MSY} | 7.19E+06 | 0.88 | 7.90E+06 | 0.82 | 6.71E+06 | 0.93 | 6.51E+06 | 0.93 | 7.19E+06 | 0.89 | 6.57E+06 | 0.93 |
| H _{MSY} | 0.106 | 0.40 | 0.091 | 0.42 | 0.120 | 0.37 | 0.099 | 0.40 | 0.105 | 0.39 | 0.097 | 0.40 |
| P ₁₉₈₂ | 0.589 | 0.20 | 0.588 | 0.19 | 0.587 | 0.20 | 0.562 | 0.20 | 0.593 | 0.19 | 0.568 | 0.20 |
| MSST ((1-M)*N _{msy}) | 5.53E+06 | | 6.08E+06 | | 5.16E+06 | | 5.01E+06 | | 5.53E+06 | | 5.05E+06 | |
| Convergence diagnostics | | | | | | | | | | | | |
| Chain mixing | Good | | Good | | Good | | Good | | Good | | Good | |
| Autocorrelations | Low | | Low | | Low | | Low | | Low | | Low | |
| Gelman-Rubin | Good | | Good | | Good | | Good | | Good | | Good | |
| (MC error)/(posterior sd) | <5% | | <5% | | <5% | | <5% | | <5% | | <5% | |
| Abundance index | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) | RMSE/(Index Mean) |
| NMFS SE Bottom LL | 0.269 | | 0.268 | | 0.268 | | 0.275 | | 0.282 | | 0.284 | |
| NMFS SEAMAP Gr Tr (F) | 0.487 | | 0.487 | | 0.485 | | 0.514 | | 0.494 | | 0.517 | |
| NMFS SEAMAP Gr Tr (S) | 0.487 | | 0.487 | | 0.486 | | 0.525 | | 0.501 | | 0.535 | |
| NMFS Small Pel Tr | 0.210 | | 0.209 | | 0.211 | | 0.235 | | 0.194 | | 0.226 | |
| DIC for model comparison | -197.906 | | -197.973 | | -197.571 | | -196.532 | | -195.252 | | -194.221 | |

Summary of results (mean and CV) for sensitivity runs 5-13 (Continued)

| Run | Base | | High P ₈₂ | | Low P ₈₂ | | High K | | Low K | |
|-------------------------------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|--------------------------|-------------|
| | Mean | CV | Mean | CV | Mean | CV | Mean | CV | Mean | CV |
| K | 1.44E+07 | 0.88 | 1.43E+07 | 0.88 | 1.45E+07 | 0.88 | 8.61E+07 | 1.38 | 3.11E+06 | 0.33 |
| r | 0.212 | 0.40 | 0.215 | 0.40 | 0.214 | 0.39 | 0.201 | 0.40 | 0.260 | 0.35 |
| MSY | 6.89E+05 | 0.95 | 6.97E+05 | 0.96 | 7.03E+05 | 0.94 | 3.96E+06 | 1.51 | 1.93E+05 | 0.40 |
| N ₂₀₁₂ | 1.27E+07 | 0.90 | 1.29E+07 | 0.91 | 1.27E+07 | 0.90 | 7.62E+07 | 1.42 | 2.78E+06 | 0.36 |
| H ₂₀₁₂ | 0.018 | 0.96 | 0.019 | 1.00 | 0.019 | 0.97 | 0.012 | 1.44 | 0.042 | 0.44 |
| N ₂₀₁₃ ratio | 0.787 | 0.24 | 0.786 | 0.24 | 0.789 | 0.23 | 0.786 | 0.24 | 0.786 | 0.23 |
| N ₁₉₈₂ | 5.28E+06 | 0.98 | 6.25E+06 | 0.99 | 4.25E+06 | 0.97 | 3.11E+07 | 1.51 | 1.19E+06 | 0.47 |
| H ₂₀₁₂ /H _{MSY} | 0.179 | 0.89 | 0.179 | 0.91 | 0.177 | 0.88 | 0.111 | 1.31 | 0.345 | 0.47 |
| N ₂₀₁₂ /N _{MSY} | 1.776 | 0.16 | 1.796 | 0.15 | 1.753 | 0.17 | 1.769 | 0.17 | 1.795 | 0.15 |
| N _{MSY} | 7.19E+06 | 0.88 | 7.17E+06 | 0.89 | 7.26E+06 | 0.88 | 4.30E+07 | 1.38 | 1.56E+06 | 0.33 |
| H _{MSY} | 0.106 | 0.40 | 0.107 | 0.40 | 0.107 | 0.39 | 0.101 | 0.40 | 0.130 | 0.35 |
| P ₁₉₈₂ | 0.589 | 0.20 | 0.740 | 0.18 | 0.430 | 0.20 | 0.588 | 0.20 | 0.590 | 0.20 |
| MSST ((1-M)*N _{msy}) | 5.53E+06 | | 5.51E+06 | | 5.58E+06 | | 3.31E+07 | | 1.20E+06 | |
| Convergence diagnostics | | | | | | | | | | |
| Chain mixing | Good | | Good | | Good | | Good | | Good | |
| Autocorrelations | Low | | Low | | Low | | Low | | Low | |
| Gelman-Rubin | Good | | Good | | Good | | Good | | Good | |
| (MC error)/(posterior sd) | <5% | | <5% | | <5% | | <5% | | <5% | |
| Abundance index | | | | | | | | | | |
| | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | | RMSE/(Index Mean) | |
| NMFS SE Bottom LL | 0.269 | | 0.269 | | 0.268 | | 0.268 | | 0.269 | |
| NMFS SEAMAP Gr Tr (F) | 0.487 | | 0.485 | | 0.487 | | 0.487 | | 0.490 | |
| NMFS SEAMAP Gr Tr (S) | 0.487 | | 0.498 | | 0.485 | | 0.485 | | 0.495 | |
| NMFS Small Pel Tr | 0.210 | | 0.213 | | 0.208 | | 0.208 | | 0.213 | |
| DIC for model comparison | -197.906 | | -195.799 | | -199.297 | | -197.855 | | -197.843 | |

Phase plot of Gulf of Mexico *Mustelus* spp. complex stock status for all runs



Probability of exploitable number being smaller than MSST (overfished condition) (top) and probability of exploitation rate being larger than H_{MSY} (bottom) for all runs

